

# Double-Sided Incremental Forming

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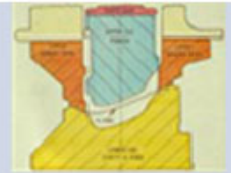
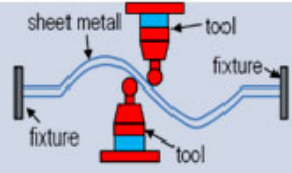
# LOW VOLUME SHEET METAL PRODUCTION

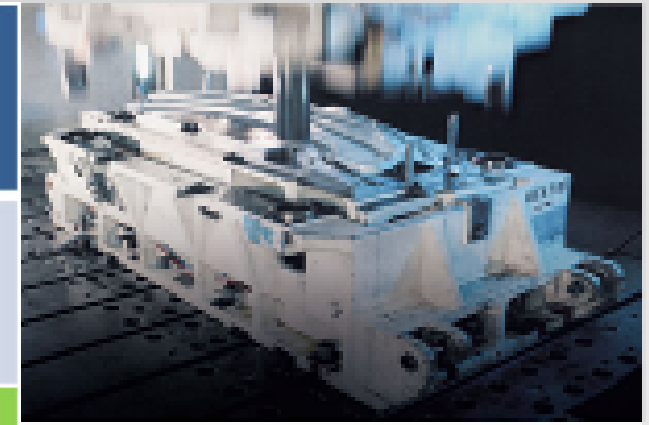
## AEROSPACE PRODUCTION



## AUTOMOTIVE DESIGN & PROTOTYPING



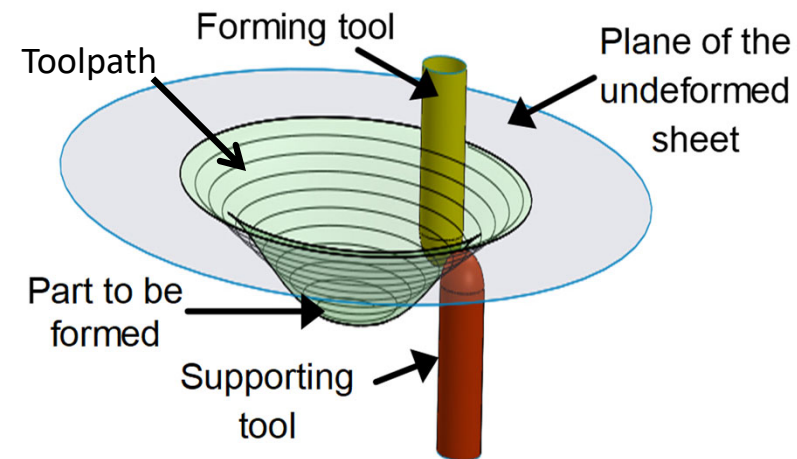
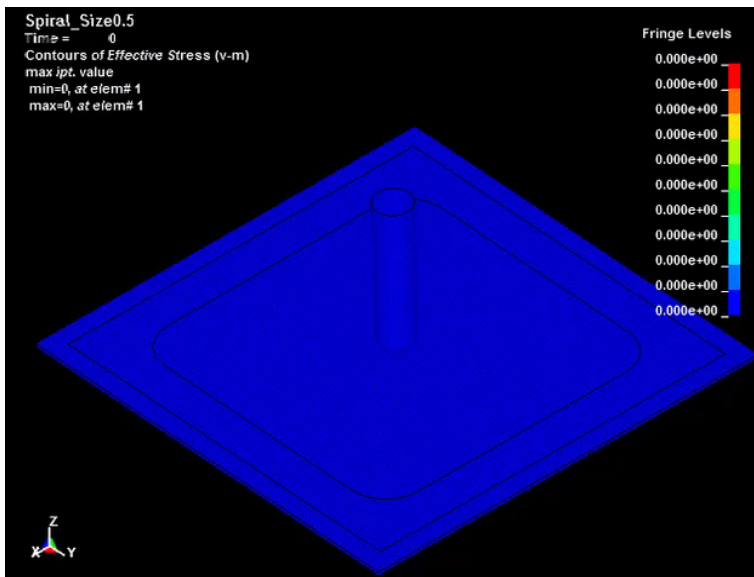
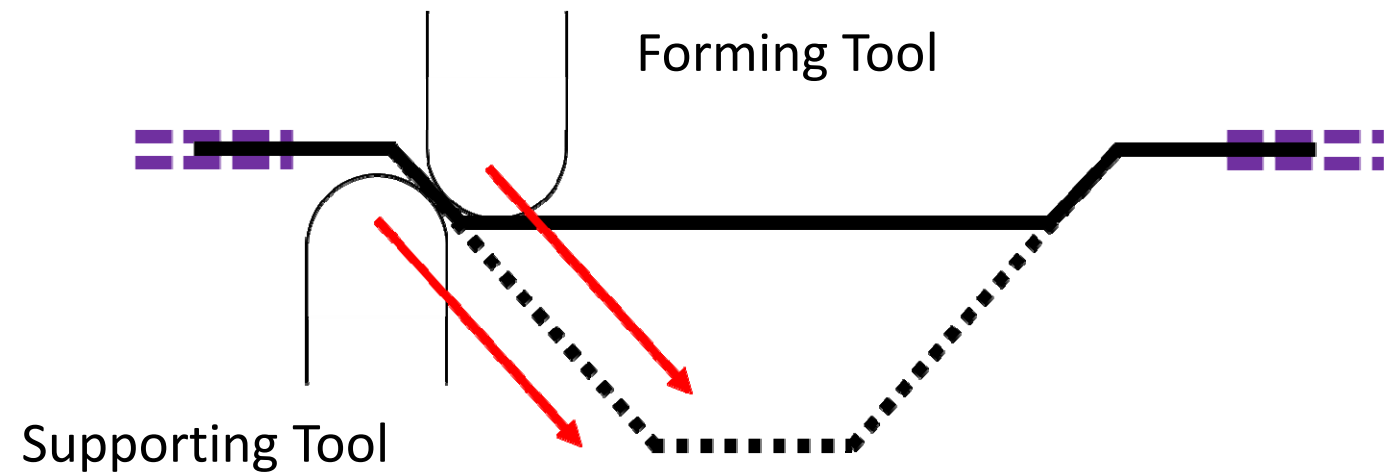
	TRADITIONAL PROCESSES	DSIF
		
TOOLING COST	\$100K - \$1M	NEGLIGIBLE
DESIGN TO PRODUCTION	8 - 15 WEEKS	< 1 WEEK
FACILITY SIZE & COMPLEXITY	HIGH	LOW
TOOLING STORAGE	REQUIRED	NONE
MATERIAL CHOICE	LIMITED	BROAD



# Potential Applications

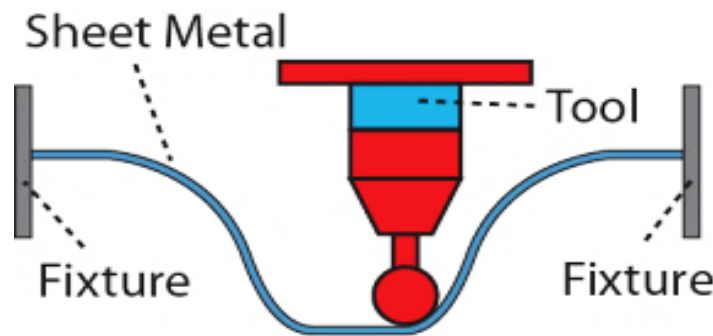


# Double-Sided Incremental Forming (DSIF)



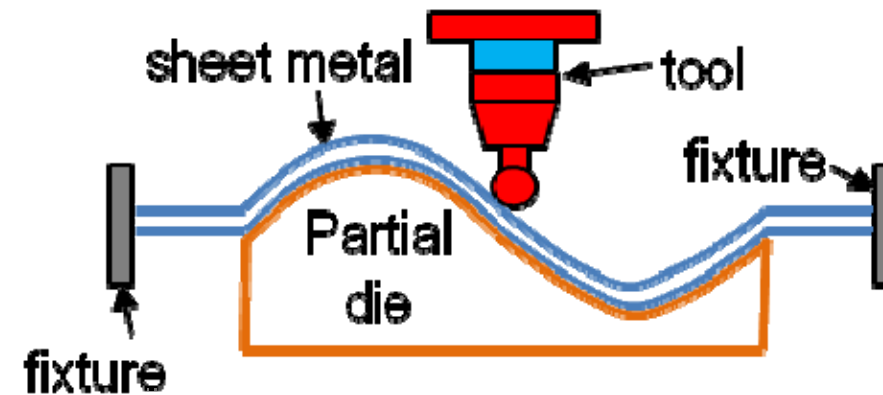
# Common Configurations of Incremental Sheet Forming

## Single-Point Incremental Forming (SPIF)



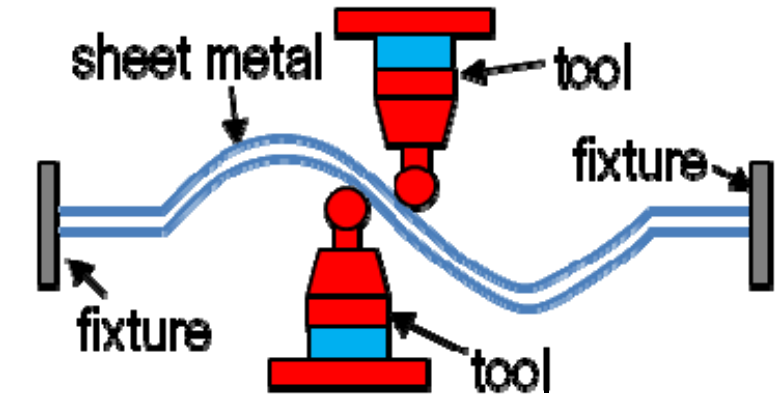
- Highly flexible manufacturing process
- Energy efficient for low-batch production
- High formability

## Two-Point Incremental Forming (TPIF)



- Utilizes a partial die or support post
- Increased geometric accuracy, but with less flexibility

## Double-Sided Incremental Forming (DSIF)

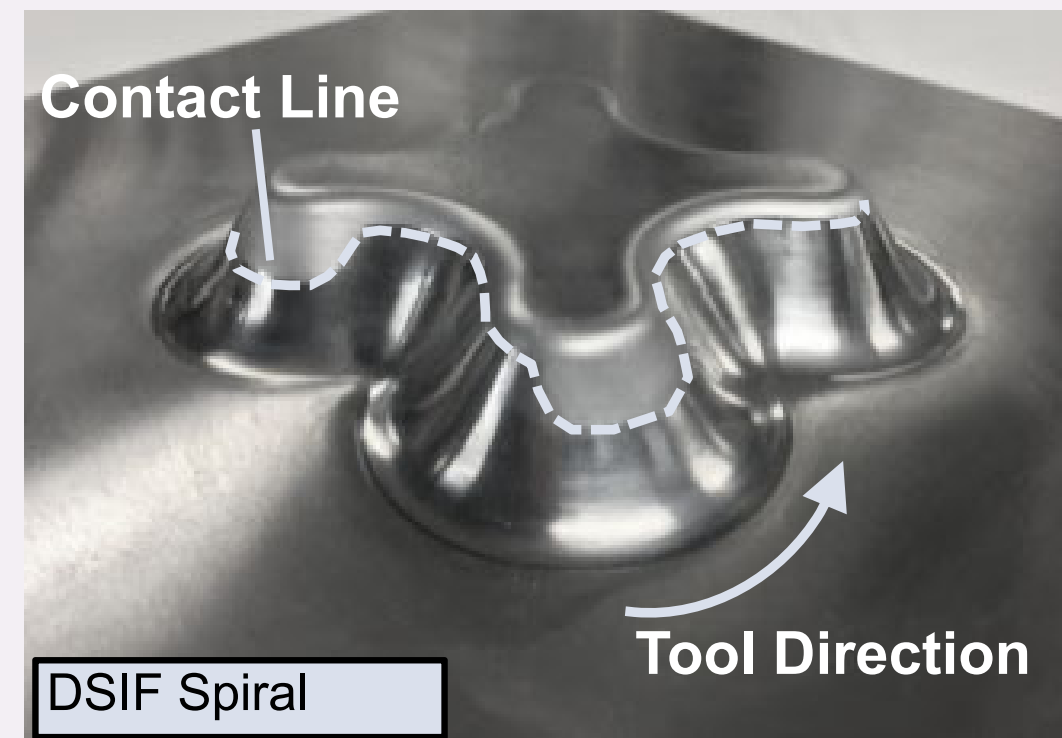
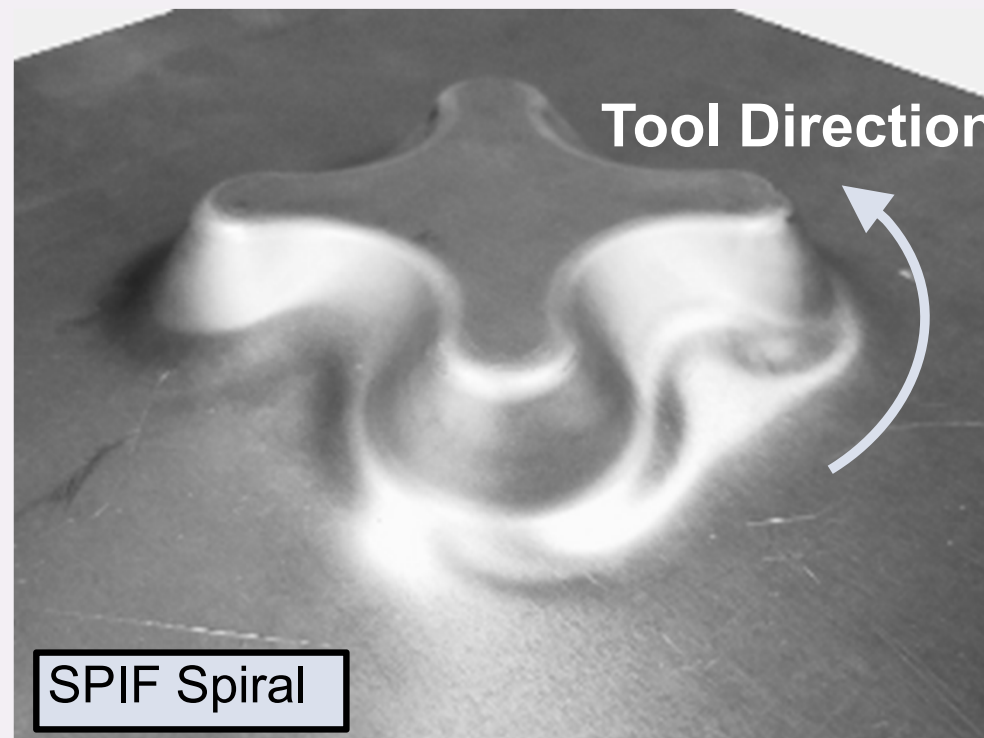


- Increased process control and accuracy, and still dieless
- Can form material above and below the sheet

# SPIF

# vs.

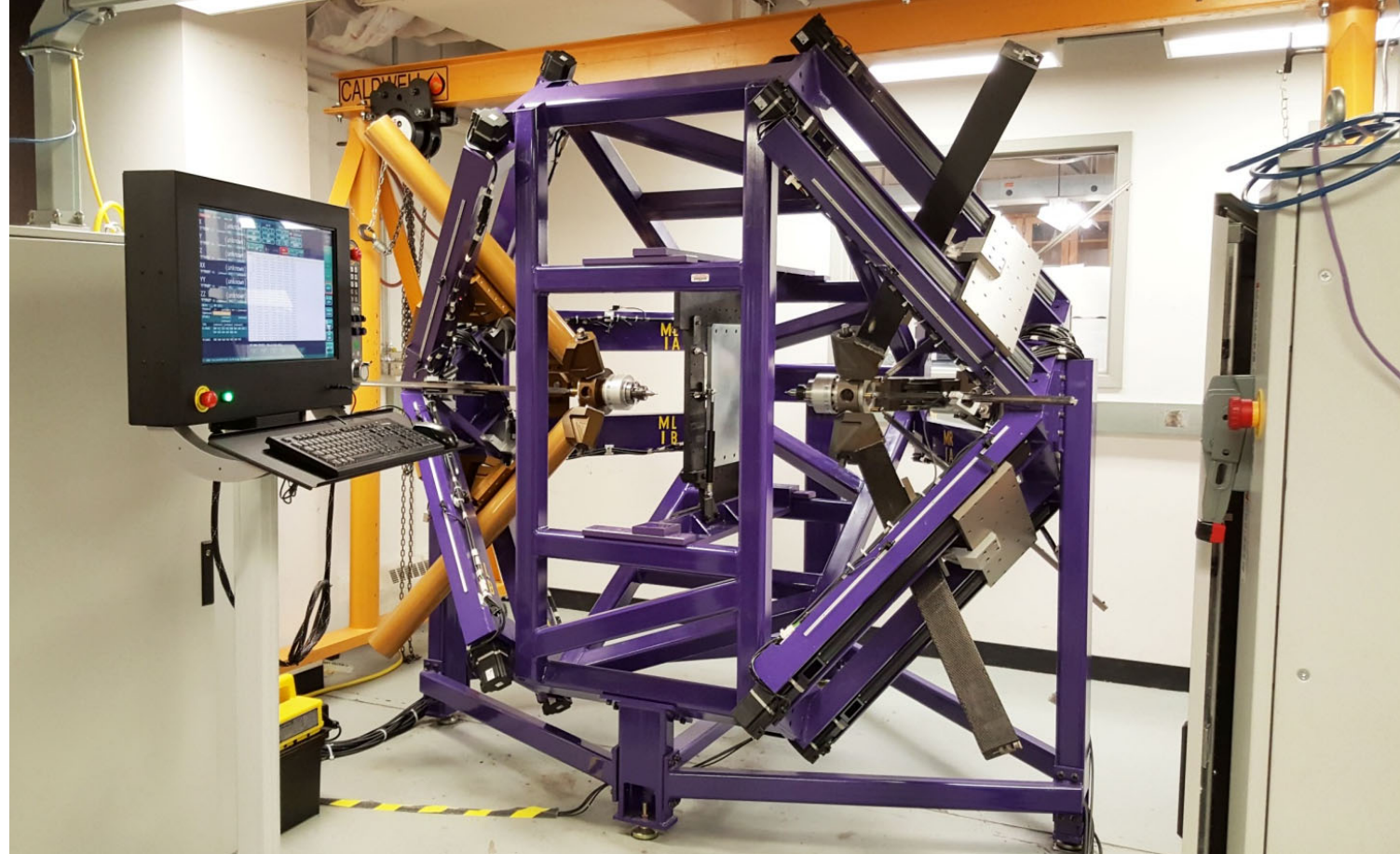
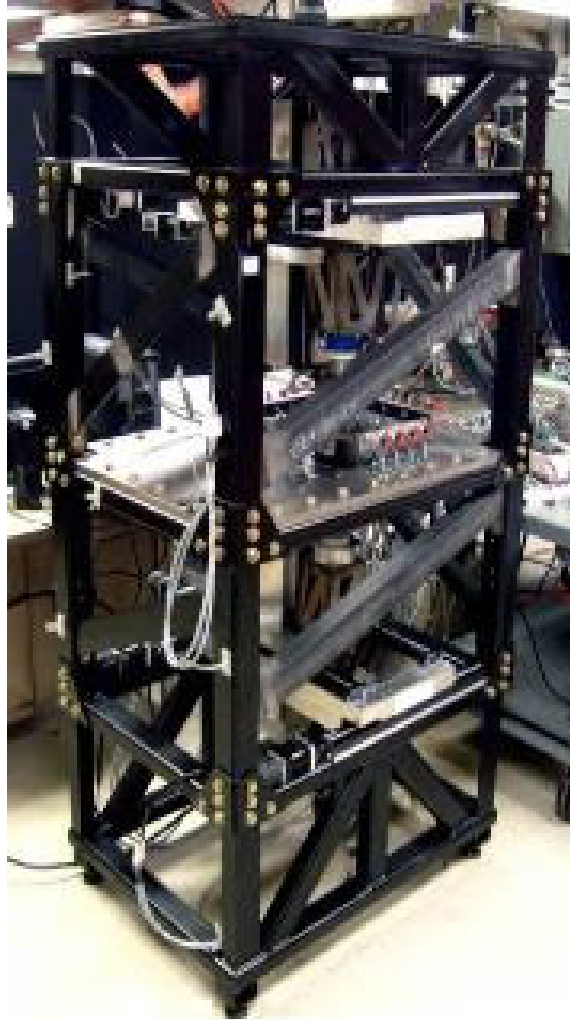
# DSIF



- Significant bending effects cause geometric deviations in concave features when using SPIF.



# DSIF Machines



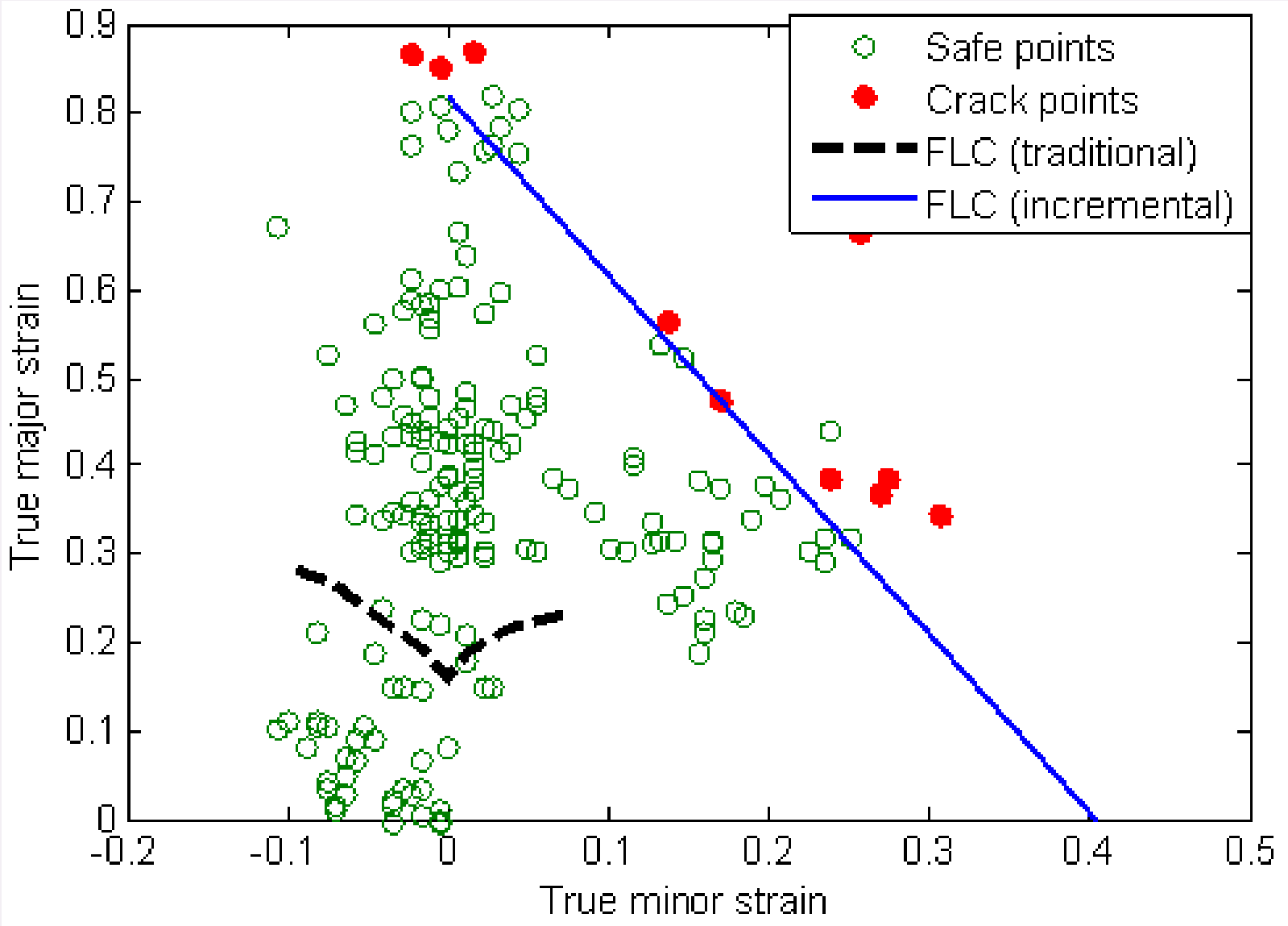
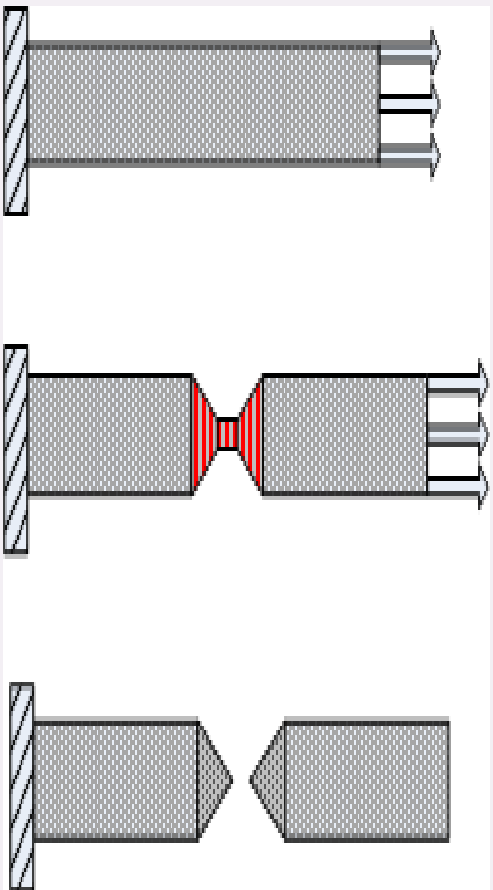


# Opportunities and Challenges of IF

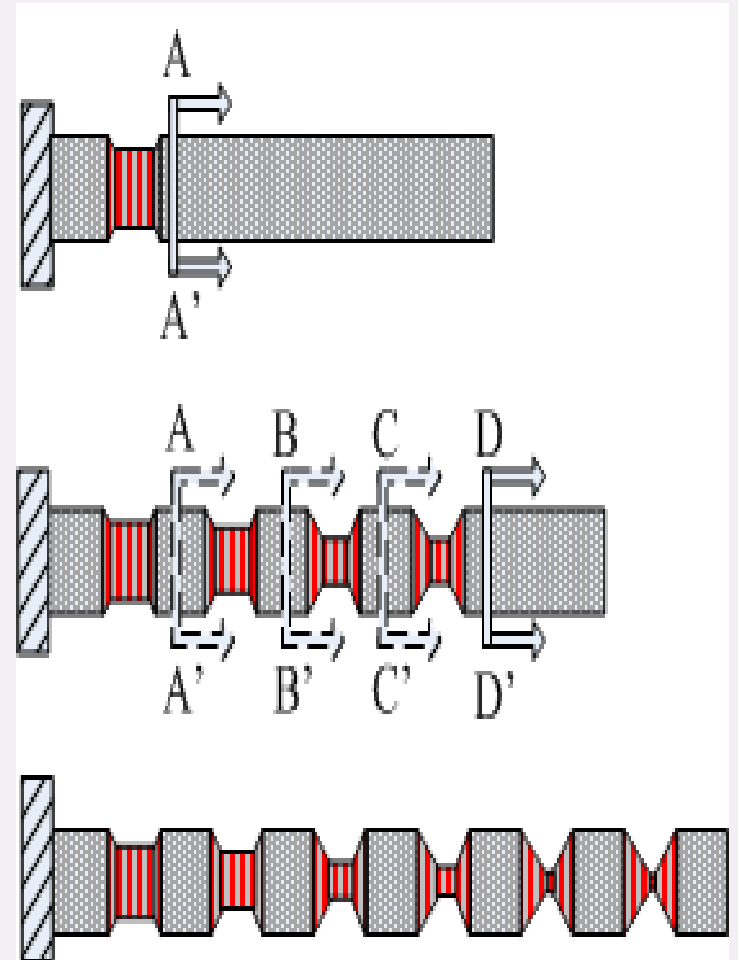
- Higher formability
- Geometric accuracy
- Forming sequence and forming time
- Turn-key operation
  - Toolpath code <https://youtu.be/fLSOVyIjr9o>

# Forming Limits in Incremental Forming

Traditional Forming



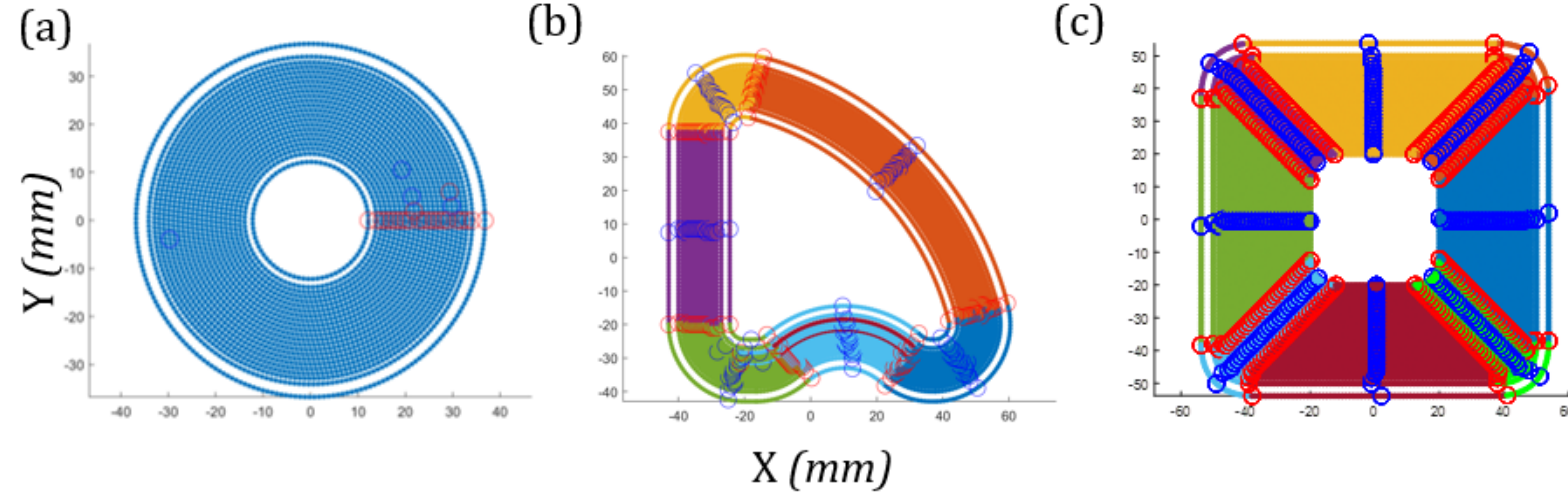
Incremental Forming



# Opportunities and Challenges of IF

- Higher formability
- **Geometric accuracy**
- Forming sequence and forming time
- Turn-key operation
  - Toolpath code <https://youtu.be/fLSOVyIjr9o>

# Geometric Accuracy



**Table 1** Comparison of geometric deviations for the test cases.

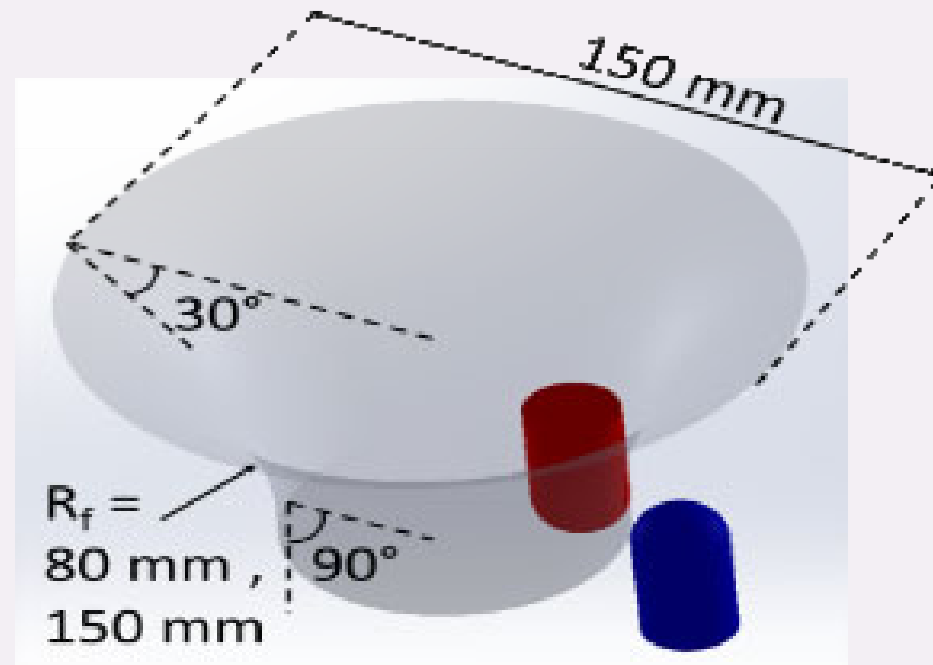
Geometry	Cone		Fish fin			Pyramid	
	Ref	SC	Ref	SC	SC+FC	Ref	SC+FC
Max. error (mm)	5.7	1.5	5.0	3.0	2.0	4.8	1.2
Avg. error (mm)	3.1	0.8	3.2	1.9	1.2	2.6	0.2

# Opportunities and Challenges of IF

- Higher formability
- Geometric accuracy
- **Forming sequence and forming time**
- Turn-key operation
  - Toolpath code <https://youtu.be/fLSOVyIjr9o>

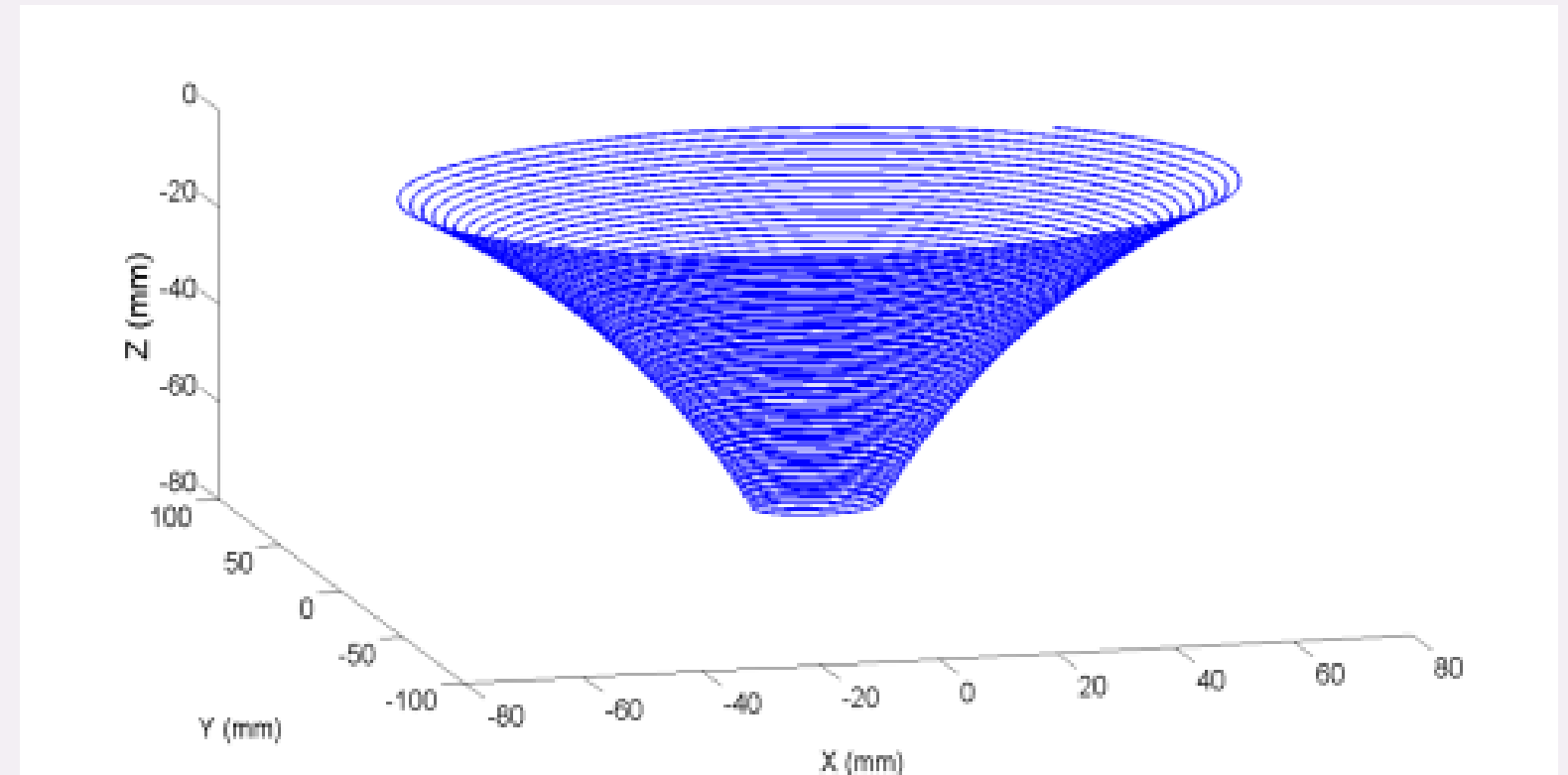
# Toolpath Generation

- CAD model for a funnel part



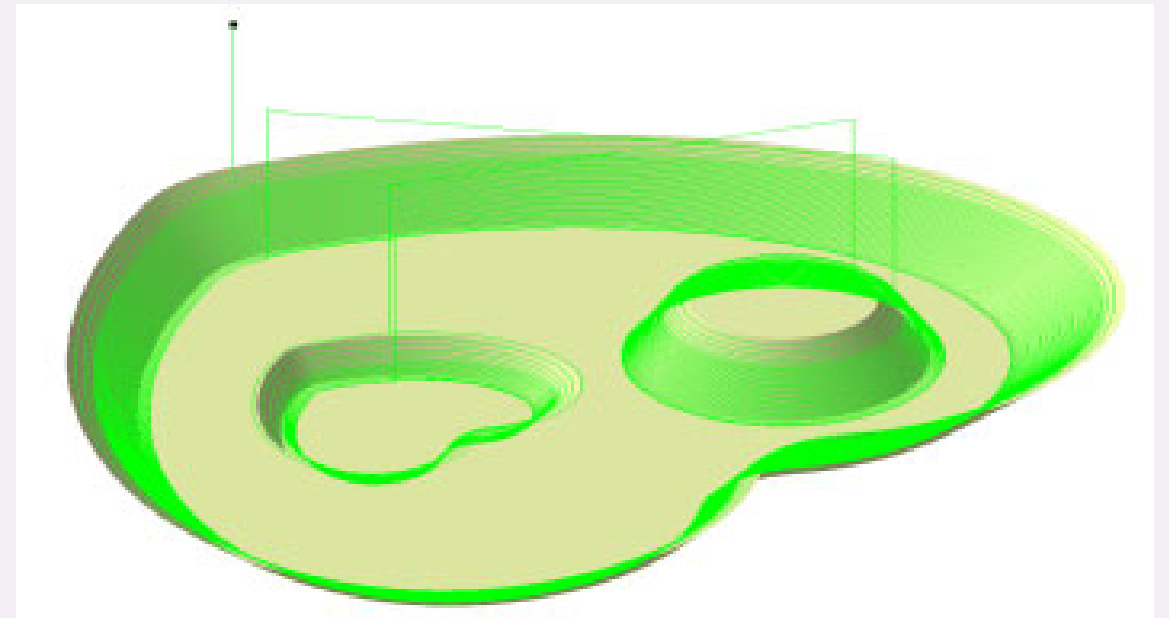
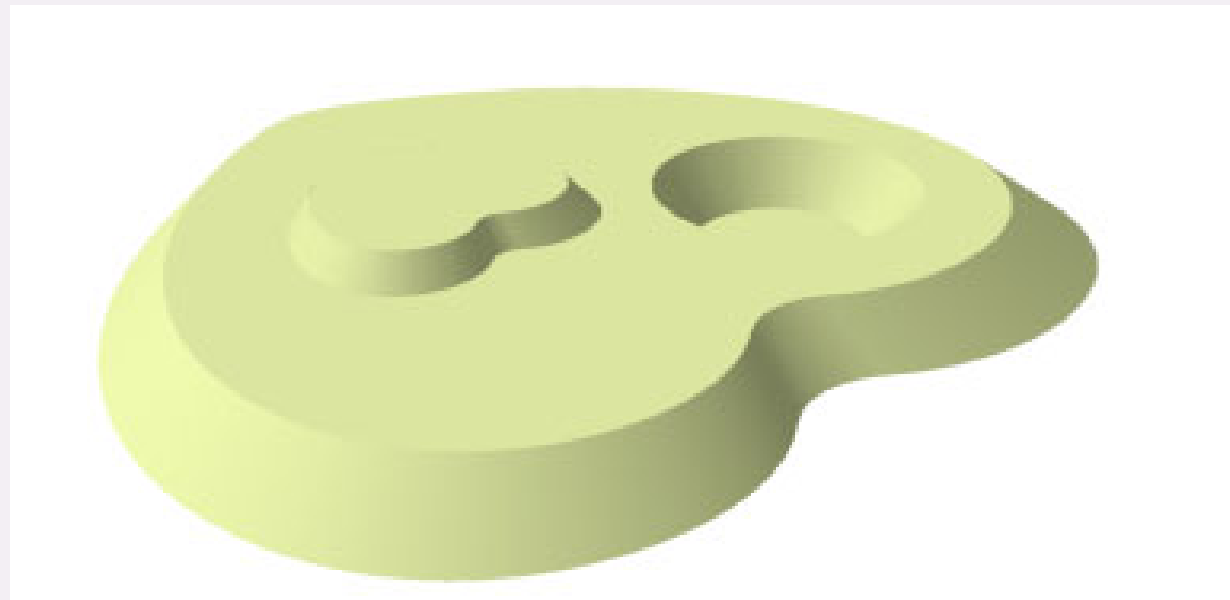
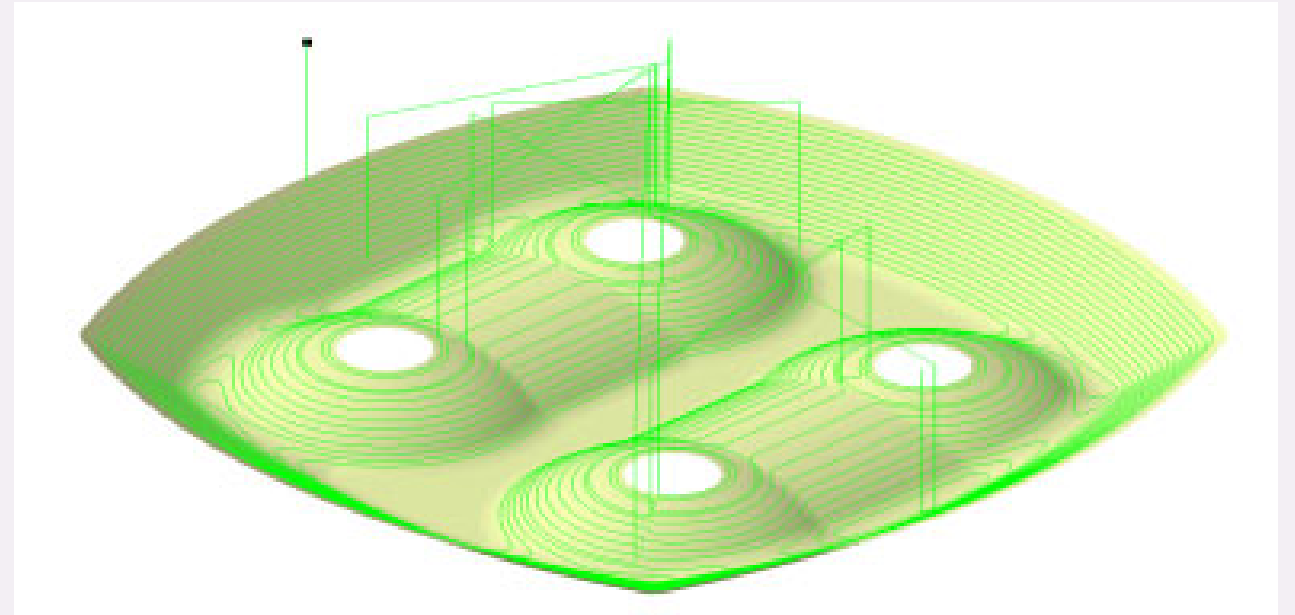
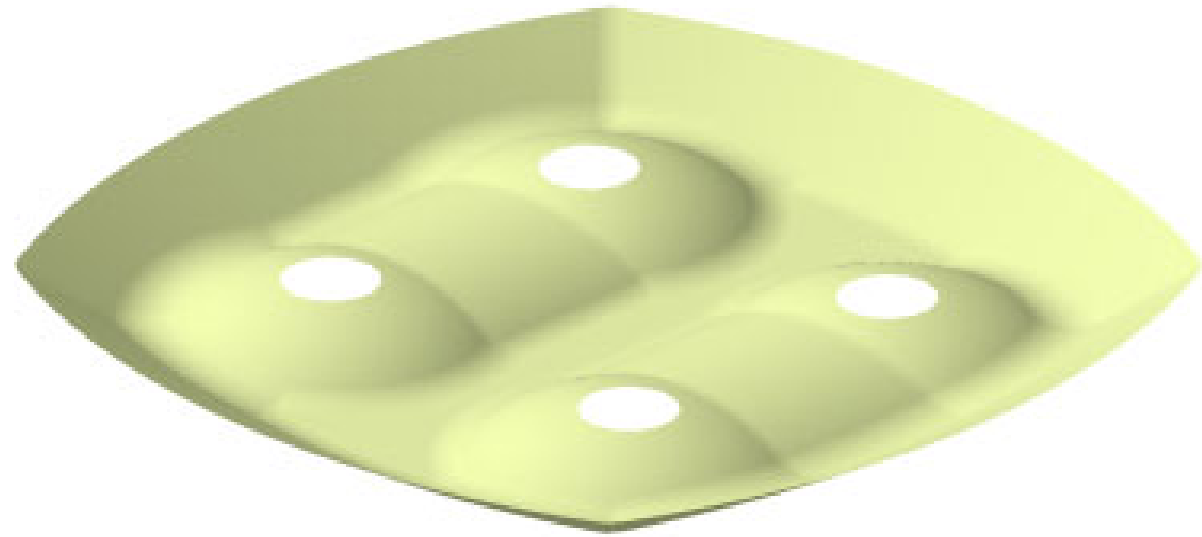
- Inputs:
  - CAD model
  - Tool radius
  - Incremental depth
  - Relative tool position

- Toolpath of the top tool



- Outputs:
  - Points (X,Y and Z) of the tool center

# Toolpath Generation

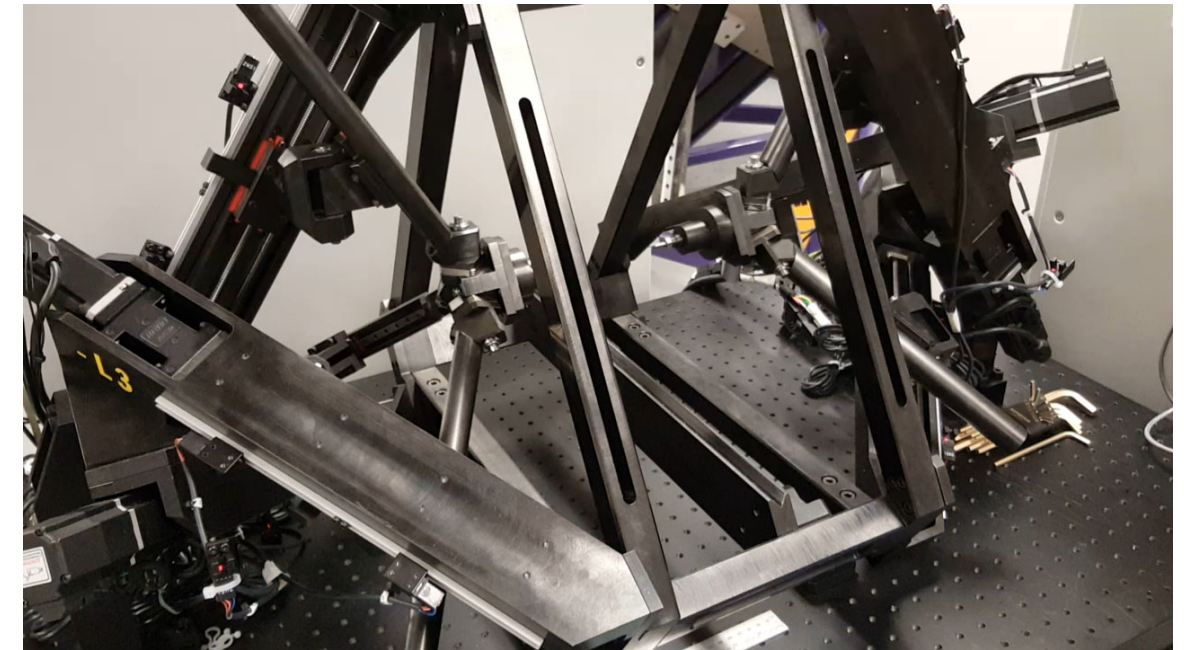


# Gen-2 DSIF – Tri-Pyramid Robots

## Macro Forming



## Micro Forming



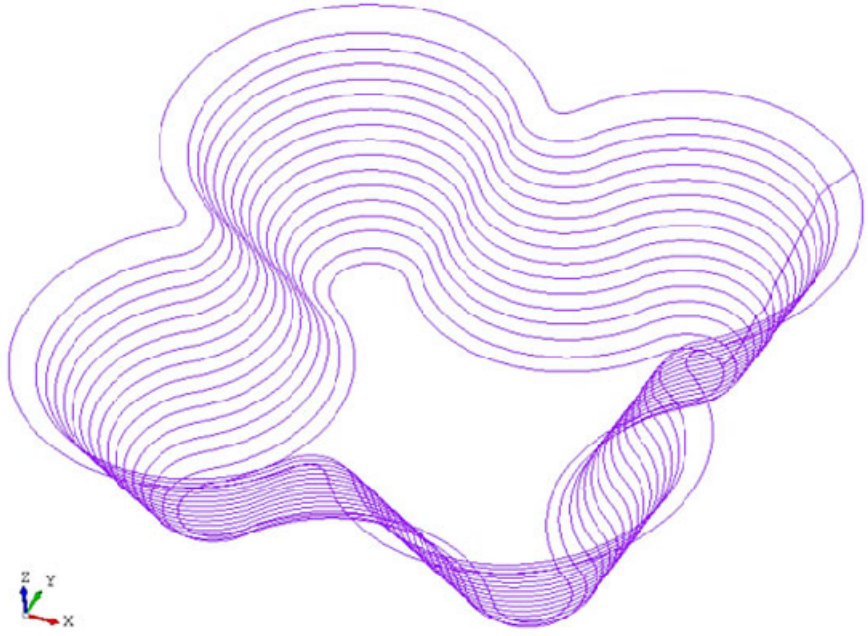


# Opportunities and Challenges of IF

- Higher formability
- Geometric accuracy
- Forming sequence and forming time
- **Turn-key operation**
  - Toolpath code <https://youtu.be/fLSOVyIjr9o>

# In-House C++ Toolpath Generation Software

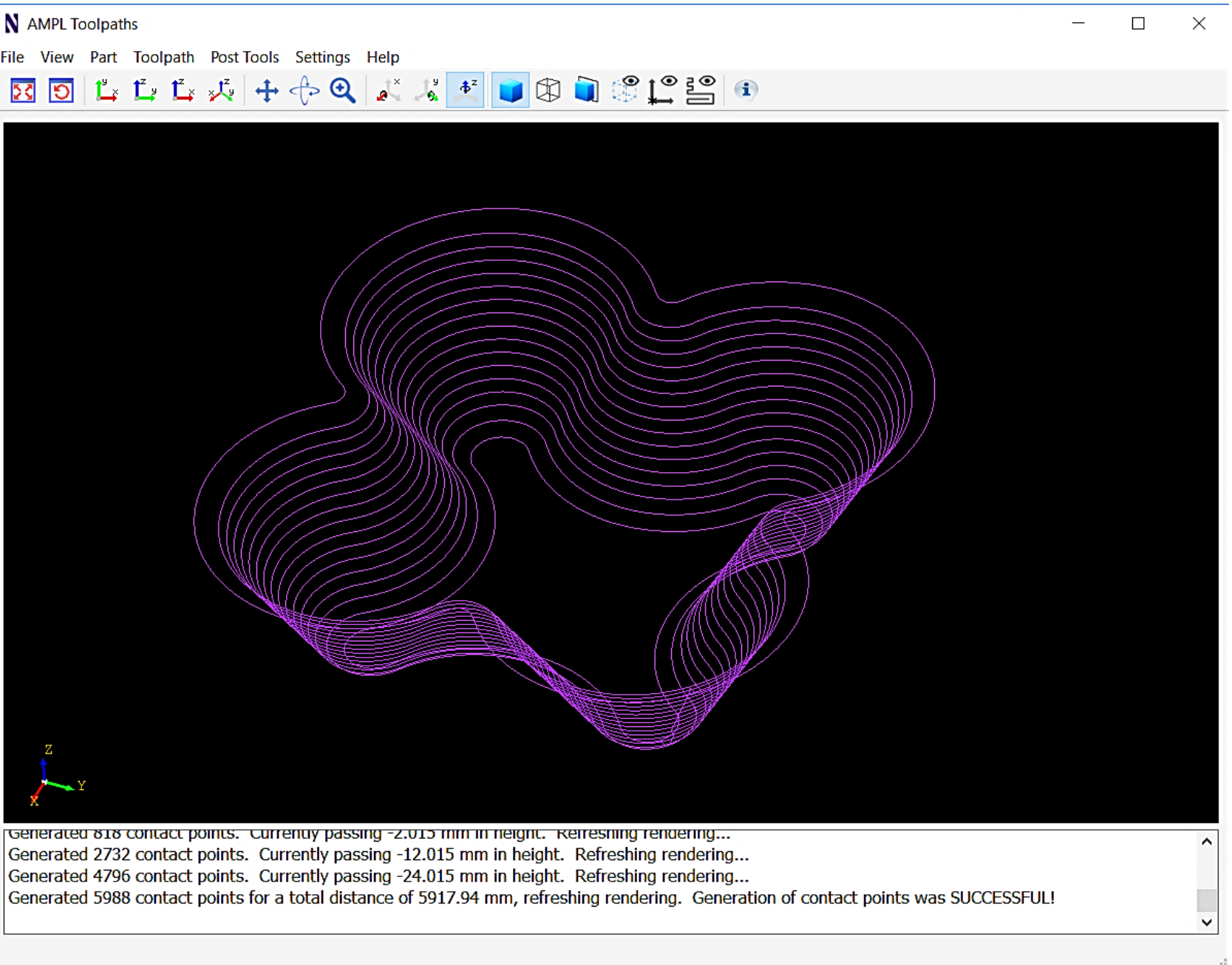
**AMPL Toolpaths – User Guide**



Software Creator:  
Newell Moser, PhD Candidate  
Advisers: Prof. Jian Cao and Prof. Kornel Ehmann  
Advanced Manufacturing Processes Laboratory (AMPL)  
Mechanical Engineering, Northwestern University

AMPL Toolpaths

File View Part Toolpath Post Tools Settings Help



Generated 818 contact points. Currently passing -2.015 mm in height. Refreshing rendering...

Generated 2732 contact points. Currently passing -12.015 mm in height. Refreshing rendering...

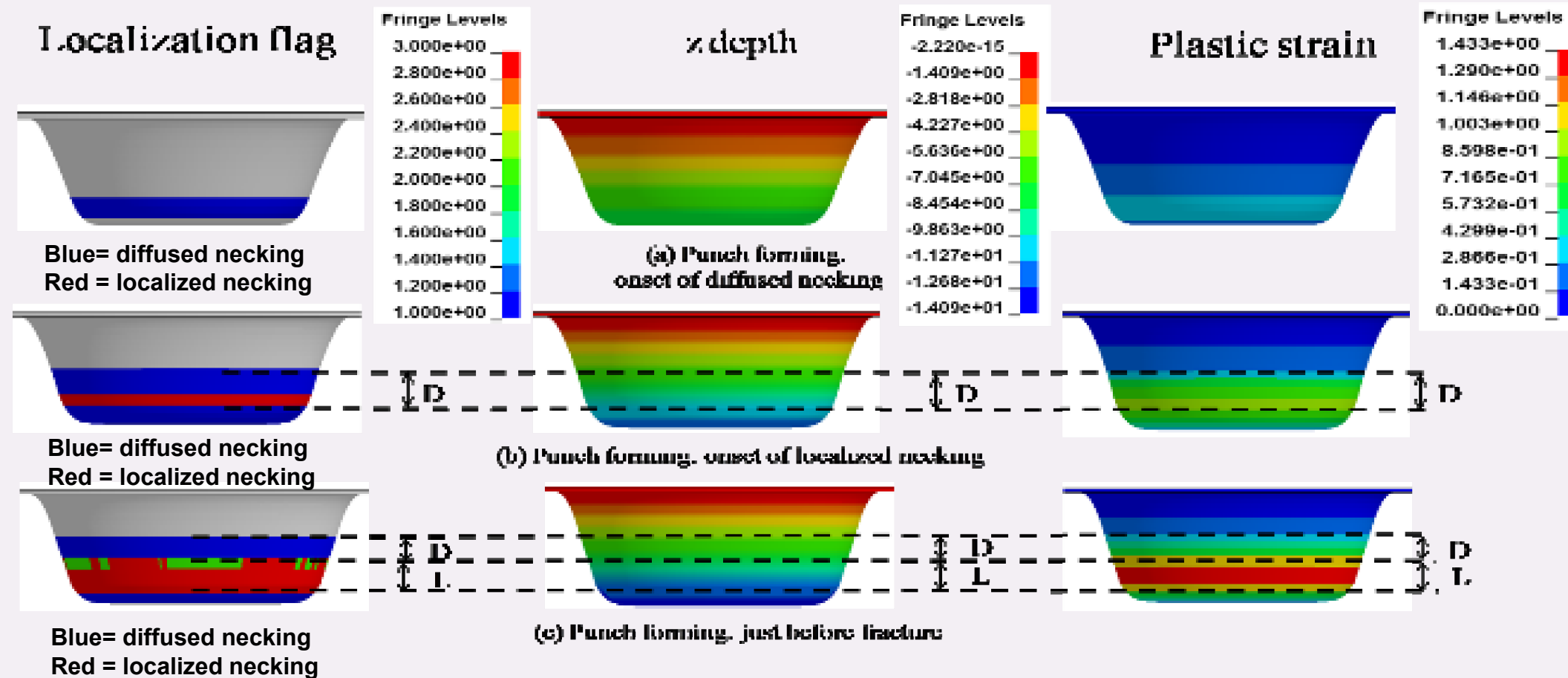
Generated 4796 contact points. Currently passing -24.015 mm in height. Refreshing rendering...

Generated 5988 contact points for a total distance of 5917.94 mm, refreshing rendering. Generation of contact points was SUCCESSFUL!

# Opportunities and Challenges of IF

- Higher formability
- Geometric accuracy
- Forming sequence and forming time
- Turn-key operation
  - Toolpath code <https://youtu.be/fLSOVyIjr9o>

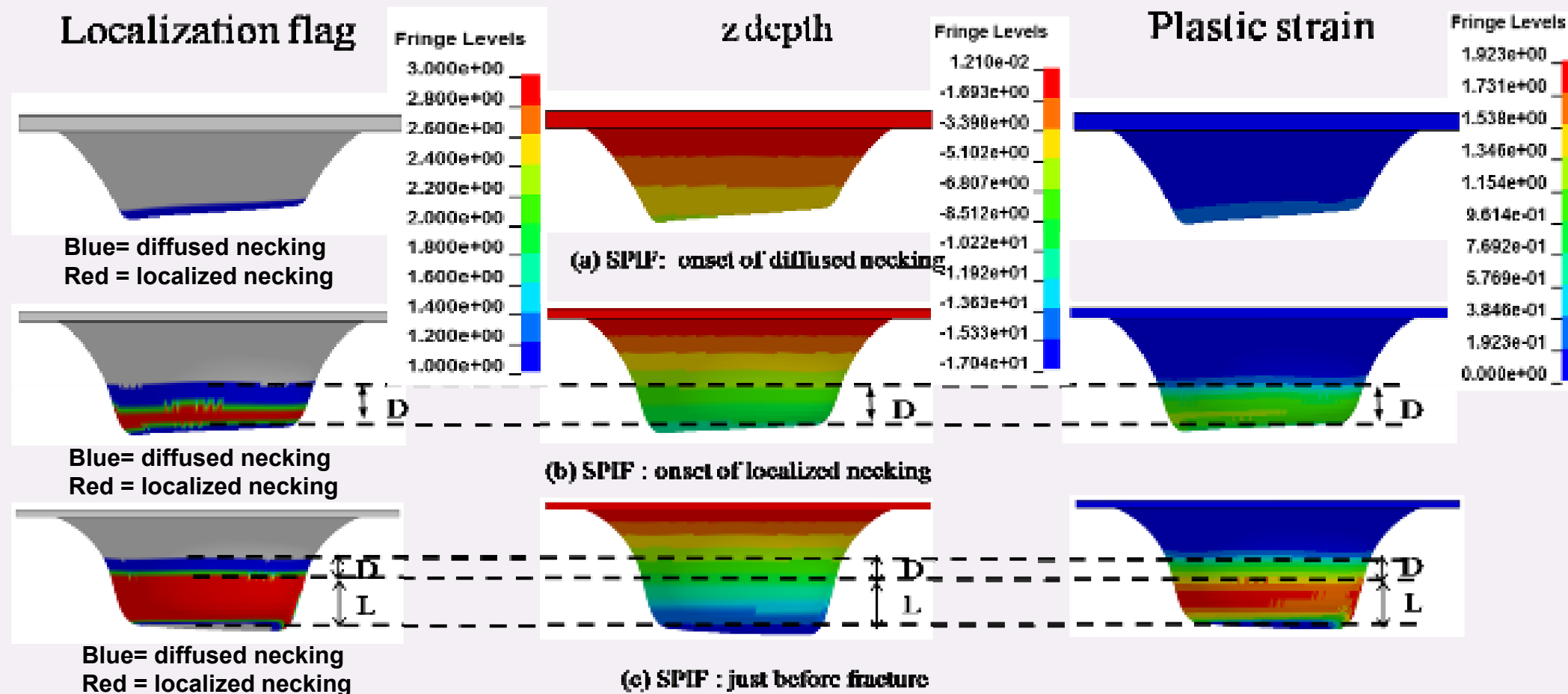
# Material Instability: Punch forming



Beginning of (a) Diffused necking at 8.6 mm (b) Localized necking at 12.6 mm (c) Fracture at 14.09 mm

- Deformation is global in nature, so after initial localized necking occurs this unstable material is still actively stretched by the punch
- Therefore the plastic strain gets concentrated in the shear bands which grow rapidly leading to rapid fracture

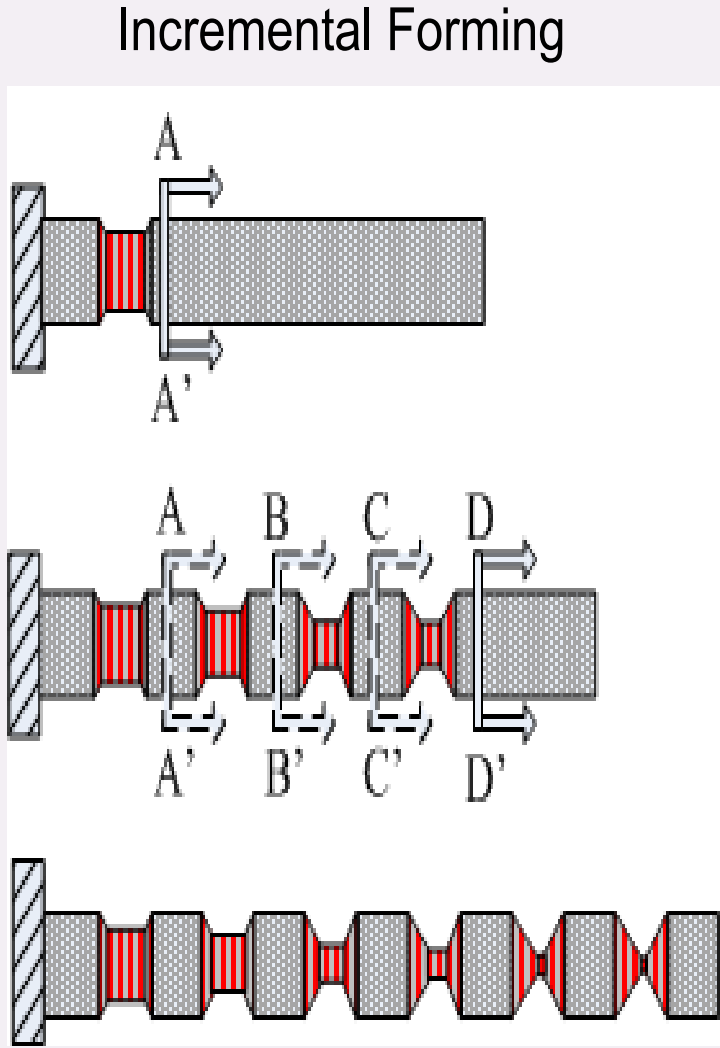
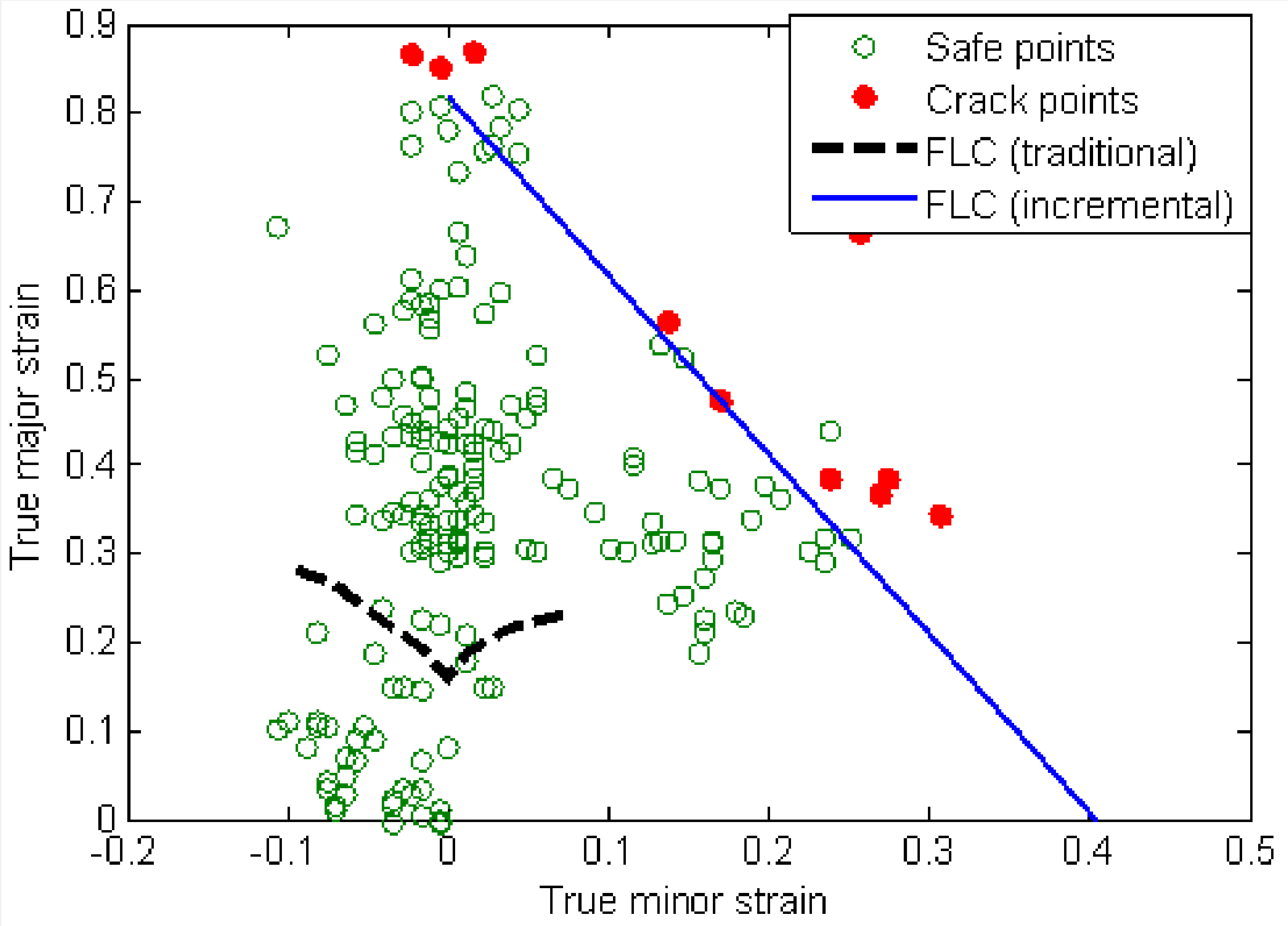
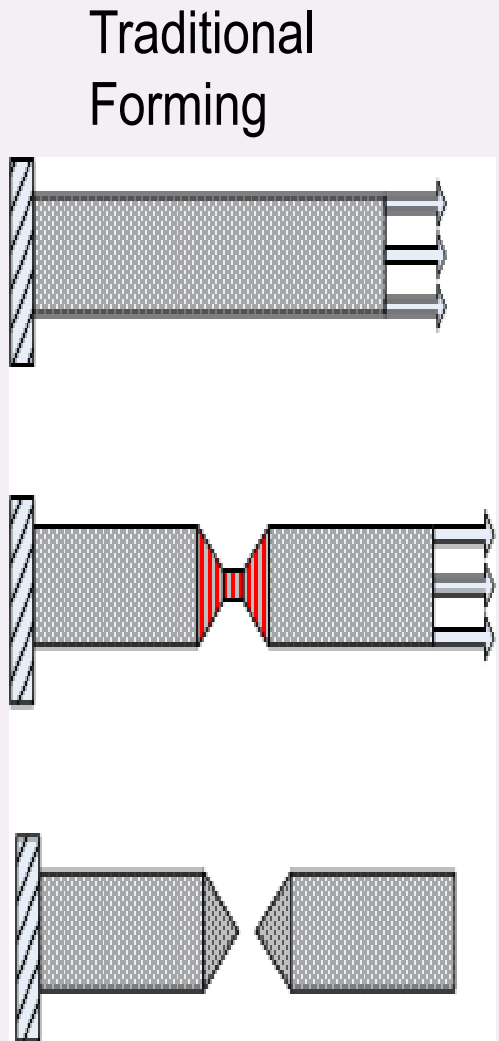
# Material Instability: SPIF



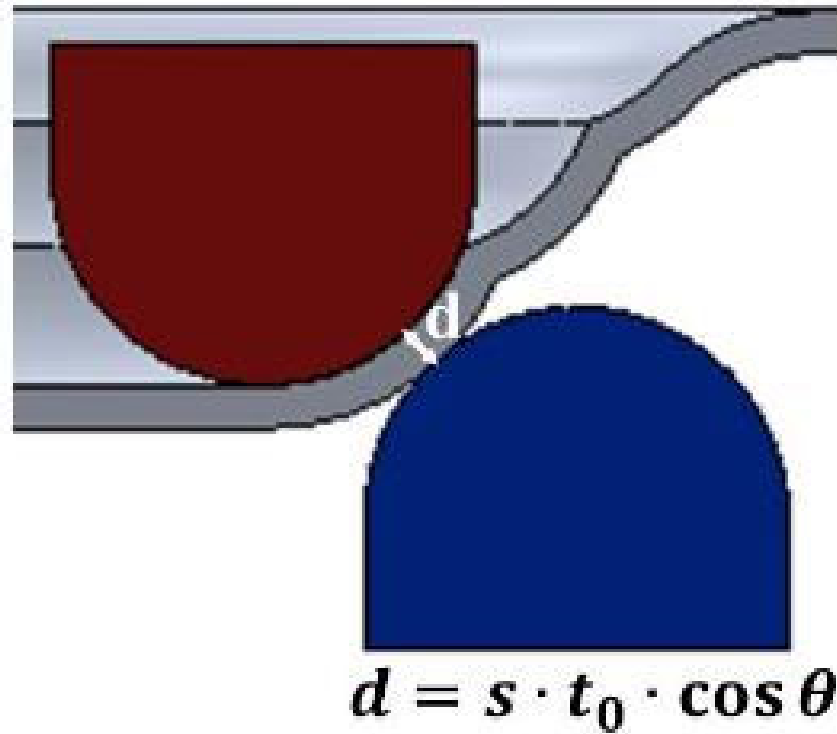
Beginning of (a) Diffused necking at 5.6 mm (b) Localized necking at 10.4 mm (c) Fracture at 16.9 mm

- Deformation is local, so shear bands in previously formed unstable region don't grow as quickly. This previous unstable region takes up some of the plastic strain of the newly formed material in subsequent tool passes
- This allows the newly formed material to take greater amount of plastic strain and reach a greater Z depth without fracture

# Forming Limits in Incremental Forming



# Squeeze Factor in DSIF



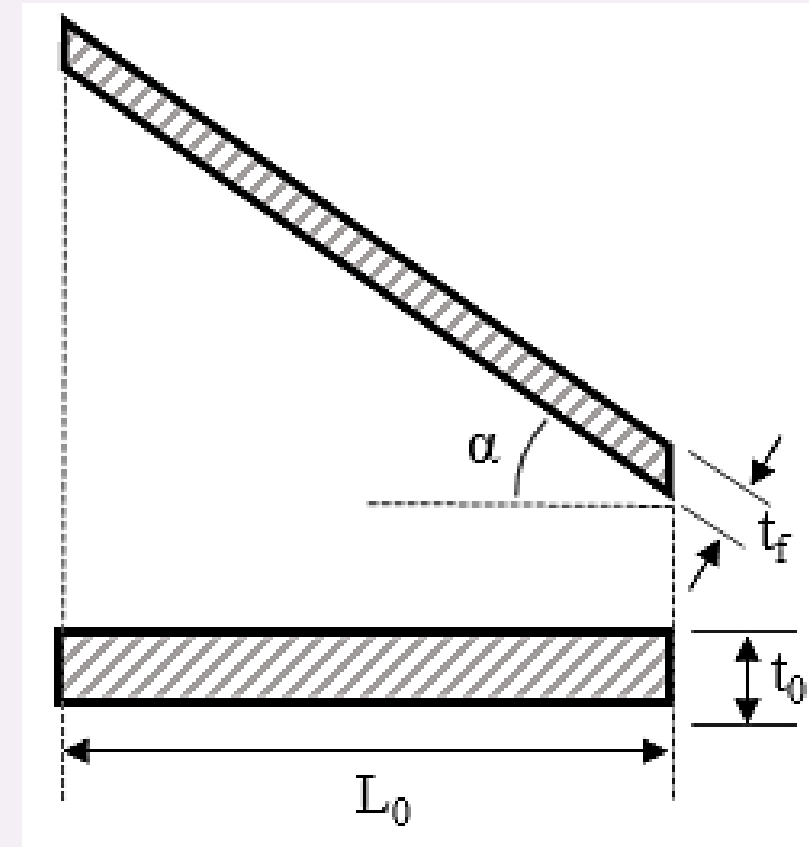
where,

$s$  (squeeze factor)  $\leq 1.0$

$t_0$ : original sheet thickness

$\theta$ : wall angle at local contact point of forming tool

$[t_0 \cdot \cos \theta]$ : Sine Law thickness



Sine Law (proposed originally for Shear Spinning)

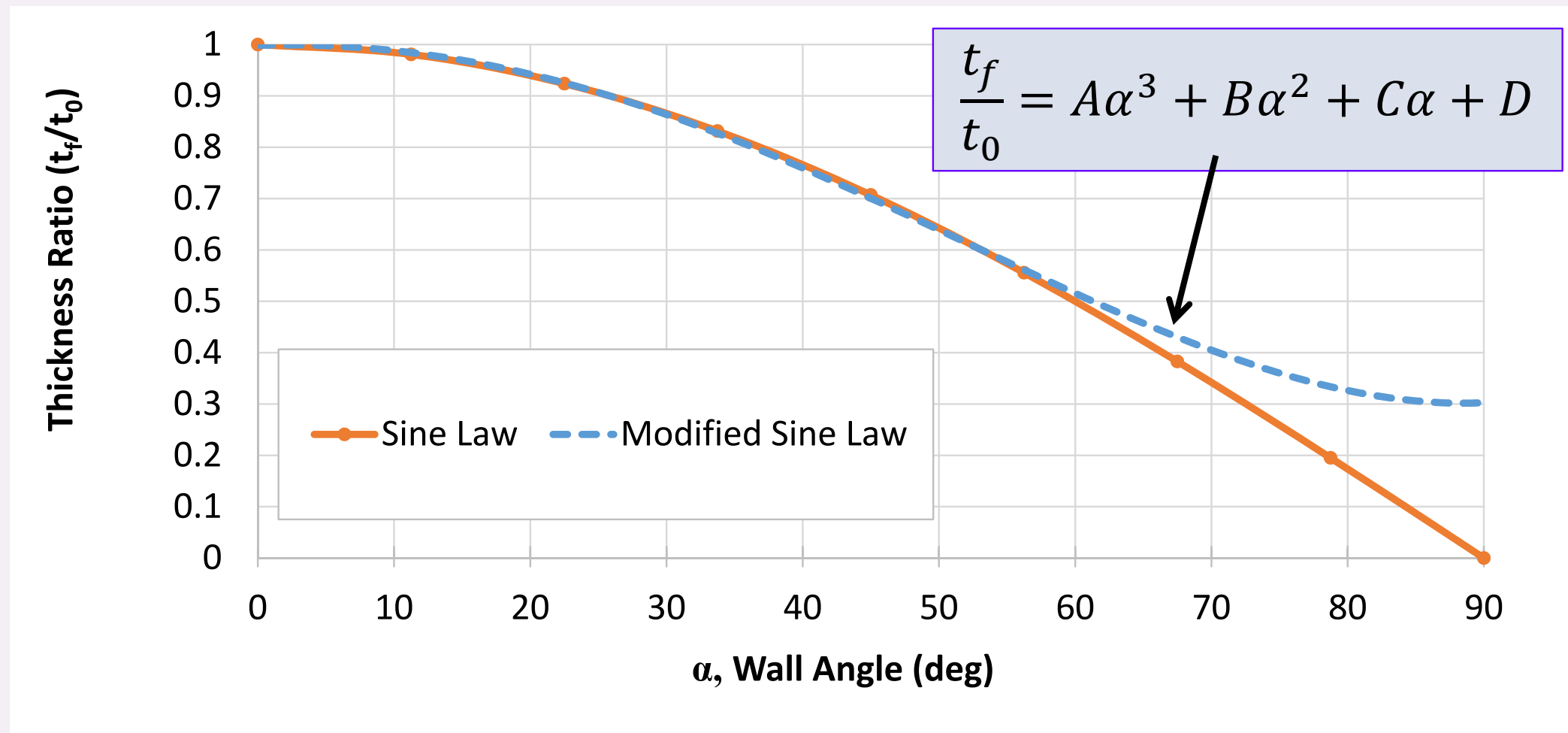
$$t_f = t_0 \sin(90^\circ - \alpha) = t_0 \cos \alpha$$

where:  $\alpha$  - Wall Angle

# Modified Thickness Prediction

Thinning Failure Criterion:  $\varepsilon_3 \leq \varepsilon_f$

where  $\varepsilon_f$  is the thickness strain at the onset of fracture in plane strain conditions





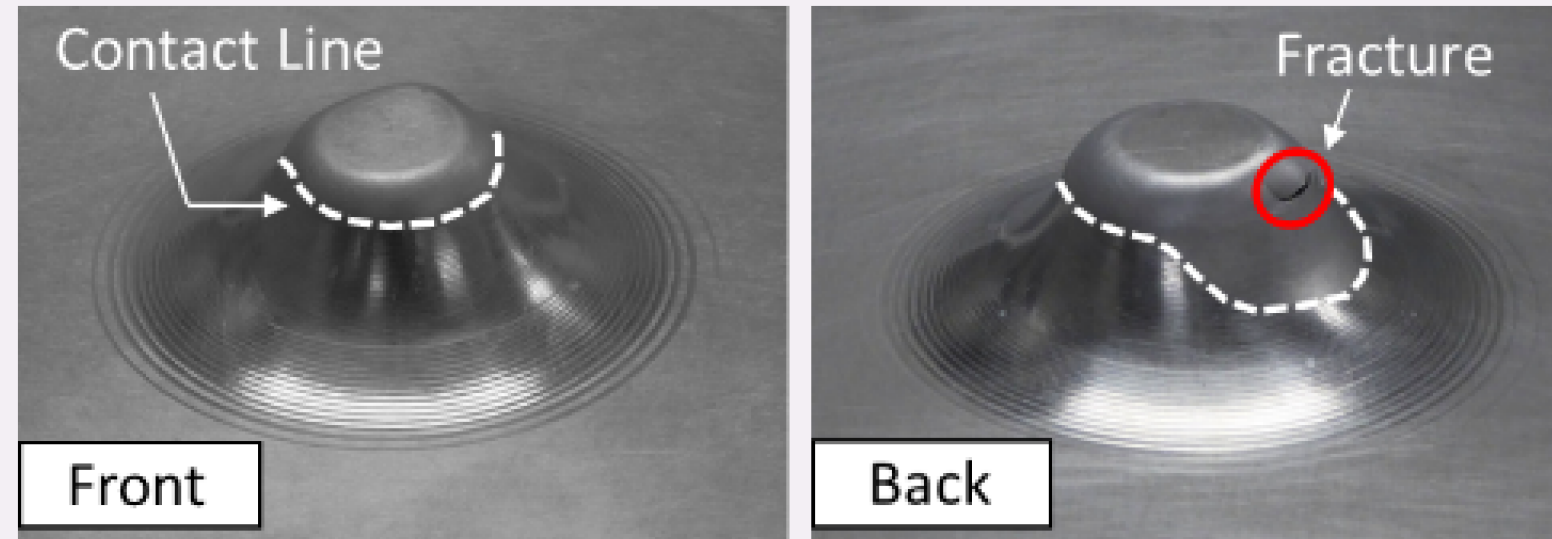
# Fracture in DSIF



Shamrock Part (63° Wall Angle)

# Objective: To Delay Fracture

Hypothesis: Lost contact leads to earlier fracture

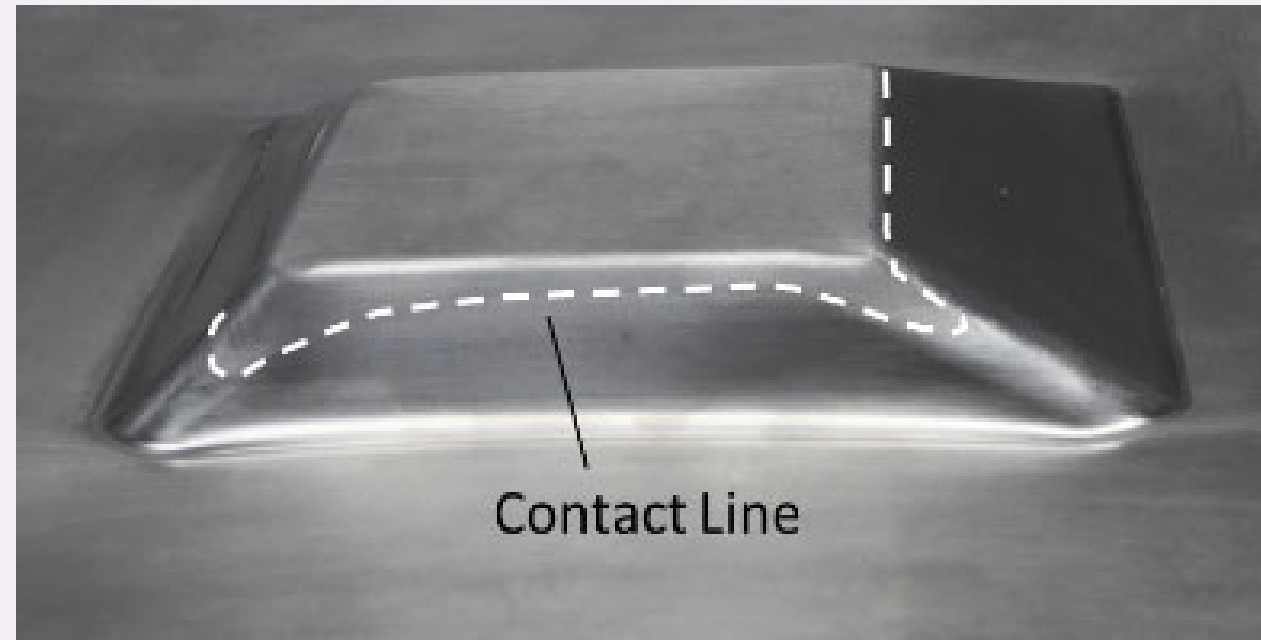


If the supporting tool loses contact with the part:

1. DSIF degenerates to Single-Point Incremental Forming;
2. The stabilizing compressive stress through-the-thickness is lost;
3. Local thinning tends to occur resulting in premature fracture.

# Potential Source Causing the Loss of Contact – Inaccurate Thickness Prediction

Truncated pyramid with **four** different wall angles – Used the Sine Law

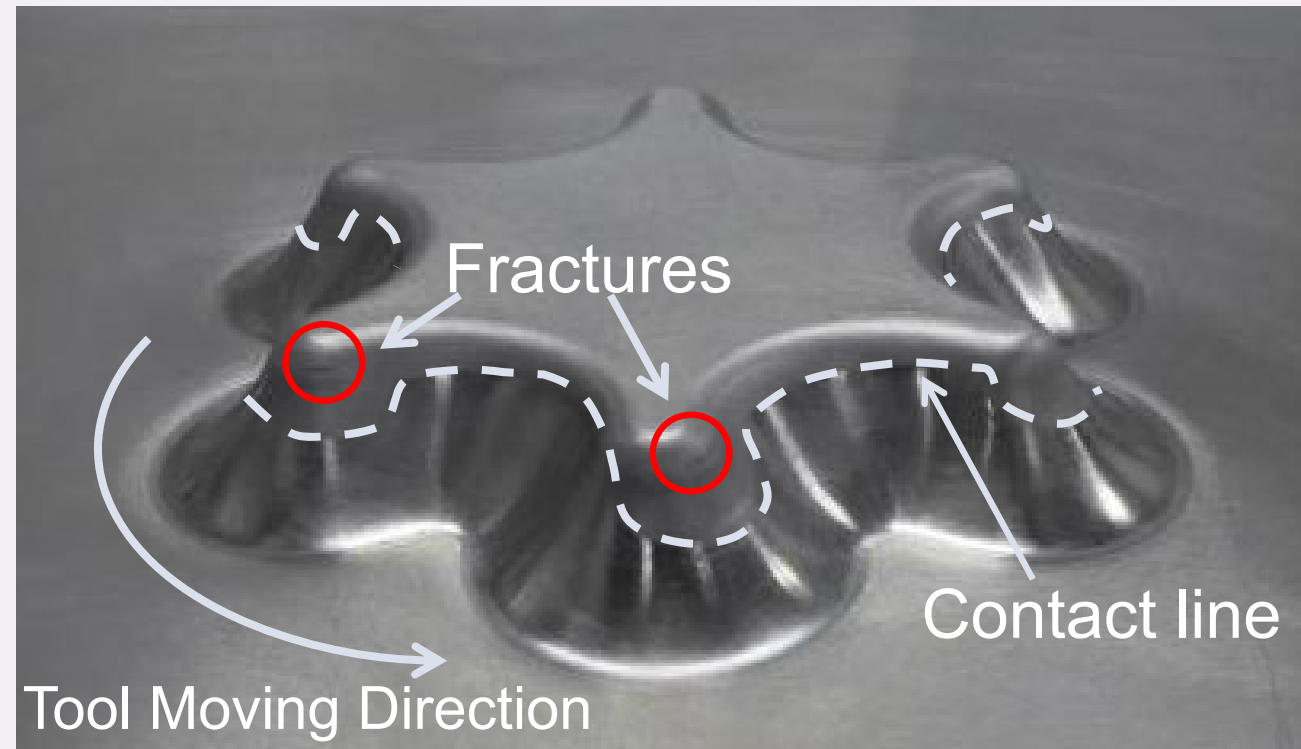


Despite the constant wall angle, the tool gap defined by the Sine Law was not adequate, particularly in transition zones near the corners.

➤ Should consider the in-plane curvature.

# and more...

Funnel-Star – Used the Sine Law

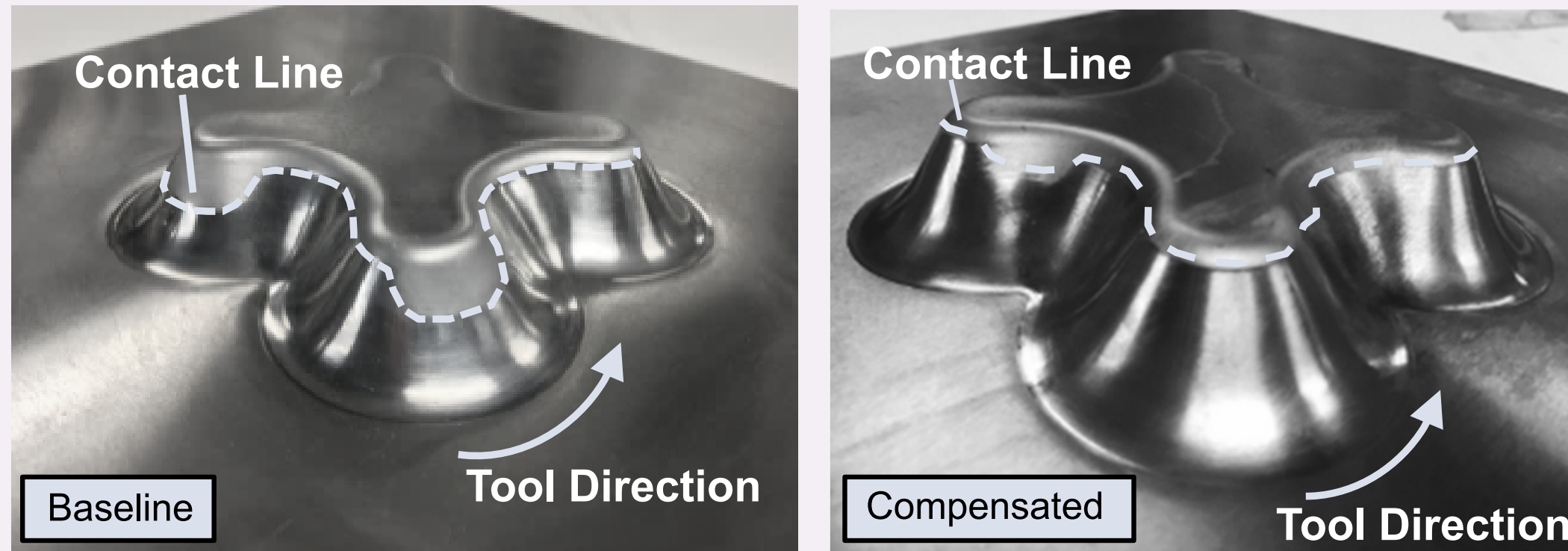


Note the **asymmetry** of contact line; in favor of the tool direction. This asymmetry was present for **ALL** corners of the part.

➤ Should consider the tool moving direction.

# Experiment Using the Proposed Correction Function

## Shamrock with 60° Wall Angle

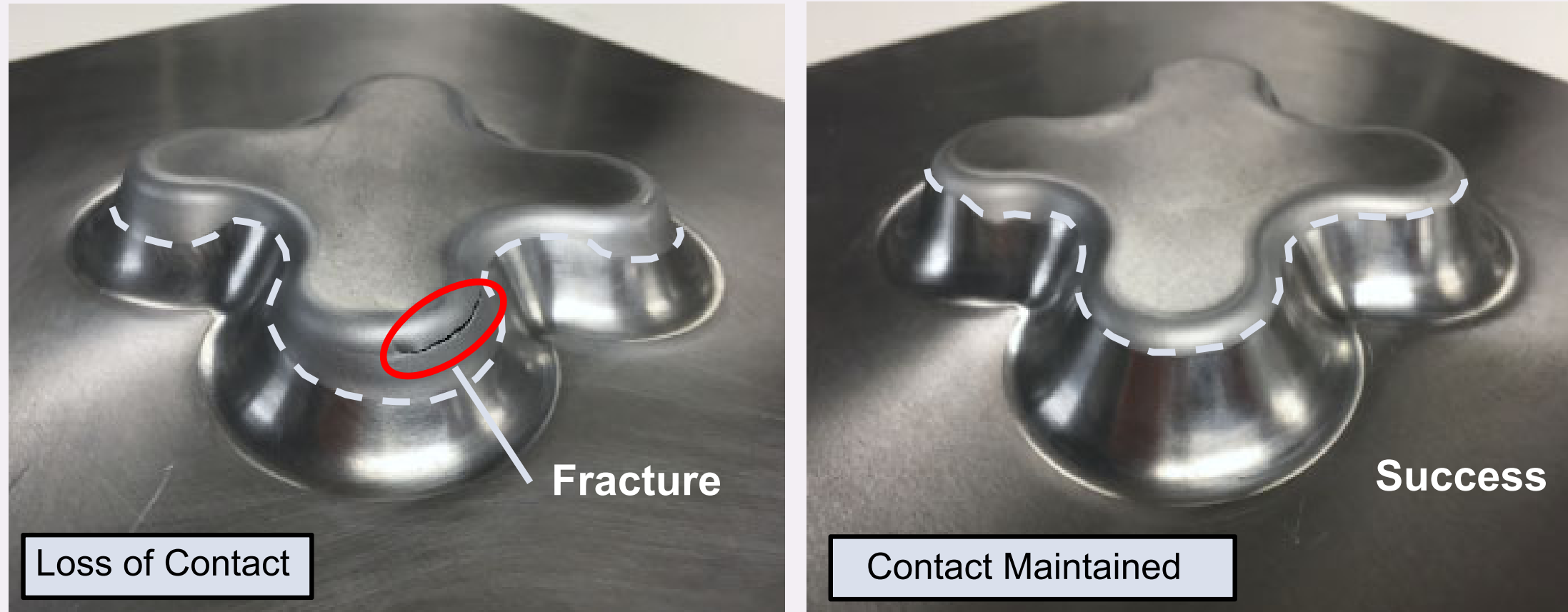


**Baseline** – Tool gap based on the Sine Law

**Compensated** – Tool gap based on the proposed correction function

Contact was maintained far better when using the proposed tool gap model.

# Verification – Shamrock Part with 65° Wall Angle

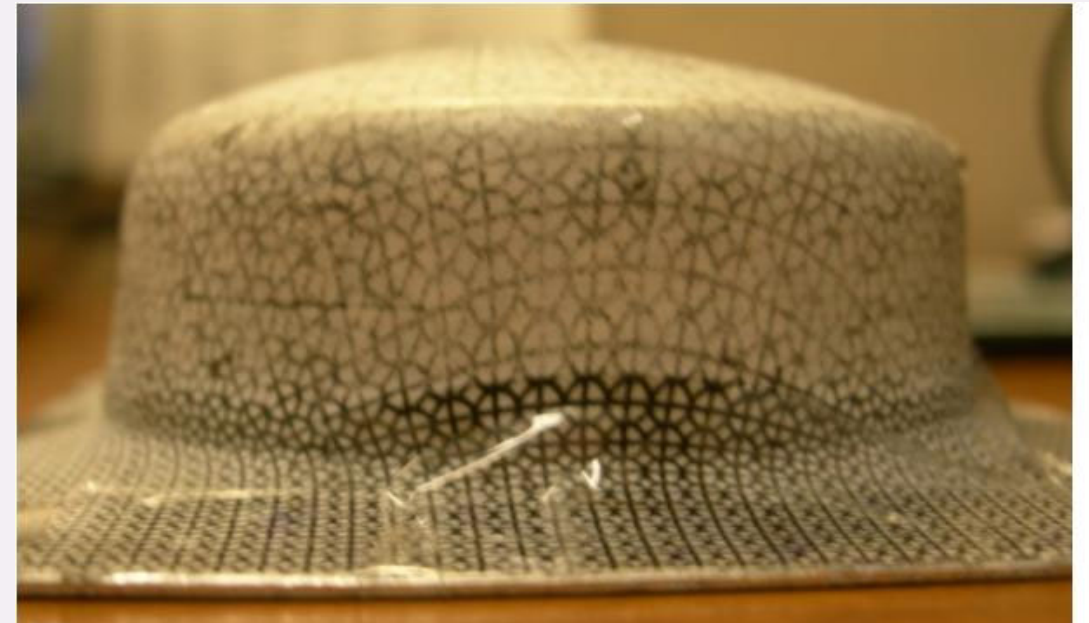
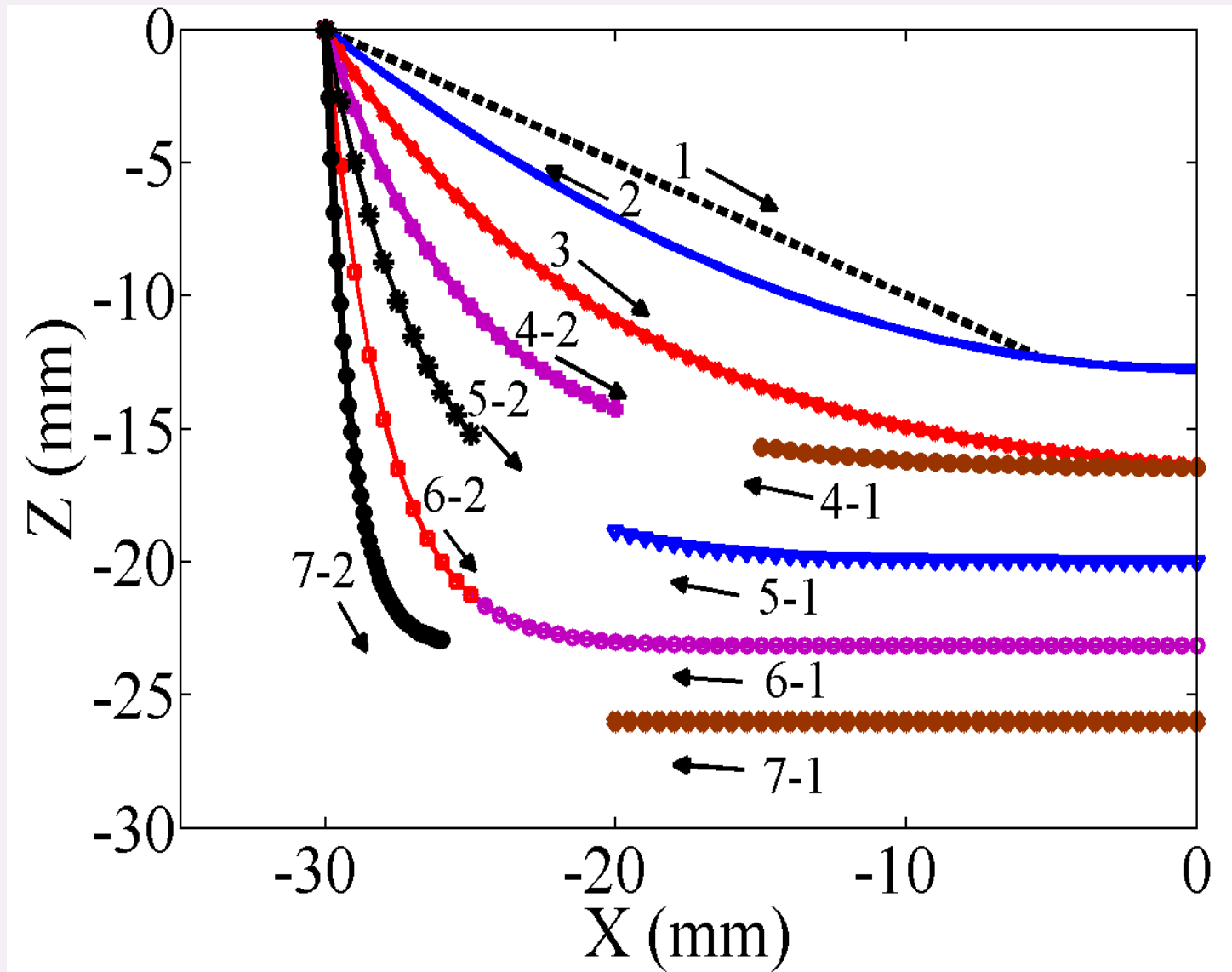


**Baseline** – Tool gap based on the Sine Law

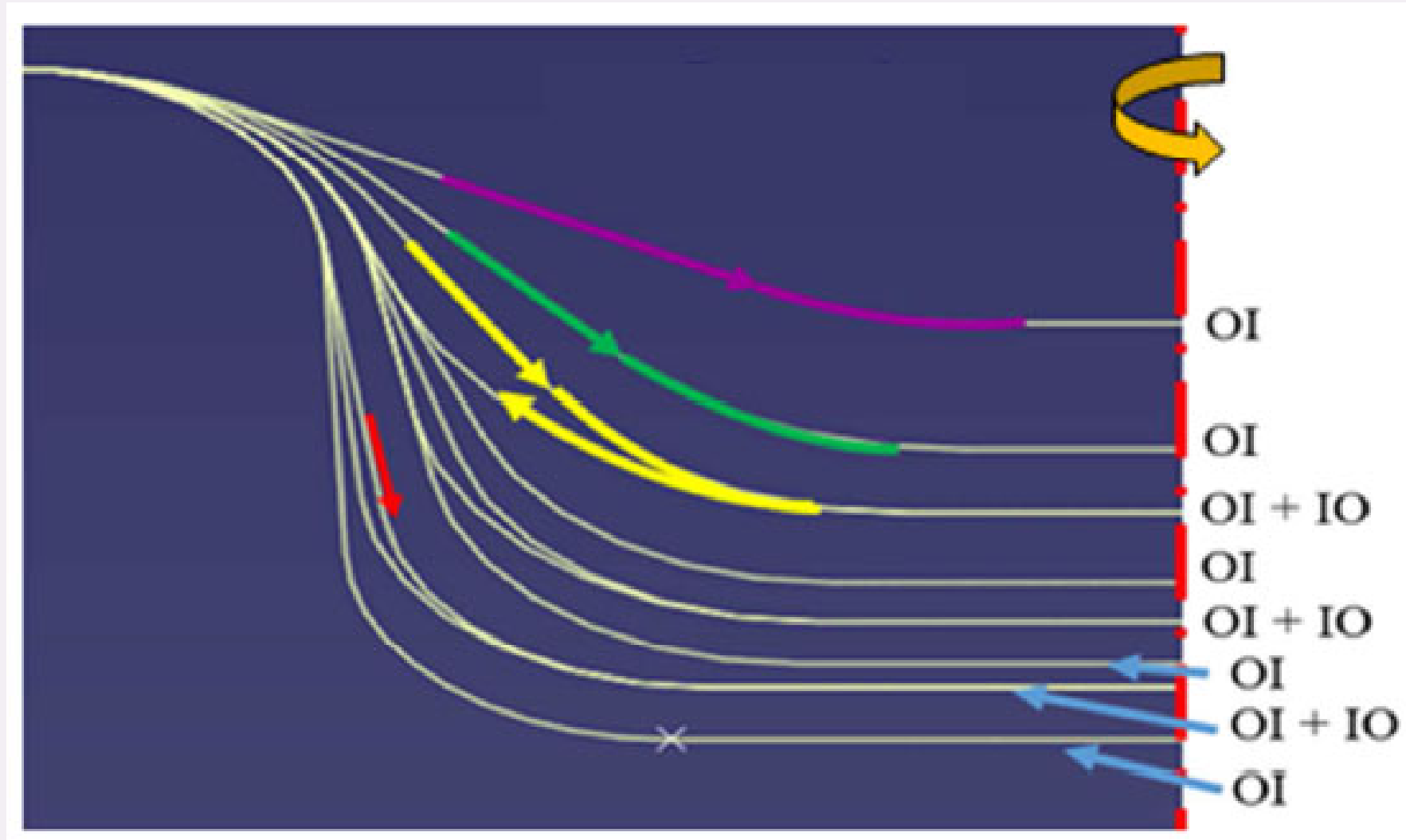
**Compensated** – Tool gap based on proposed correction function

Upon increasing the wall angle, maintaining contact helped to prevent thinning and increased formability.

# Multi-pass SPIF

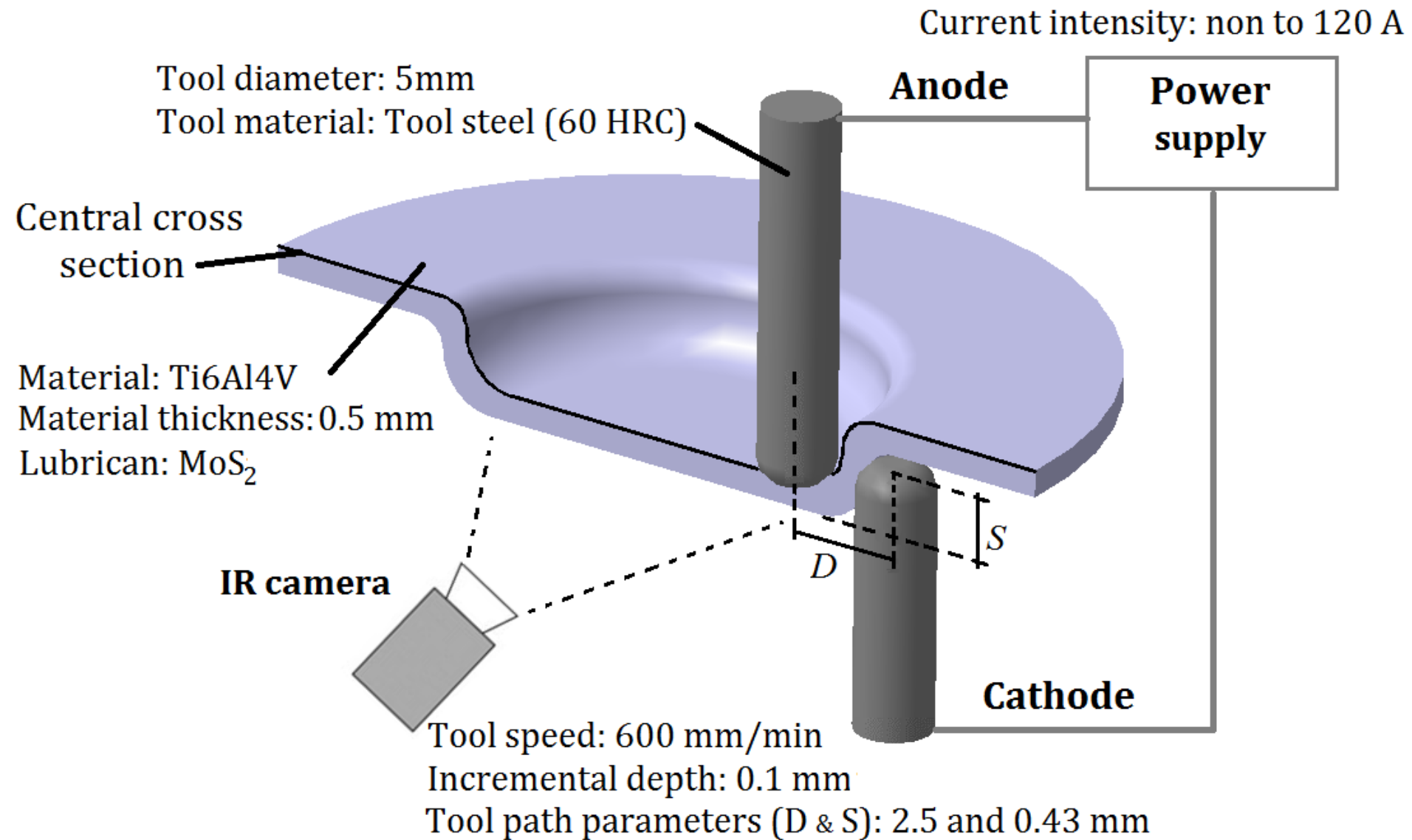


# Multi-pass DSIF

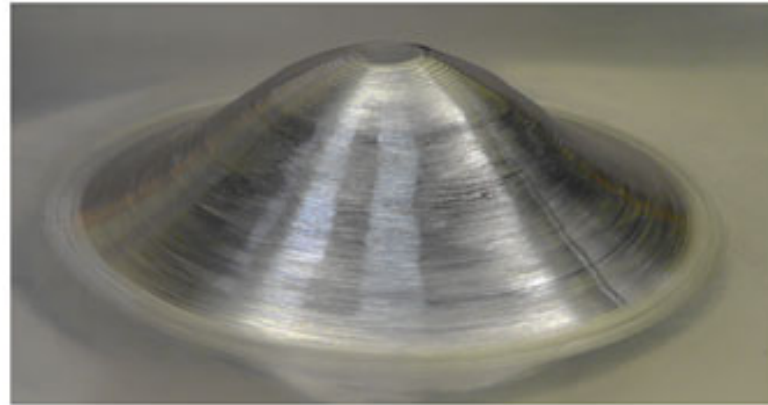




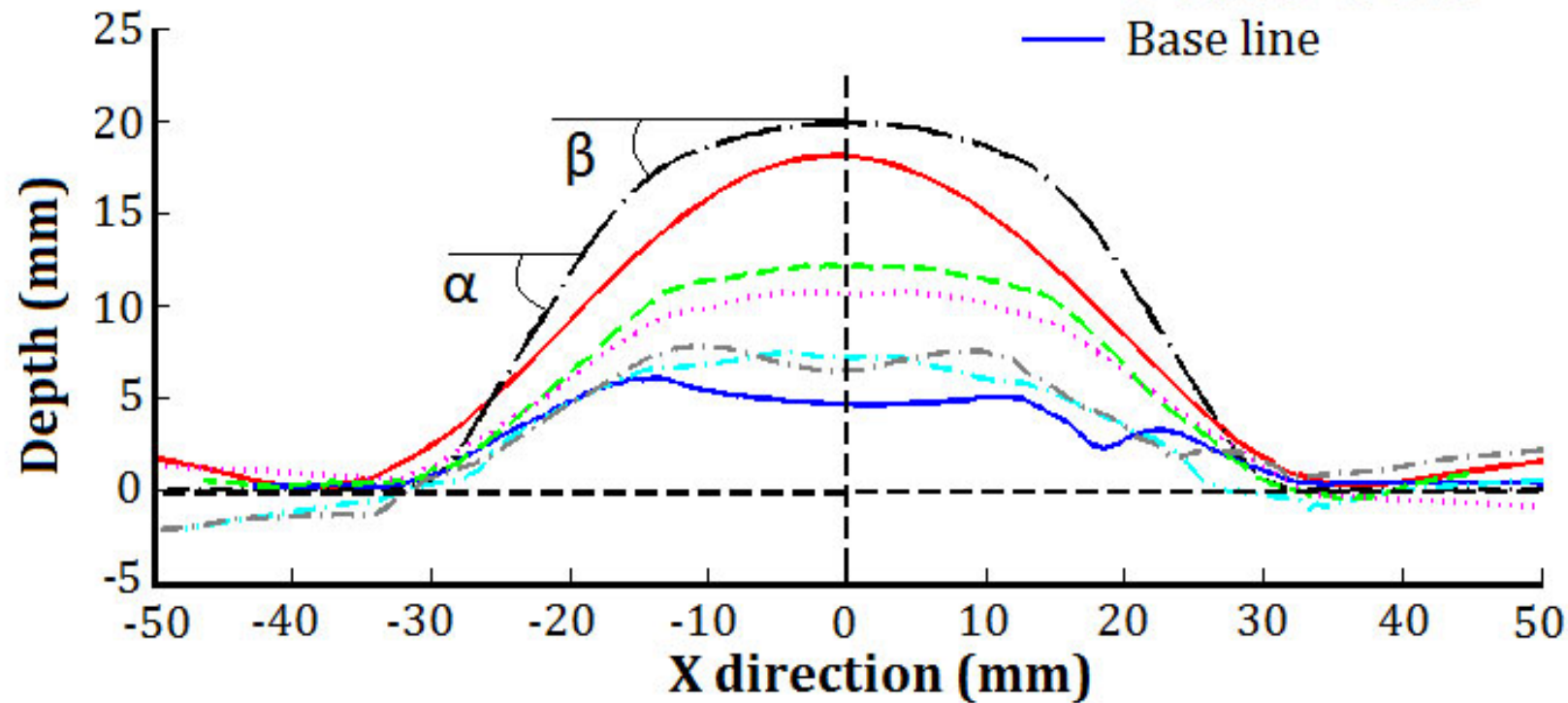
# Electrically-Assisted ADSIF (E-ADSIF)



# Varying the Amperage and Resultant Formability



- - Desired geometry
- E - MDSIF 50A
- - E - ADSIF 50 A
- ⋯ E - ADSIF 100 A
- · - E - ADSIF 40 A
- · - E - ADSIF 120 A
- Base line



Forming **Ti6Al4V** in room temperature fractured at the depth of 4.58 mm

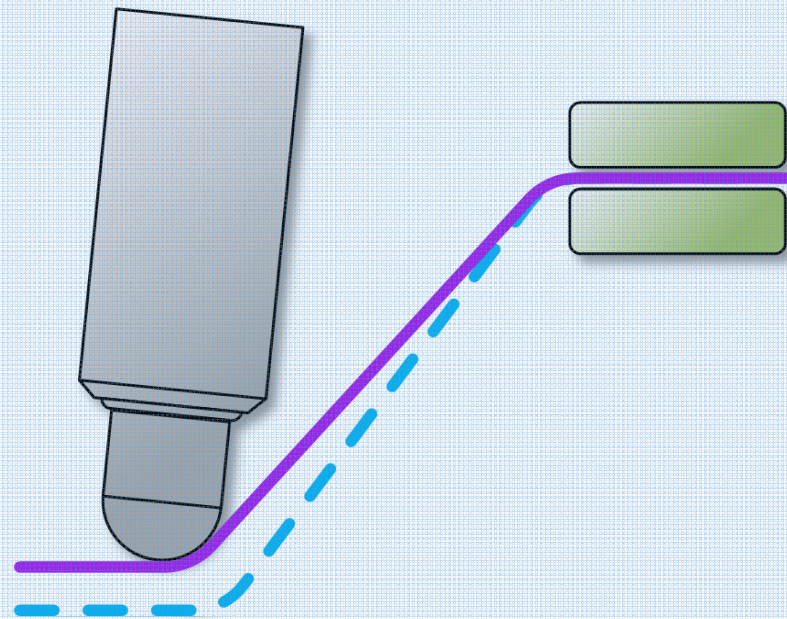
Need to maintain tool contact or else risk sparking/welding, so ADSIF is used.

# Opportunities and Challenges in Incremental Forming

- Higher formability
- **Geometric accuracy** –
  - System compliance
  - Springback in forming
  - Springback after unclamping
- Forming sequence and forming time

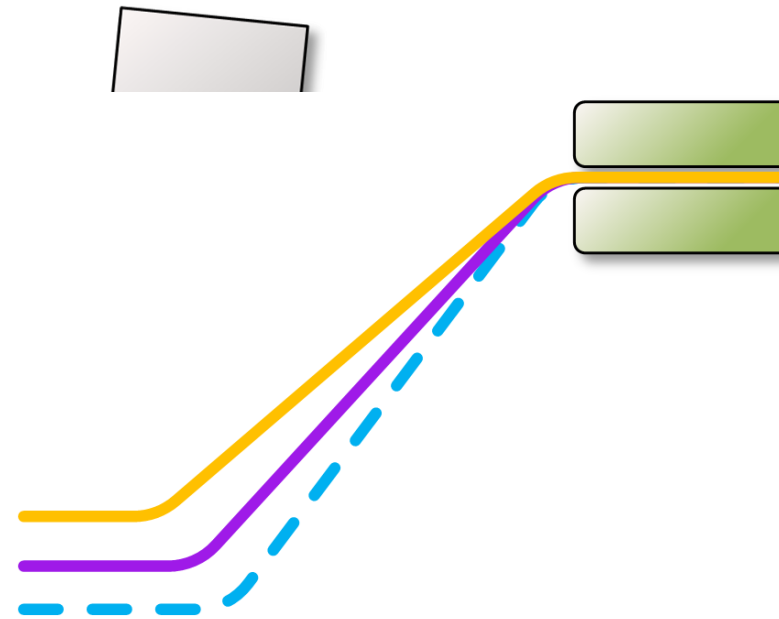
# Challenge - Geometric Accuracy

Tool/Machine Deflection

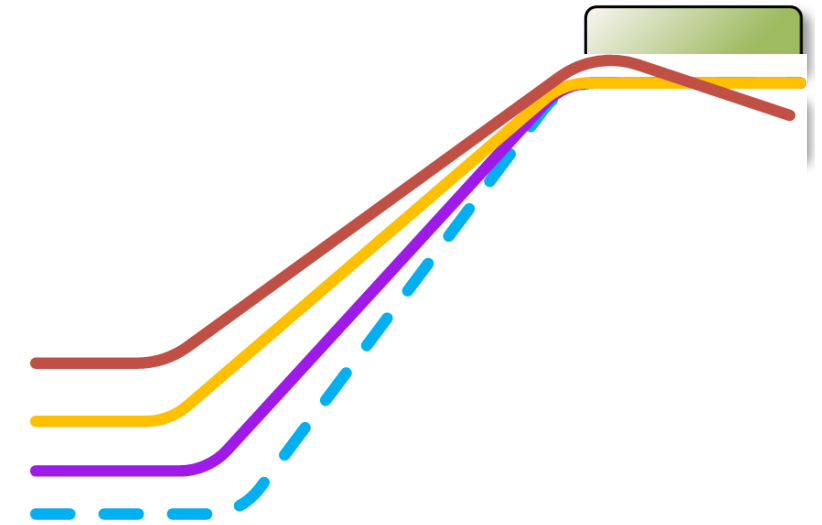


- requires **Compliance Compensation** for forming tool

In-process Springback



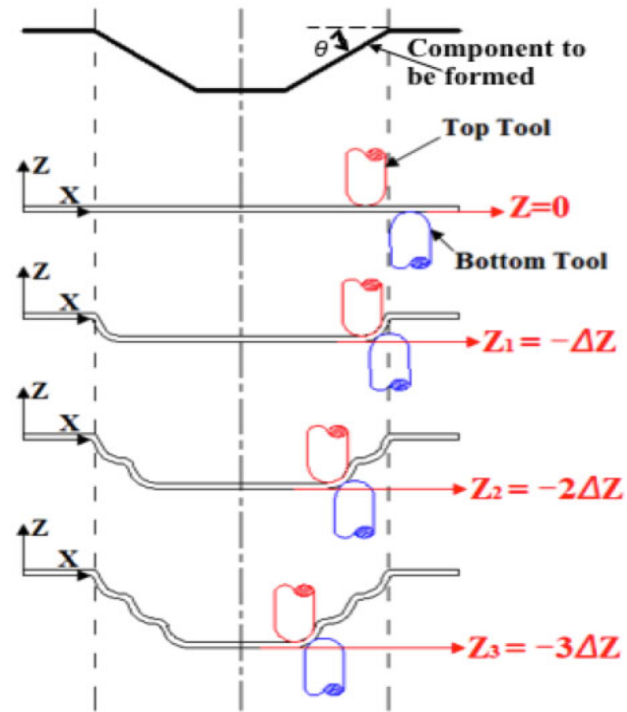
Post-process Springback



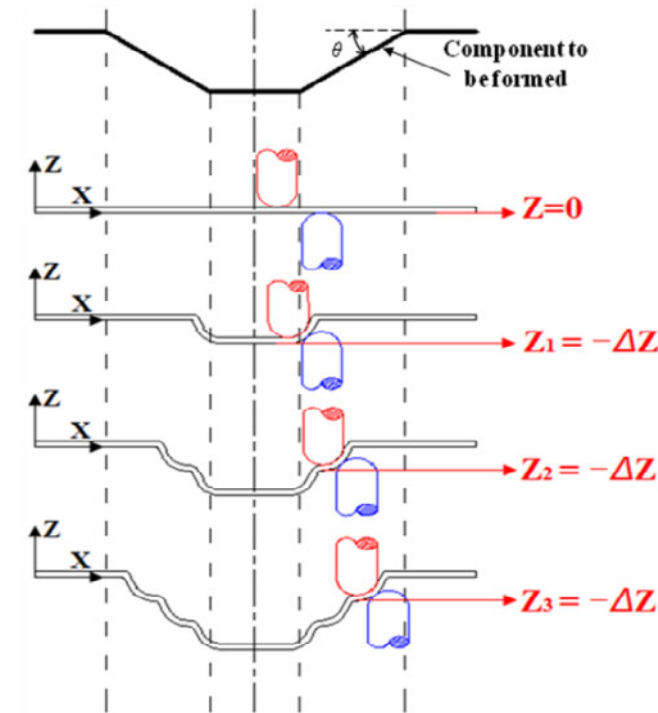
# Two Forming Strategies – DSIF and ADSIF



Double-Sided Incremental Forming (**DSIF**)

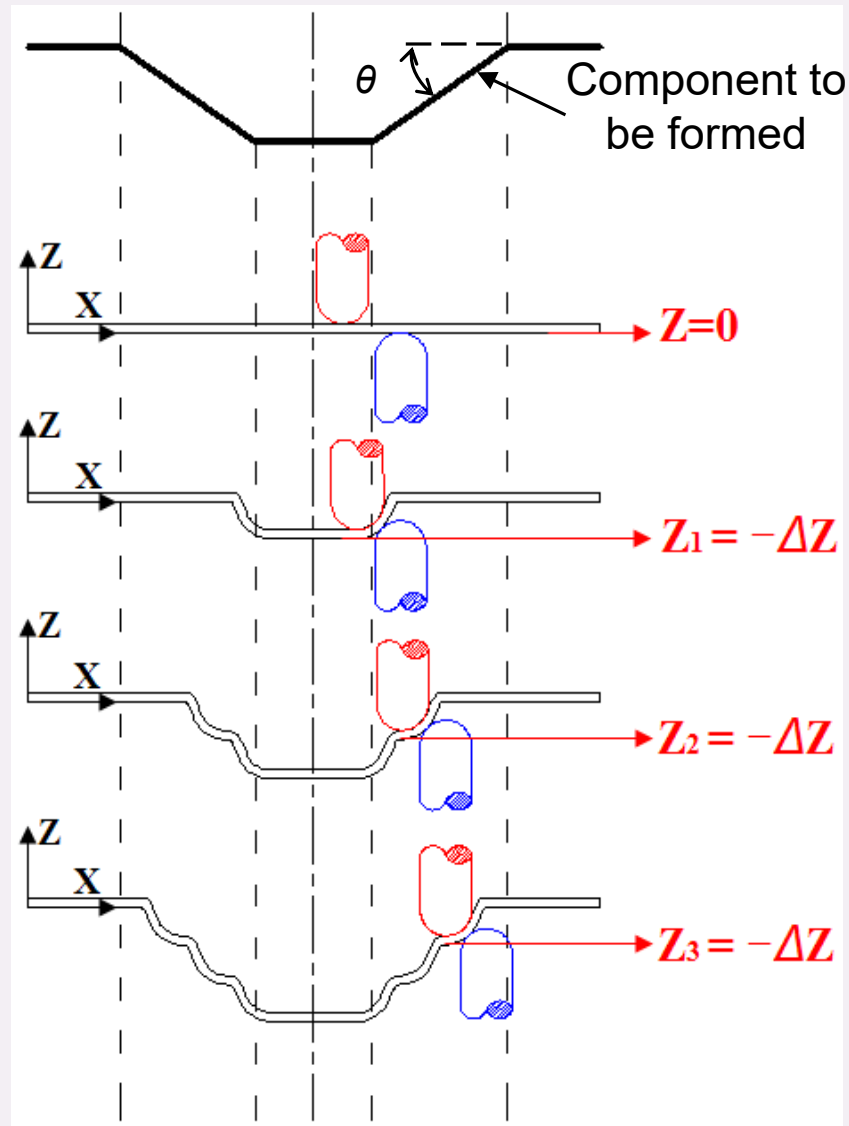


Accumulative Double-Sided Incremental Forming (**ADSIF**)

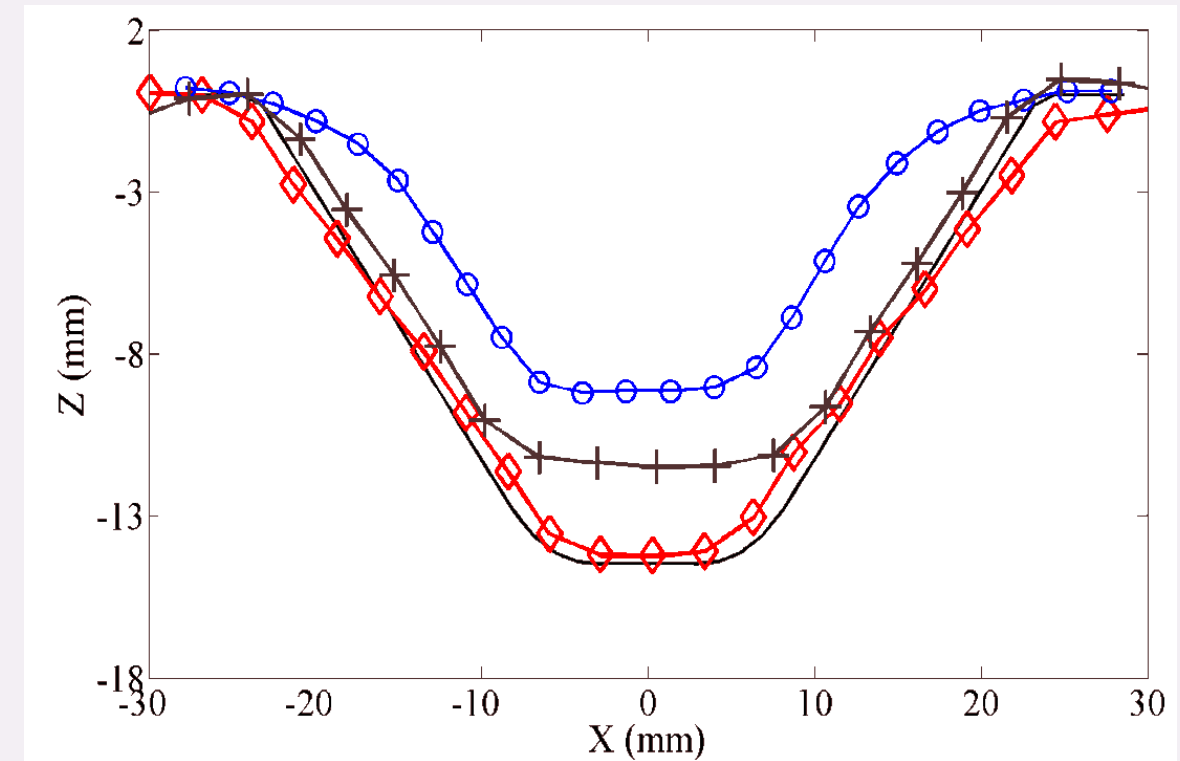


# Advantages of ADSIF

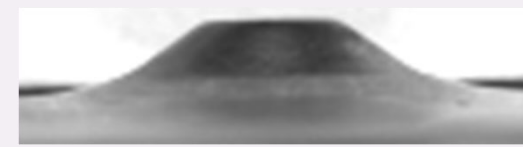
## Accumulative DSIF (ADSIF)



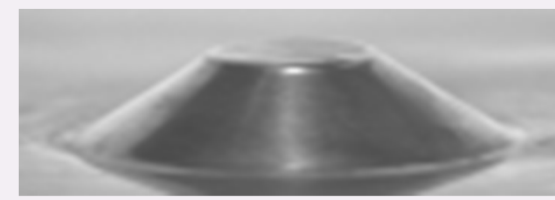
40° cone formed on 0.5 mm thick AA2024 sheet



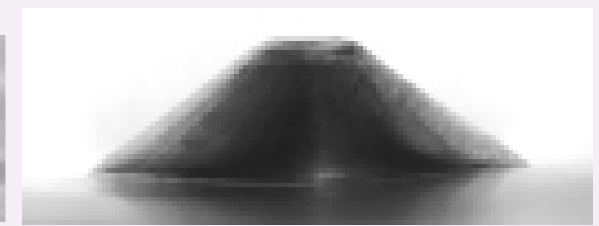
— Ideal Geometries  $\blacklozenge$  ADSIF  $\oplus$  SPIF + DSIF



SPIF

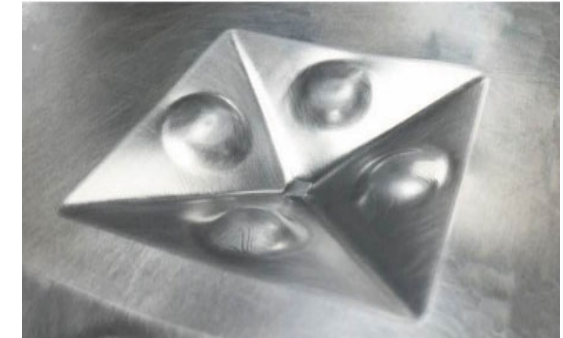
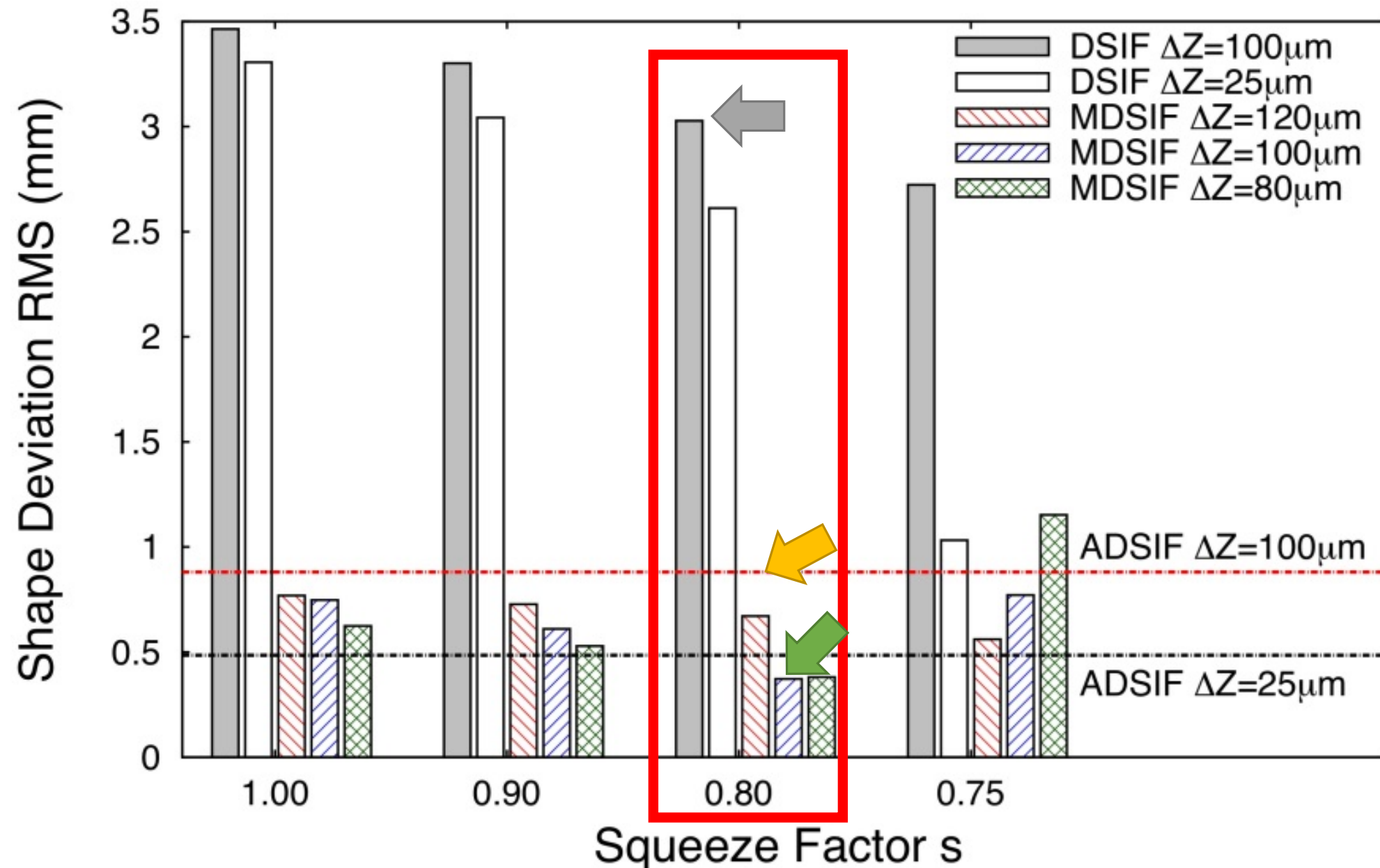


DSIF

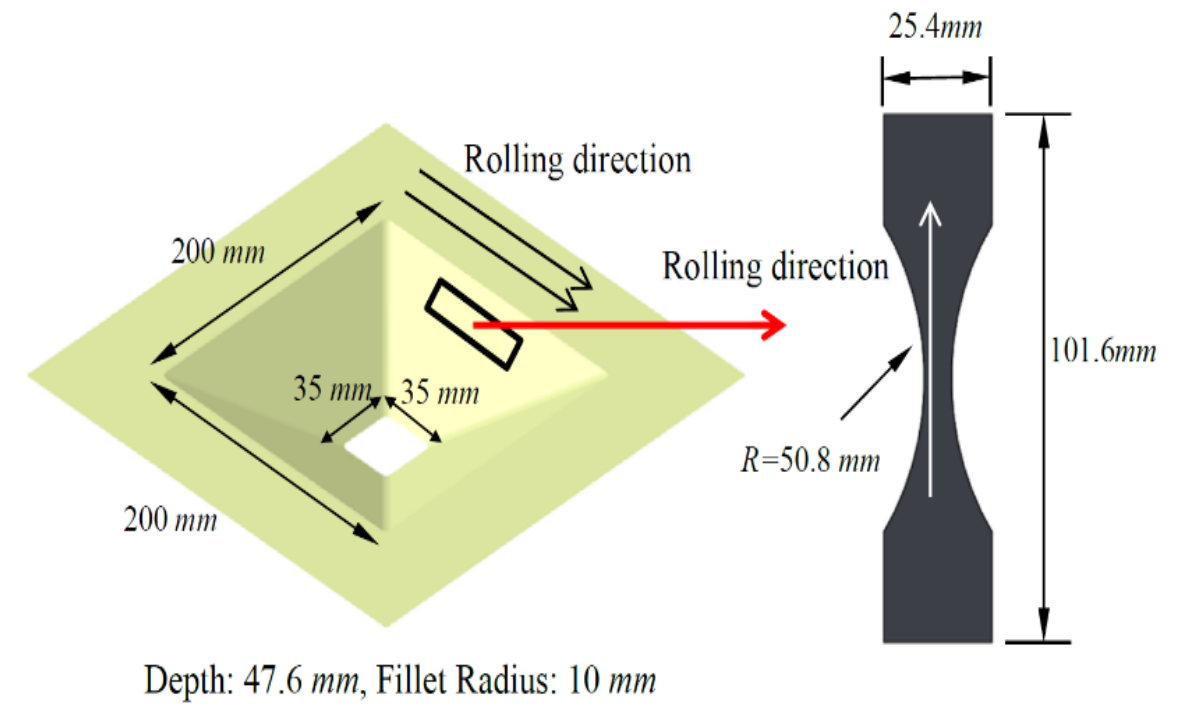
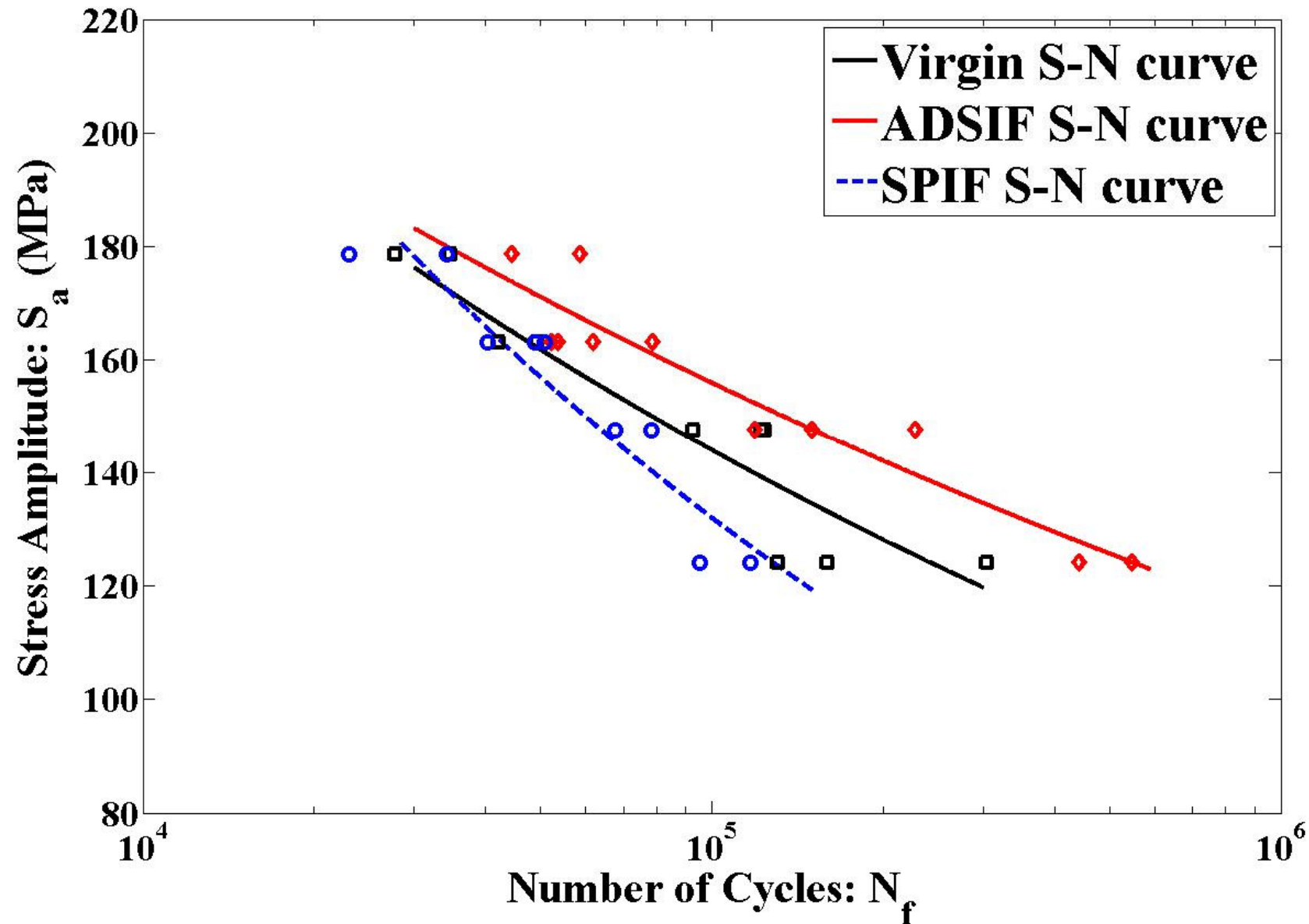


ADSIF

# Geometry Comparisons – DSIF, ADSIF, MDSIF (ADSIF+DSIF)

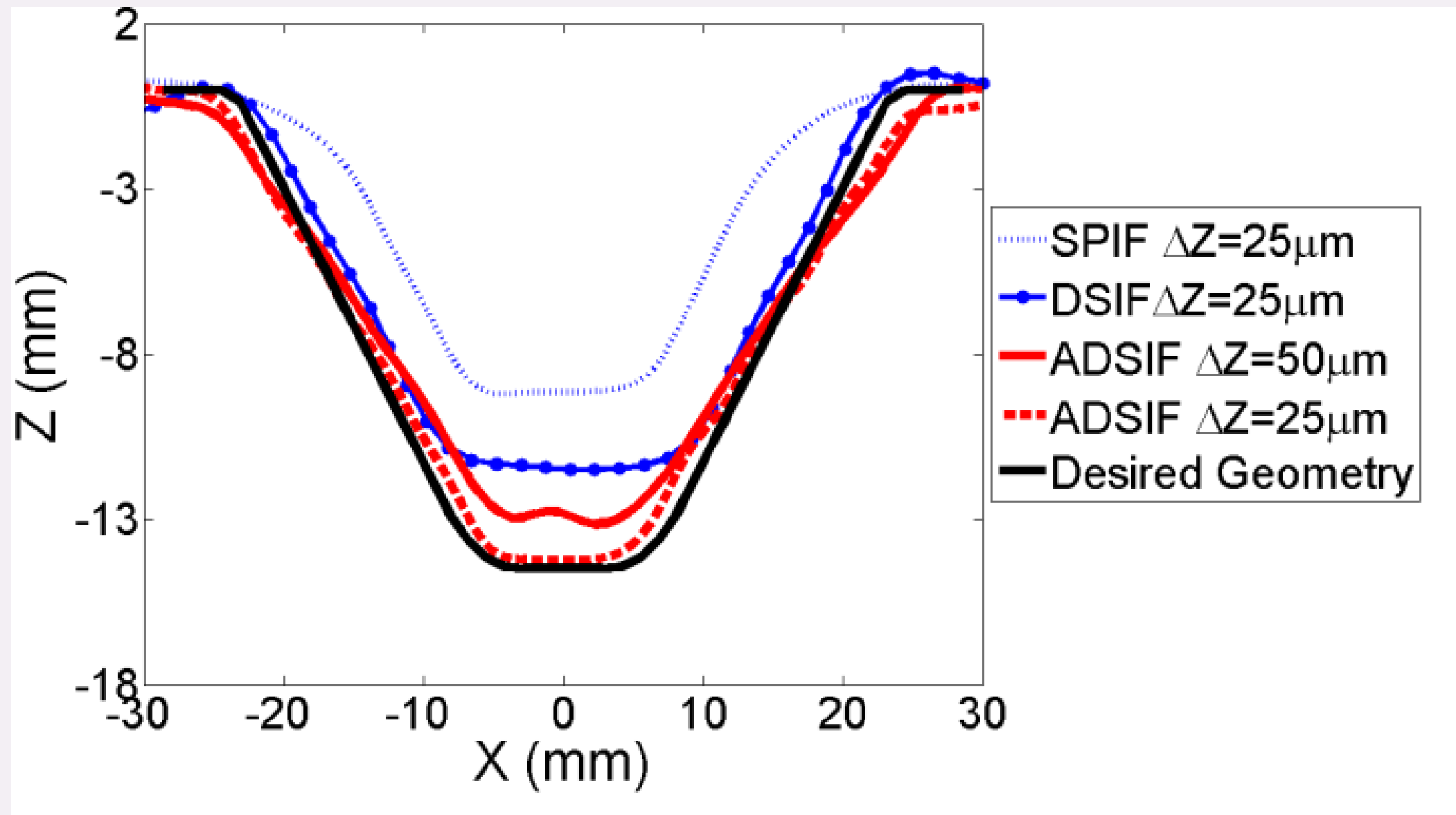


# Fatigue Life Comparison





# Challenge in ADSIF

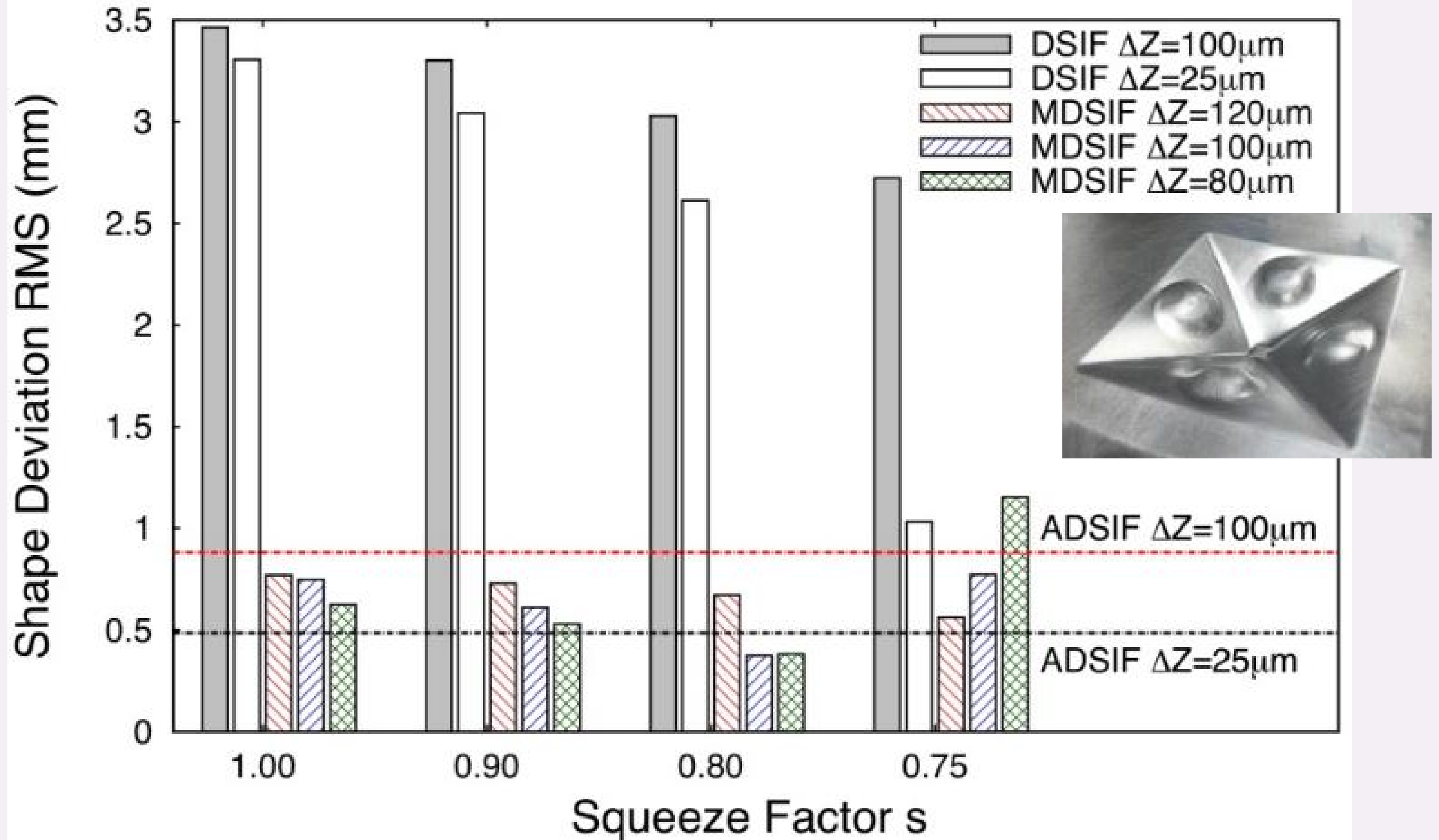


Challenge:

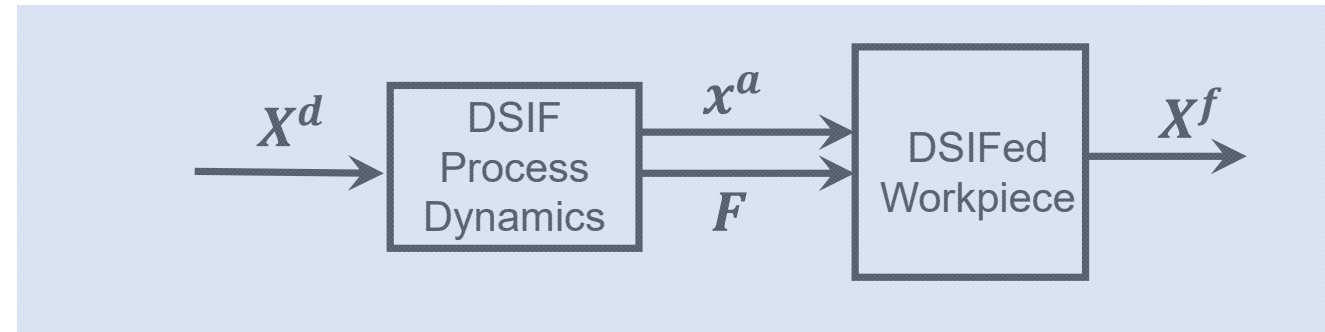
Extremely small incremental depth is needed:  $25\mu\text{m}$

# Forming Strategy: MxDSIF

Mixed Toolpath (MxDSIF) = ADSIF + DSIF



# Conventional DSIF Process



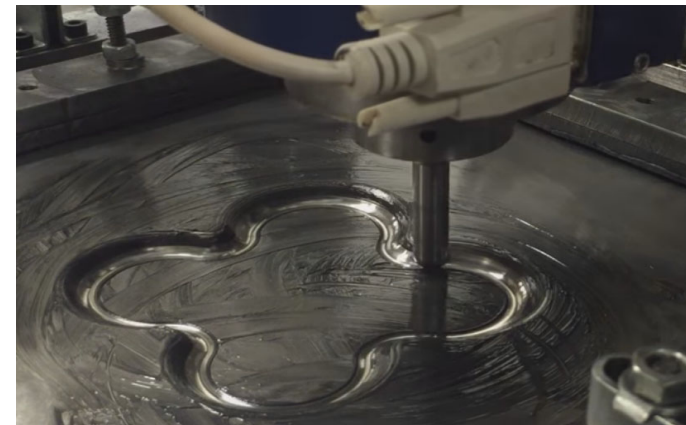
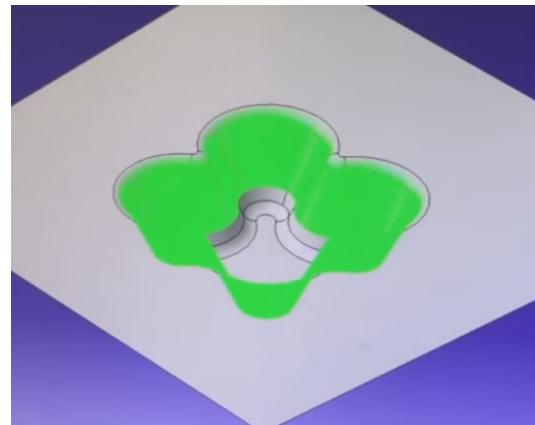
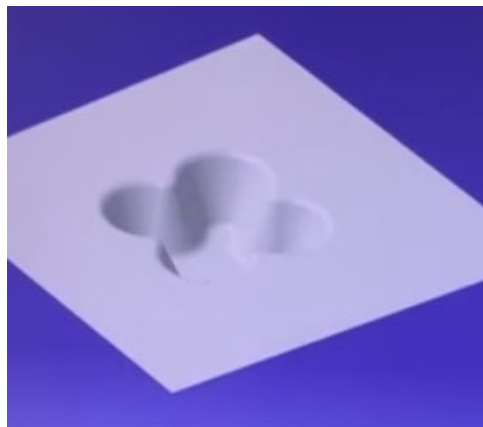
$x^d$  Desired Part Geometry



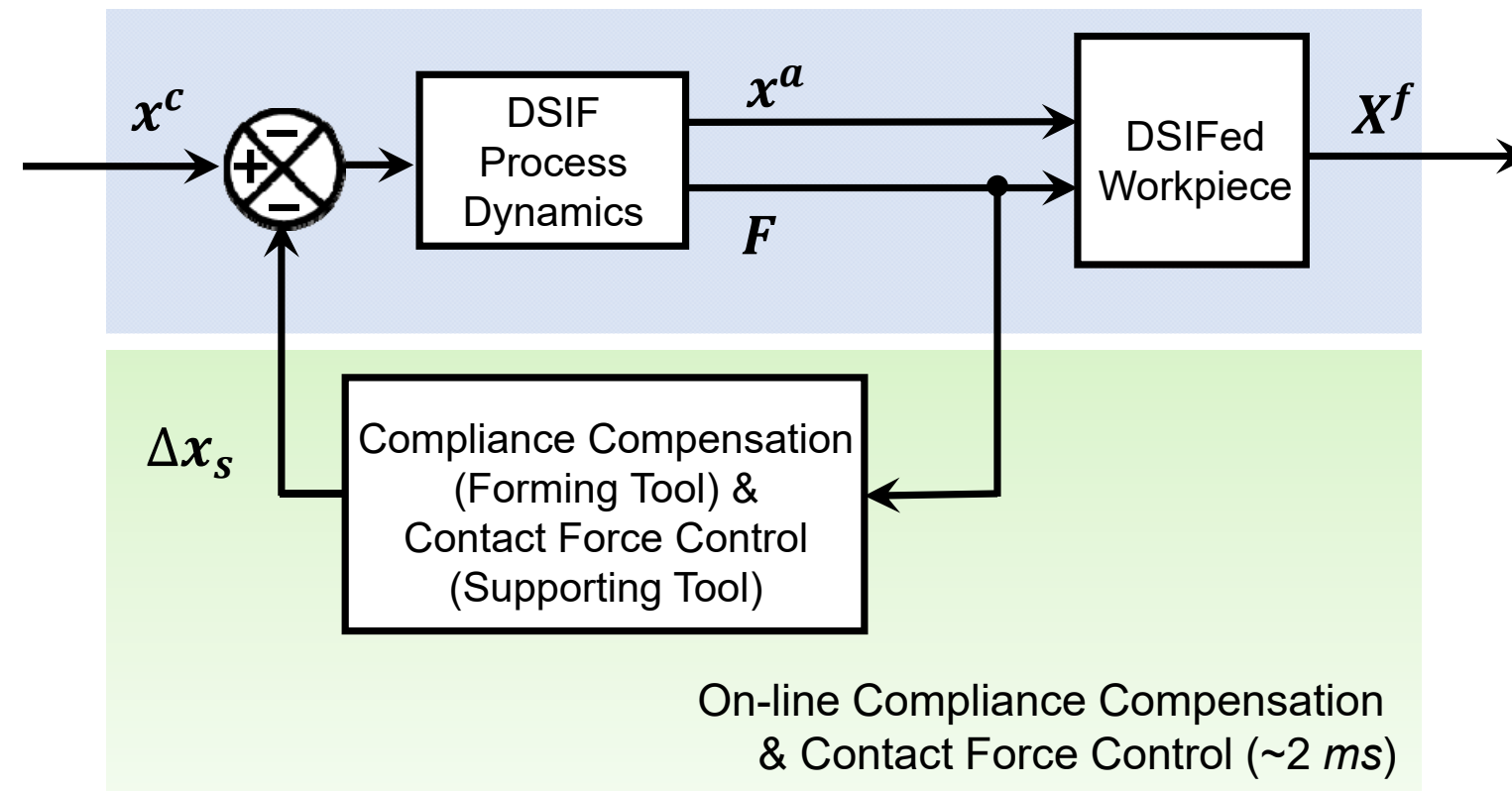
$x^a$  Actual Tooltip Position  
 $F$  Forming Force



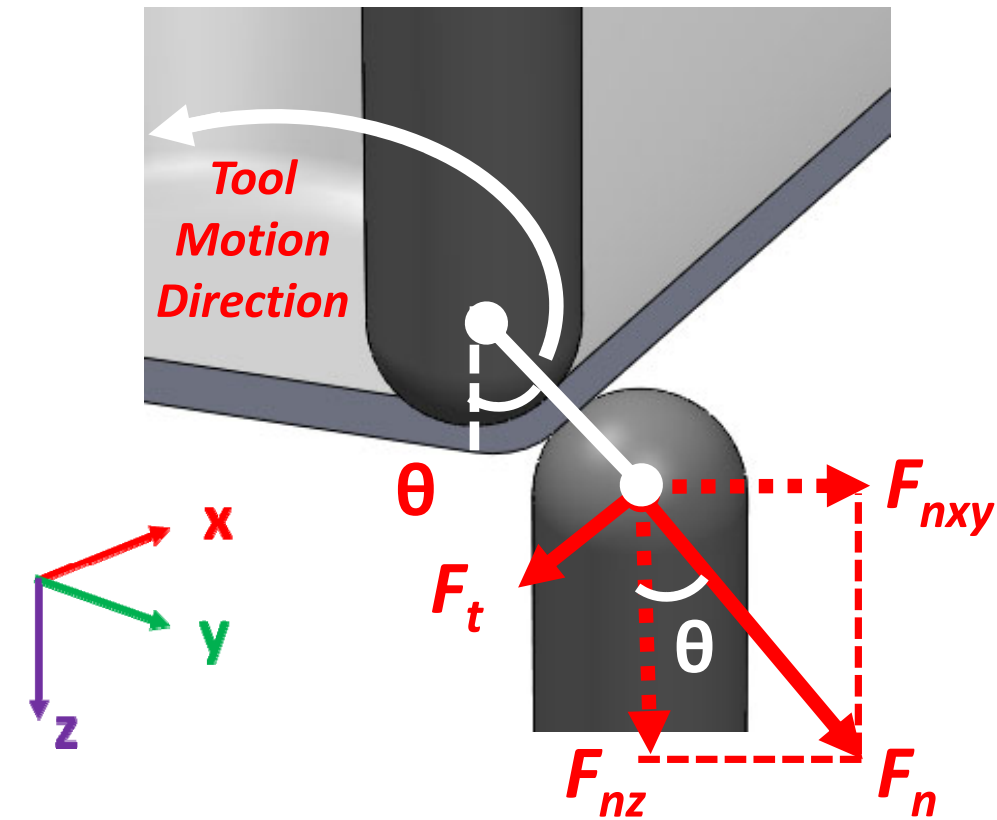
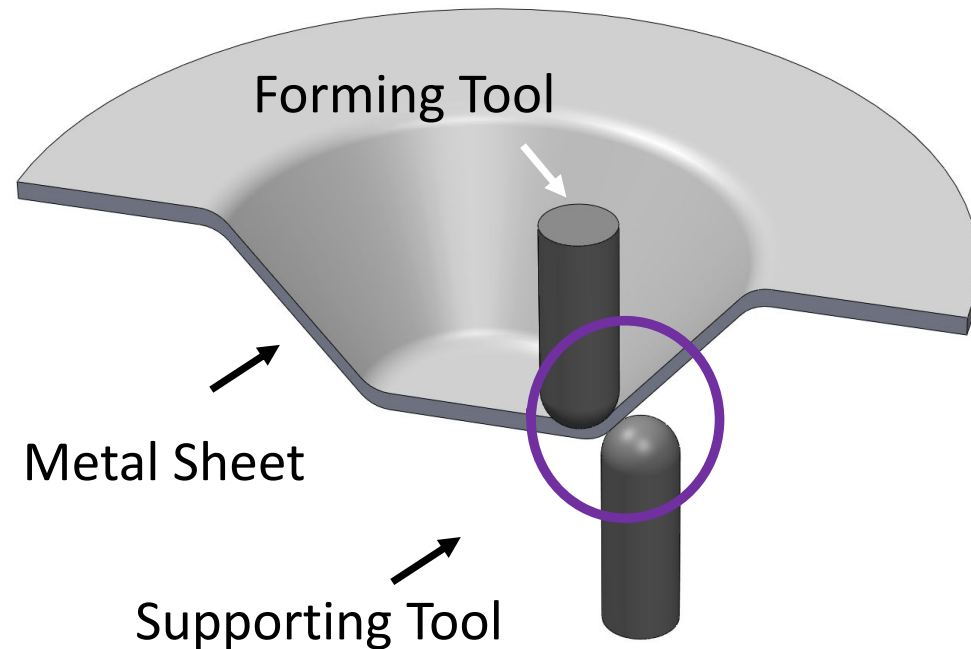
$x^f$  Final Part Geometry



# Proposed Control System for DSIF



# Force Control Algorithm



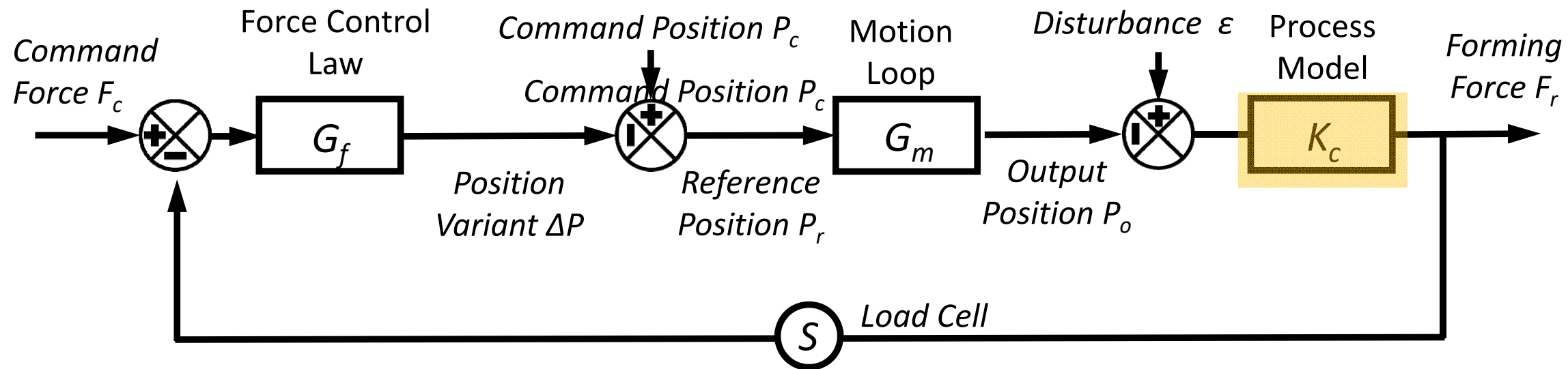
Particularly, we directly control  $F_{nxy}$  assuming:

$$F_{nz} = F_{nxy} \cot\theta$$

or

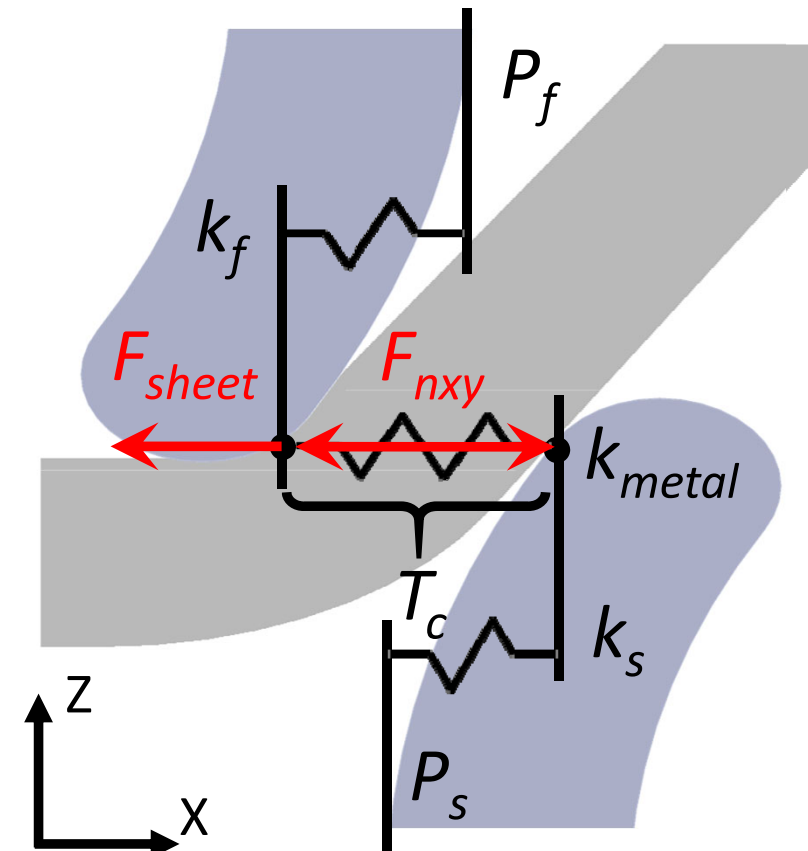
$$F_n = F_{nxy} / \sin\theta$$

# Control Scheme – Explicit Force Control



A principal characteristic of this explicit force control scheme is that the force control signal only acts as a modifier to the commanded position signal and, consequently, does not require direct interference with the inner position control loop,  $G_m$ .

# Determination of the Process Model



$P_f, P_s$  : controller output tool position

$F_{nxy}$  : normal contact force in x-y plane

$F_{sheet}$  : sheet force on forming tool

$k_f, k_s$  : tool and machine stiffness

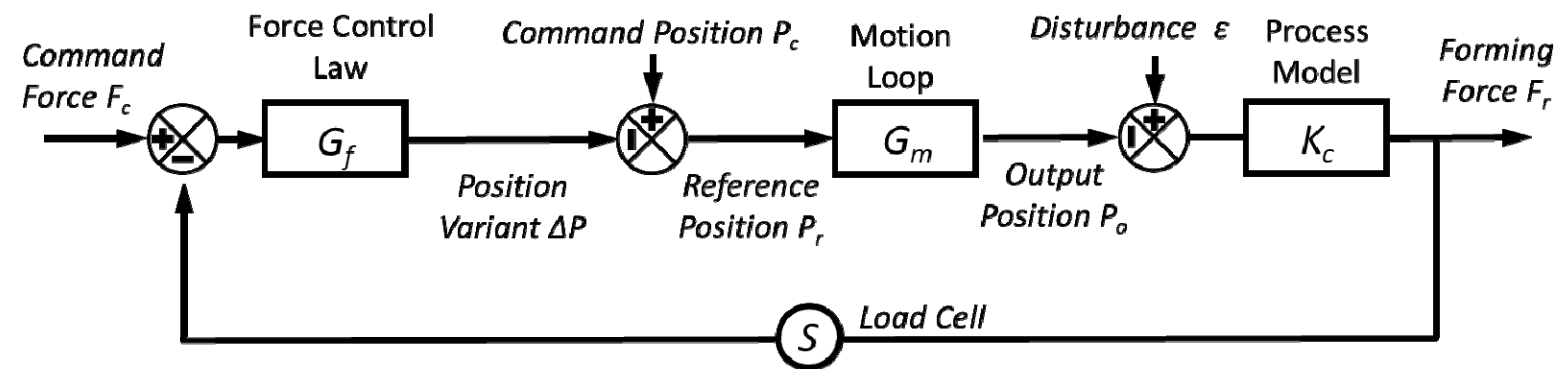
$k_{metal}$  : squeezing stiffness for sheet metal

$T_c$  : horizontal sheet thickness

$$F_r = K_c(\varepsilon - P_s),$$

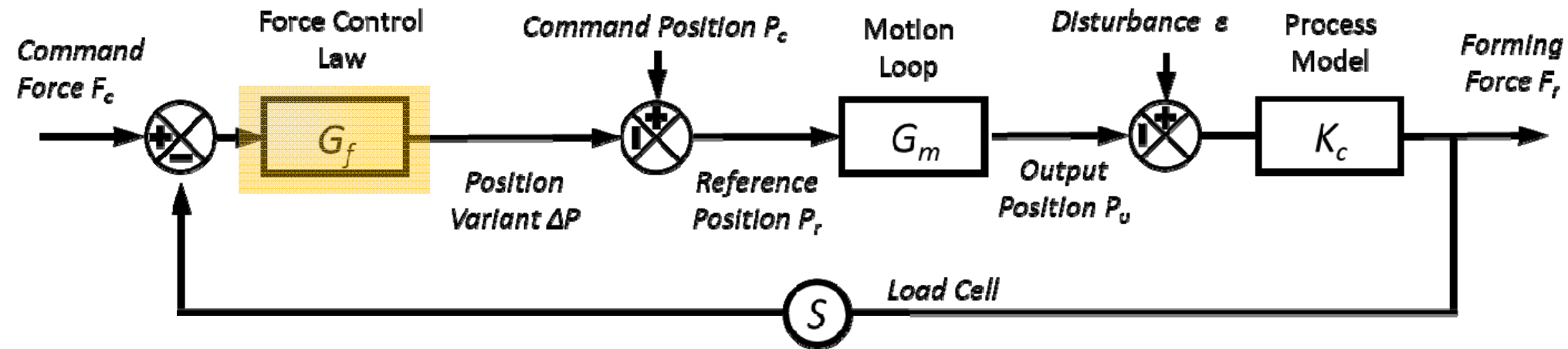
$$K_c = 1 / \left( \frac{1}{k_f} + \frac{1}{k_{metal}} + \frac{1}{k_s} \right)$$

$$\varepsilon = -F_{sheet}/k_f + P_f + T_c$$





# Control Scheme – Explicit Force Control

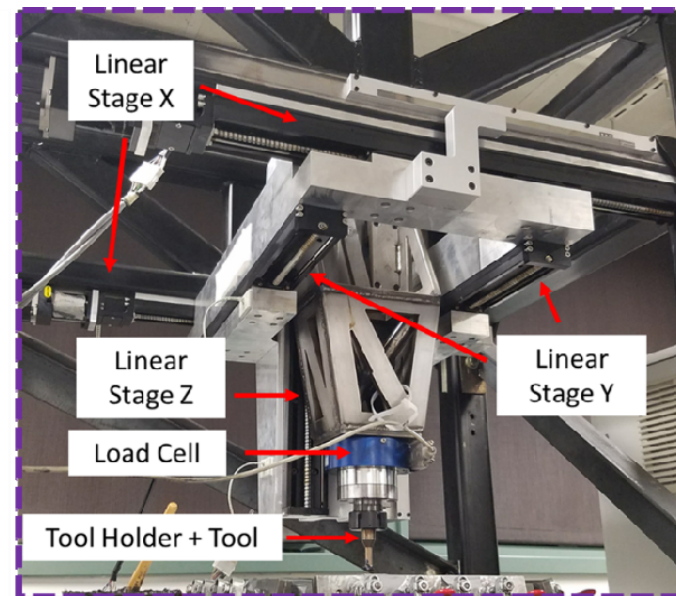
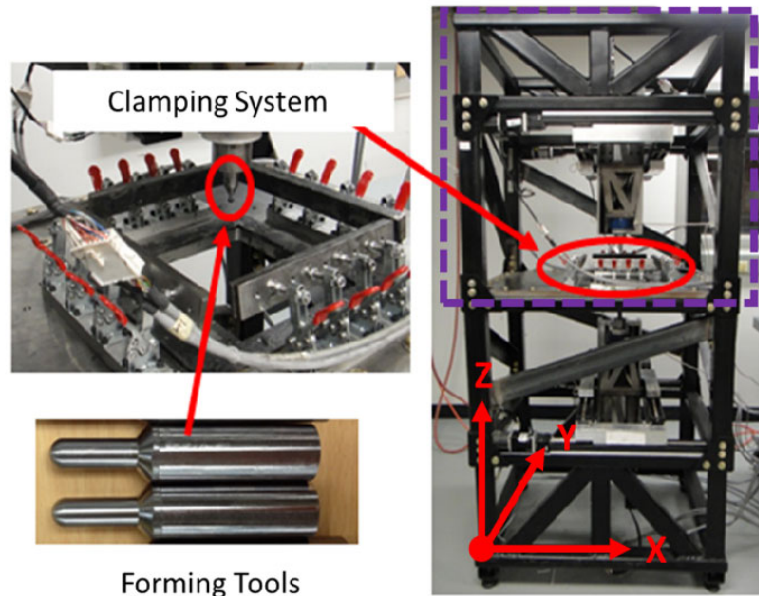


$$F_r = \frac{G_f G_m K_c}{1 + G_f G_m K_c} F_c + \frac{G_m K_c}{1 + G_f G_m K_c} P_c + \frac{K_c}{1 + G_f G_m K_c} \varepsilon$$

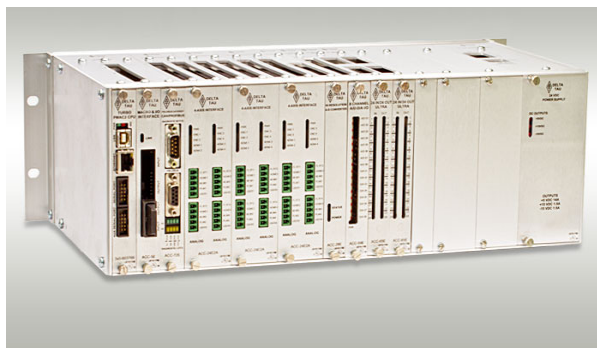
- To guarantee the possibility of implementing the control algorithm in most standard controllers, a **simple integral controller** ( $K_i/s$ ) is proposed for  $G_f$ .
- The advantages of integral control are its low pass nature and **zero steady state error** for a constant desired force and a disturbance,  $\varepsilon$ , for a given  $K_c$ .

$$\lim_{s \rightarrow 0} \left( \frac{G_f G_m K_c}{1 + G_f G_m K_c} \right) = 1, \lim_{s \rightarrow 0} \left( \frac{G_m K_c}{1 + G_f G_m K_c} \right) = 0, \lim_{s \rightarrow 0} \left( \frac{K_c}{1 + G_f G_m K_c} \right) = 0$$

# DSIF Machine System at Northwestern University



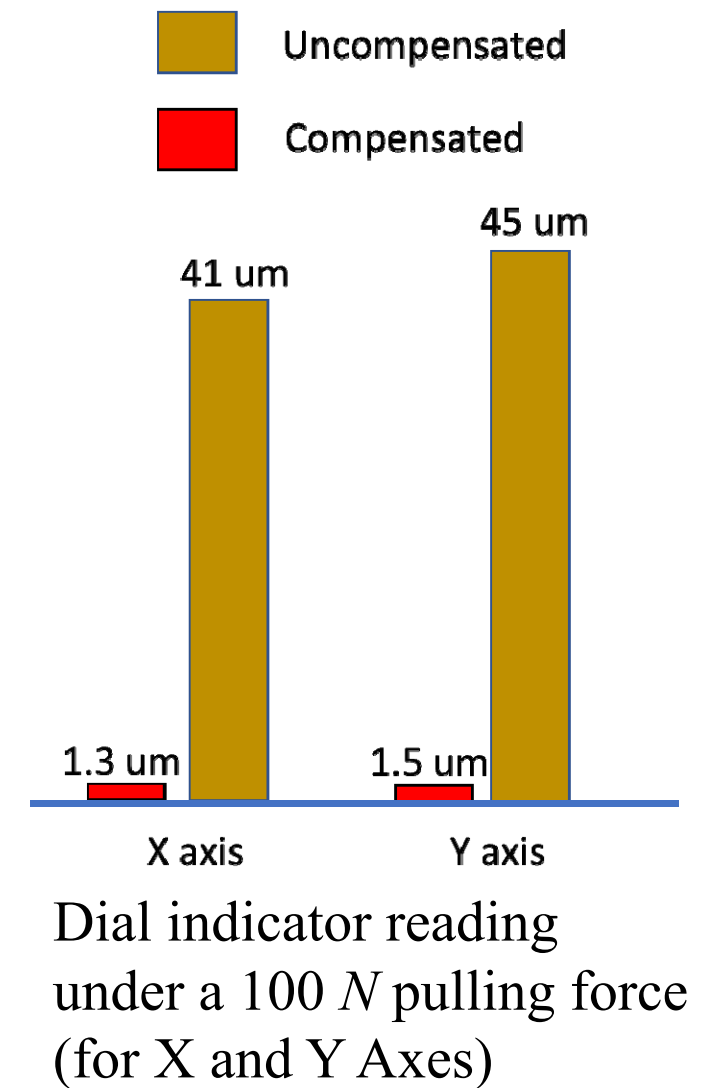
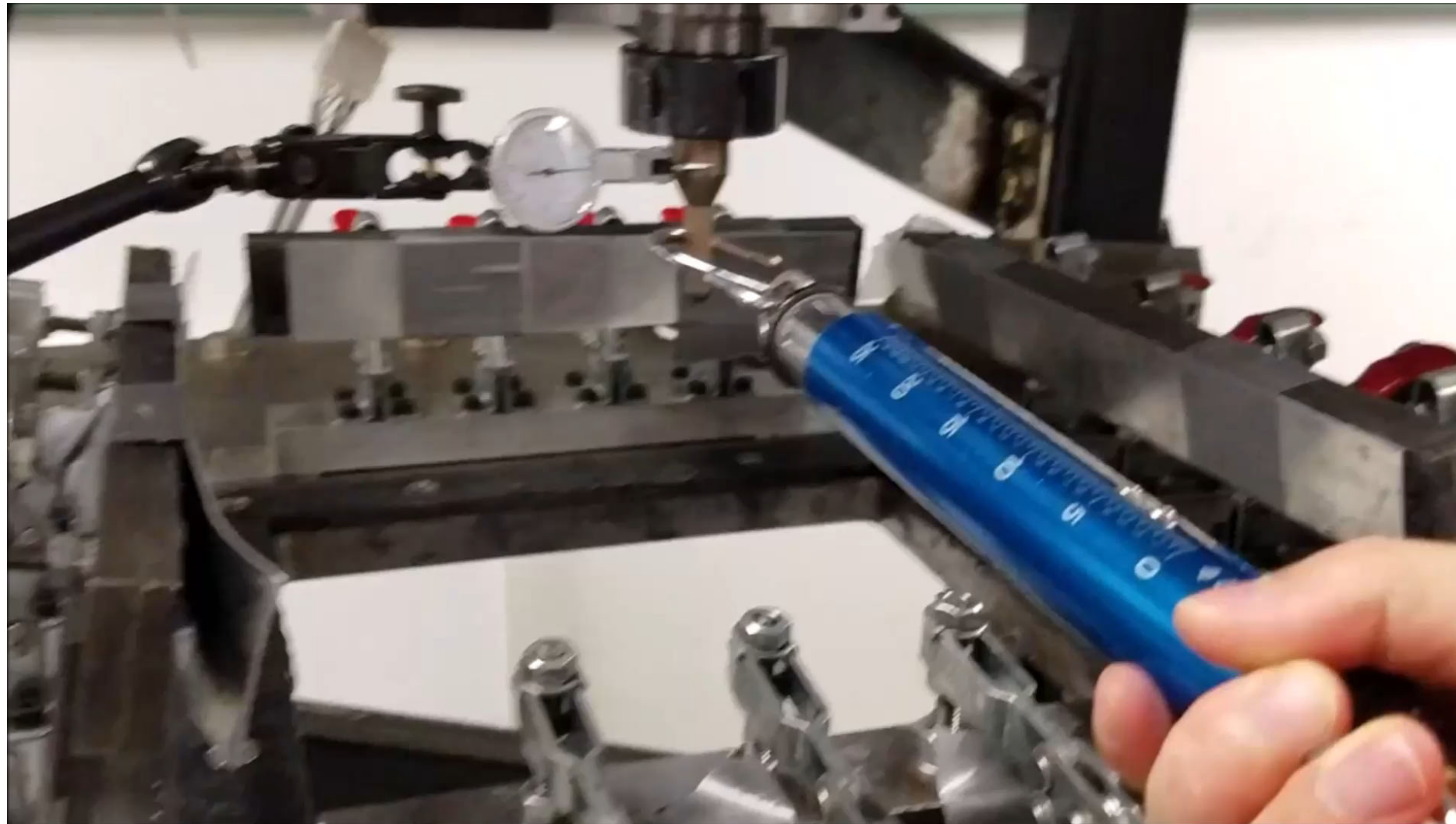
Turbo PMAC Controller  
80 MHz DSP56303 CPU  
~ 10 Mb Memory



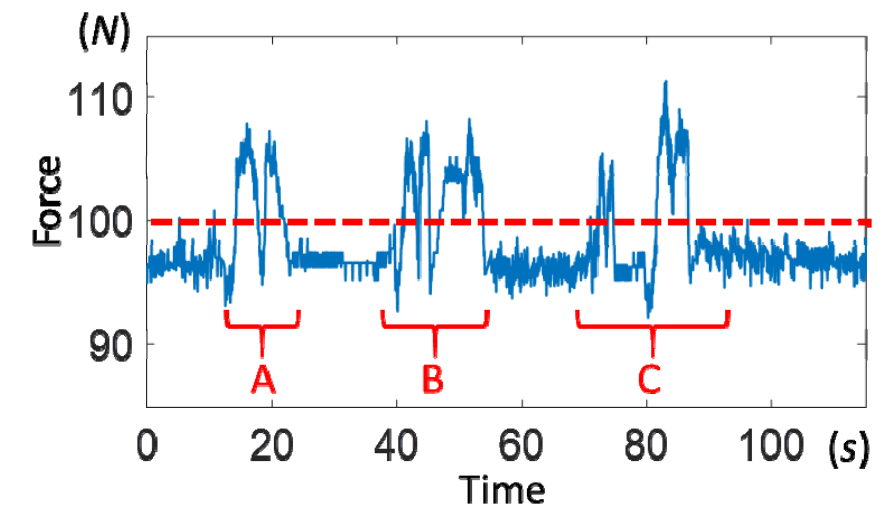
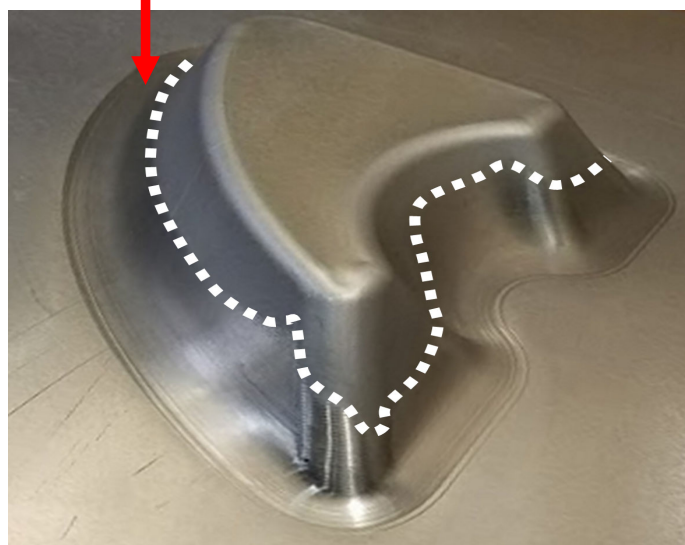
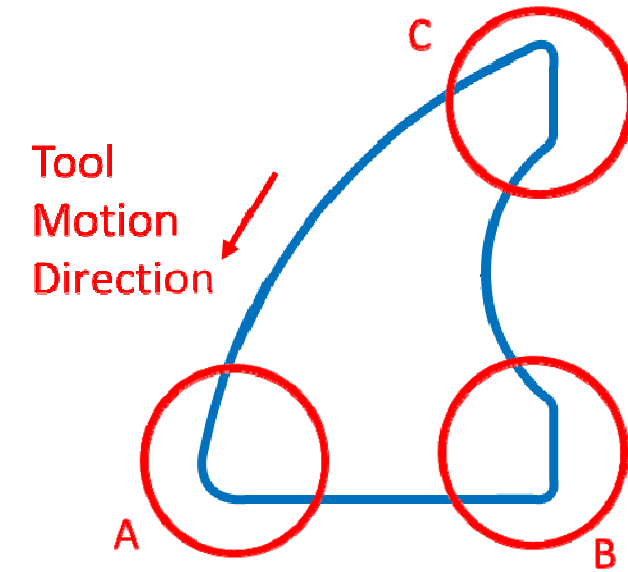
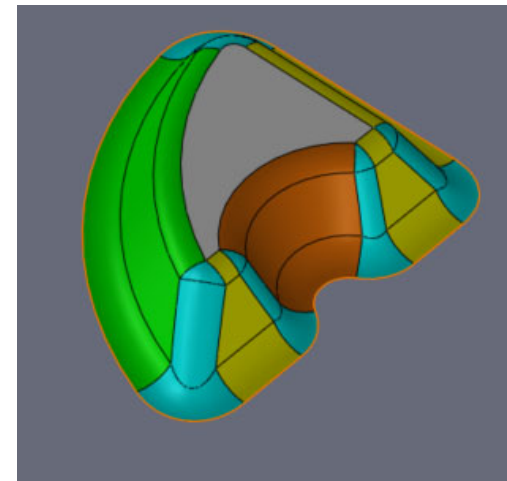
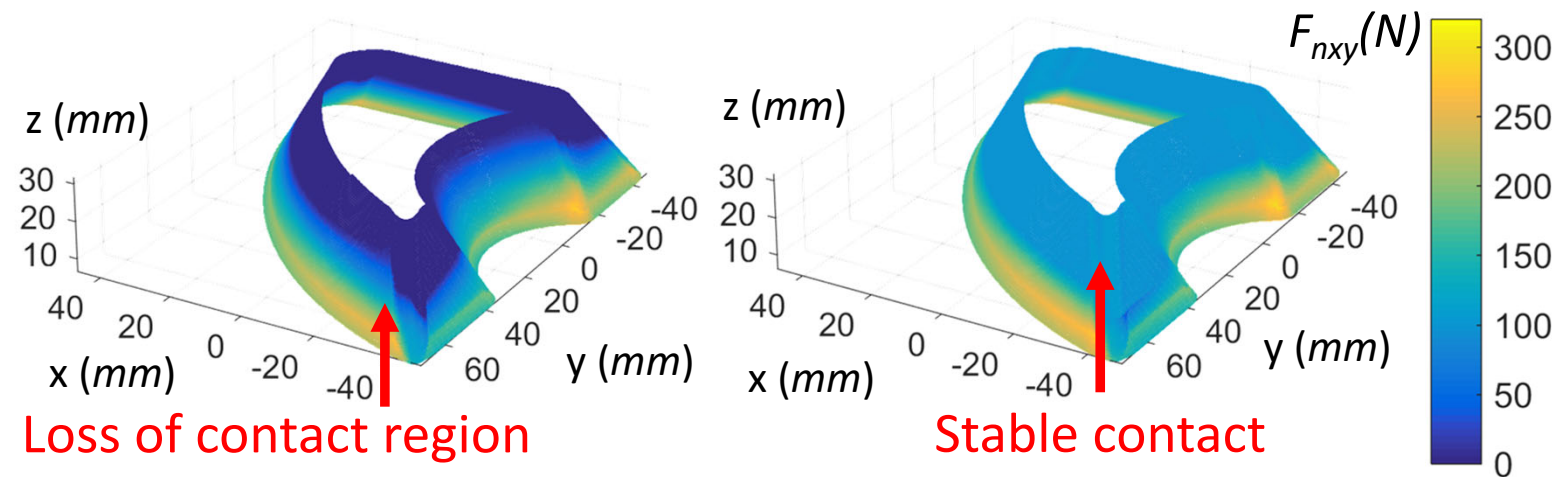
Parameters	Value
Total Motor	10
Maximum Tool Speed	9.6 mm/s
Load Cell Resolution	1 N
Servo Frequency	2.2 kHz
Linear Position Error	< 12 $\mu\text{m}$ / $\pm 100$ mm
Circular Position Error	< 15 $\mu\text{m}$ for $R = 50$ mm

Stiffness	Value (N/ $\mu\text{m}$ )
X - forming	0.98
Y - forming	1.11
Z- forming	6.67
X- Supporting	0.91
Y - Supporting	0.76
Z- Supporting	6.67
Metal (AA5754-O)	~20.0
$K_c$ (X)	0.46
$K_c$ (Y)	0.44
$K_c$ (Z)	2.86

# Experimental Verification – Compliance Compensation

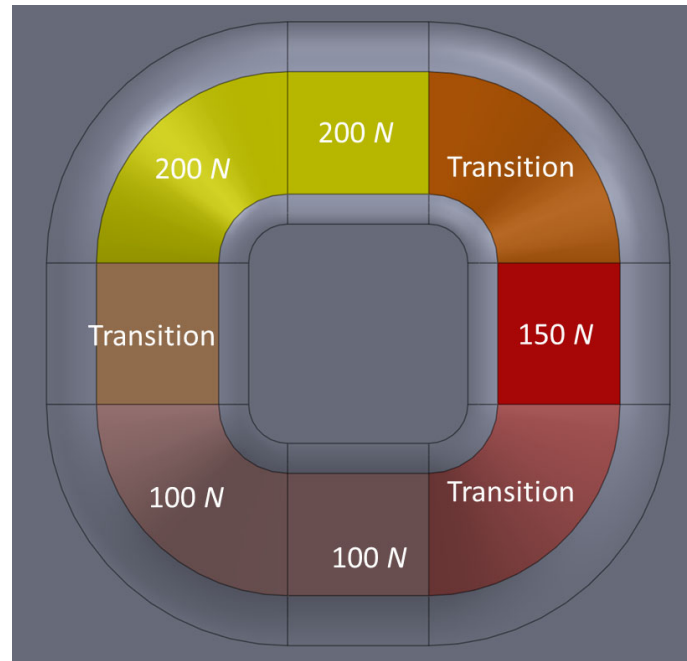
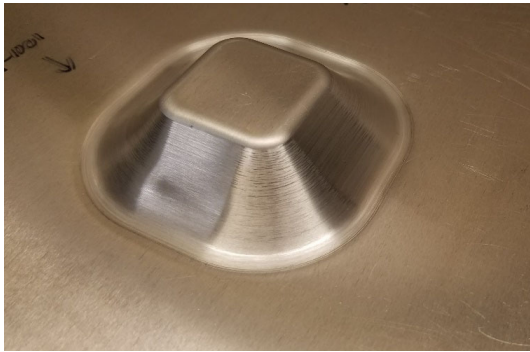


# Force Control for the Complex Geometry

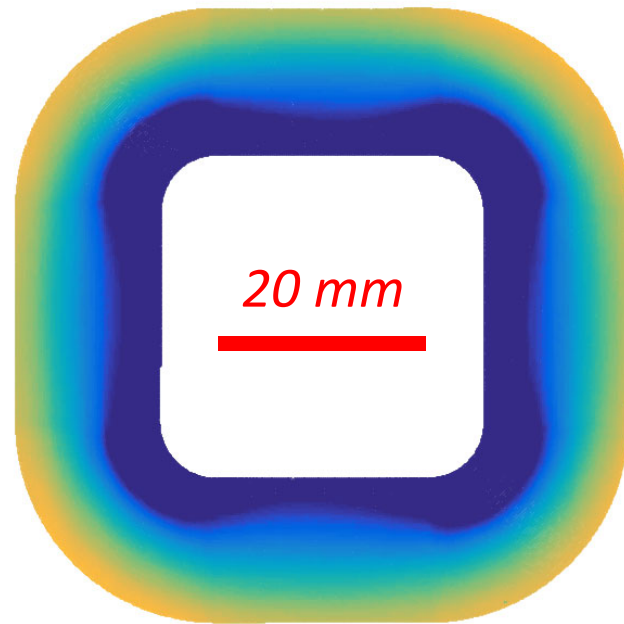
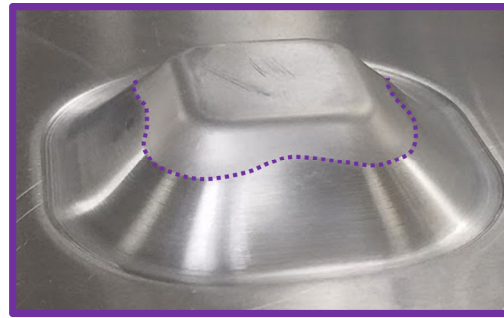


\* AA1100-O, 1 mm thick, 5 mm radius tool

# Complex Command Contact Force



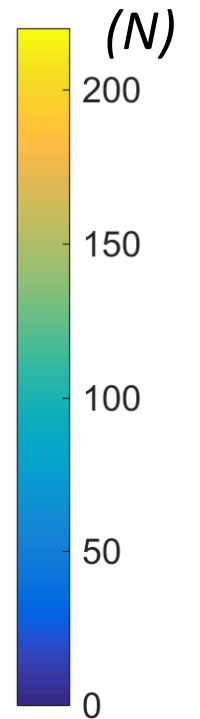
- AA5754-O, 1 mm thick, 5 mm radius tool



$F_{nxy}$  without Force Control



$F_{nxy}$  with Force Control



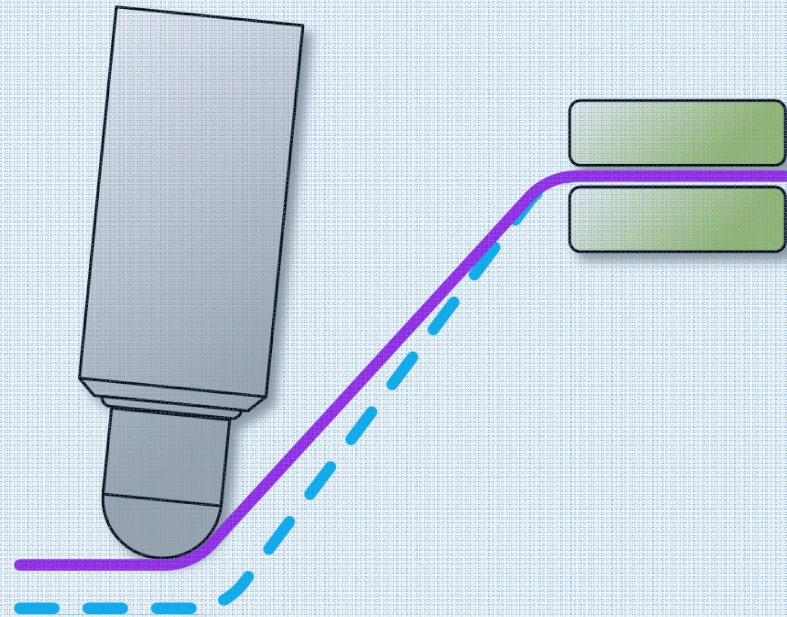
# Conducted Experiments to Examine Applicability

Test Case	A	B	C	D	E	F	G
Shape	Funnel	Funnel	Cone	Fin	Pyramid	Funnel	Cone
Aluminum Alloy	1100-O	5754-O	2024-T3	1100-O	5754-O	1100-O	5754-O
Strategy	DSIF	DSIF	ADSIF	DSIF	DSIF	DSIF	DSIF
Sheet Thickness	1.0 mm	1.0 mm	0.5 mm	1.0 mm	1.0 mm	1.0 mm	1.0 mm
Tool Radius	4.5 mm	5.0 mm	2.5 mm	5.0 mm	5.0 mm	4.5 mm	5.0 mm
Inc. Depth	0.5 mm	0.5 mm	0.1 mm	0.5 mm	0.2 mm	0.5 mm	0.2 mm
Command $F_{nxy}$	120 N	200 N	180 N	100 N	100-200 N	120 N	350 N
Wall Angle $\phi$	$\geq 50^\circ$	$\geq 65^\circ$	$40^\circ$	$60^\circ$	$45^\circ$	$\geq 60^\circ$	$55^\circ$
Tool Speed	5 mm/s	5 mm/s	5 mm/s	5 mm/s	5 mm/s	8 mm/s	5 mm/s

\* Force control error was kept less than  $\pm 10$  N for all cases

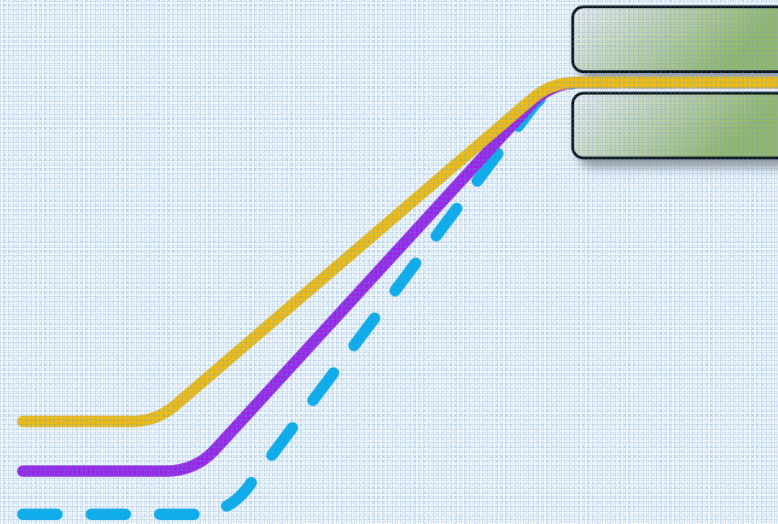
# Challenge - Geometric Accuracy

Tool/Machine Deflection



- requires **Compliance Compensation** for forming tool

In-process Springback

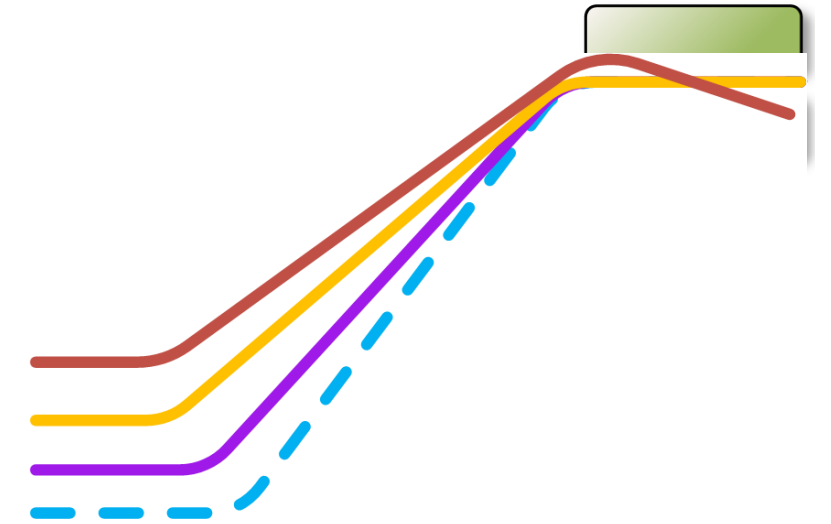


- requires **Springback Compensation**

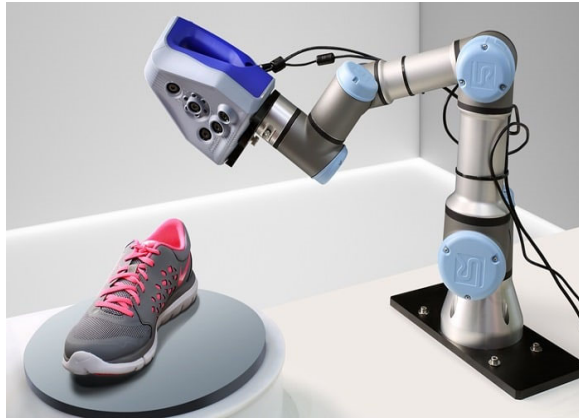


Can we enhance the functions of tooling?

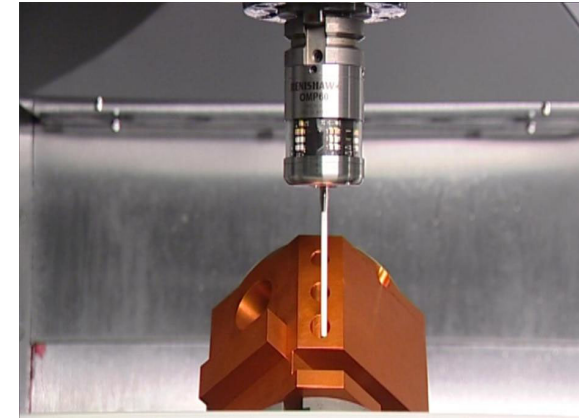
Post-process Springback



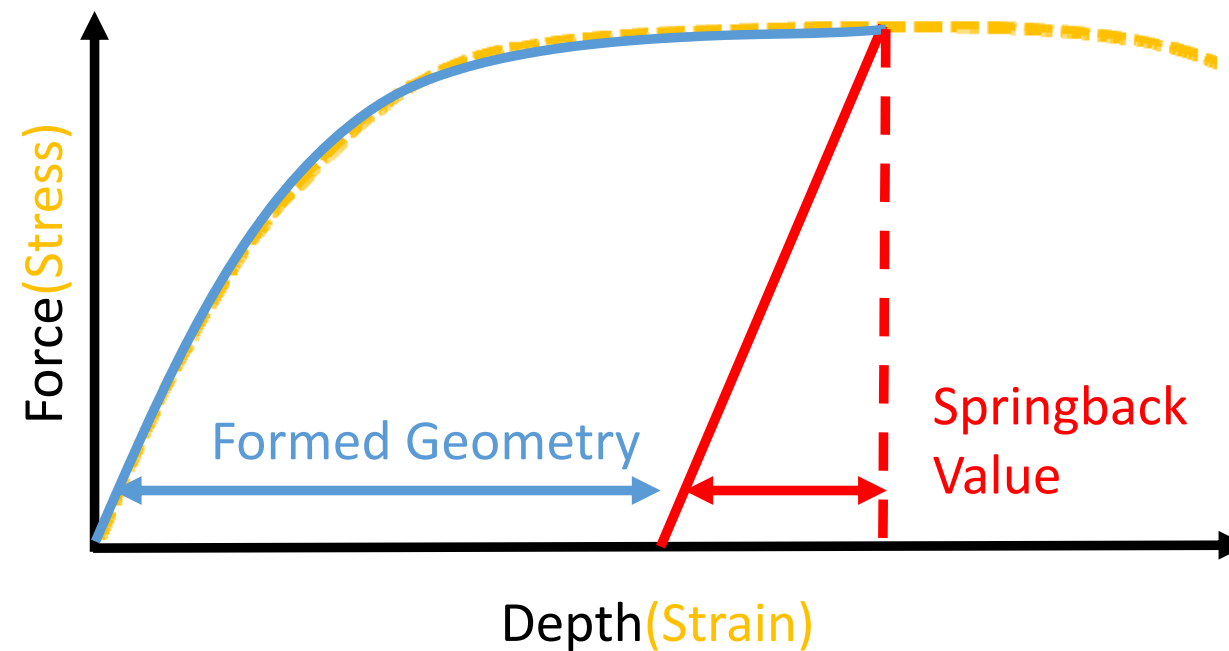
# Springback Measurement – Smart Tooling



- Accuracy vs price
- Surface texturing requirement
- Space requirement



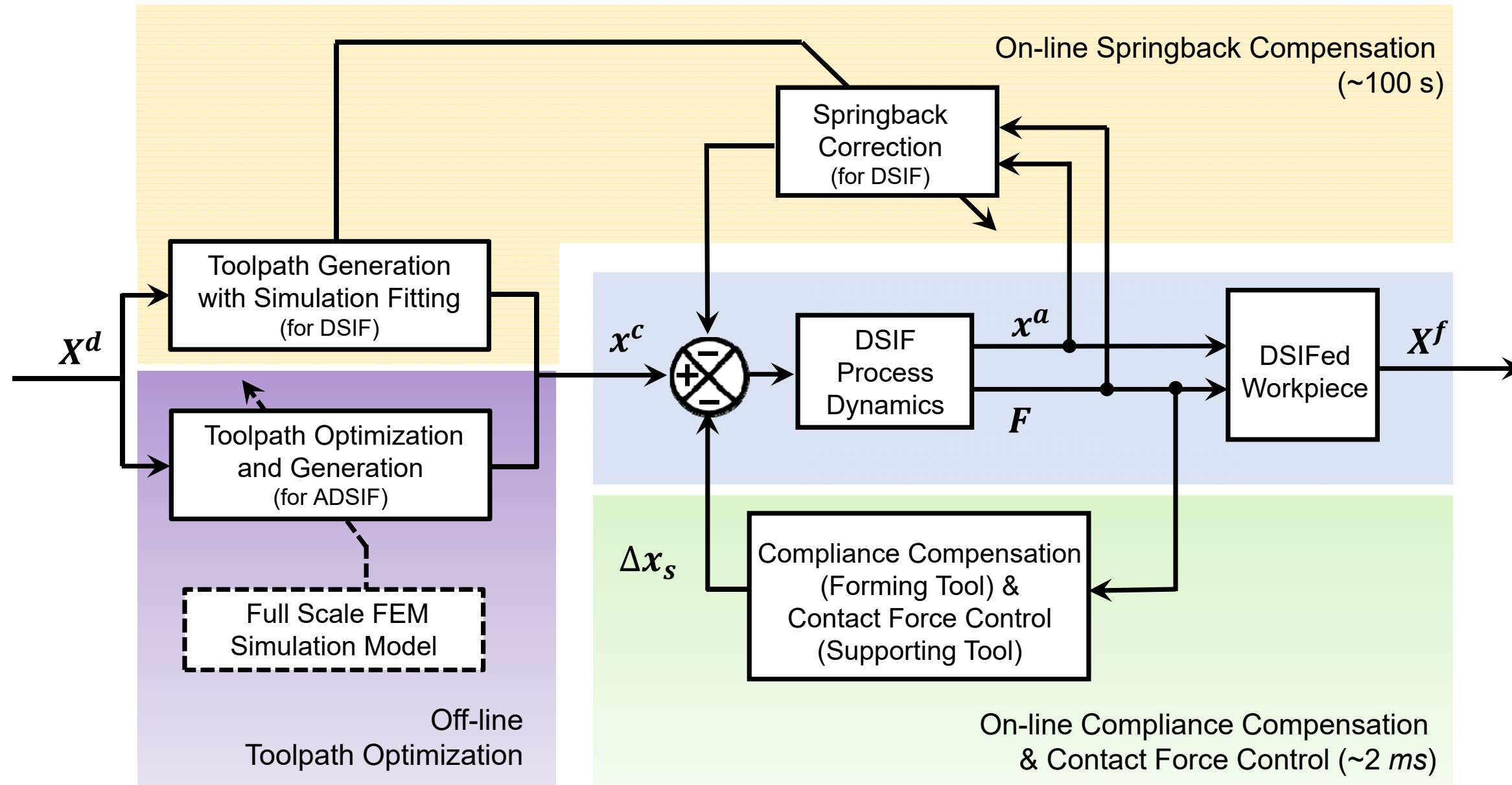
- Speed
- Tool exchangeability
- Space requirement



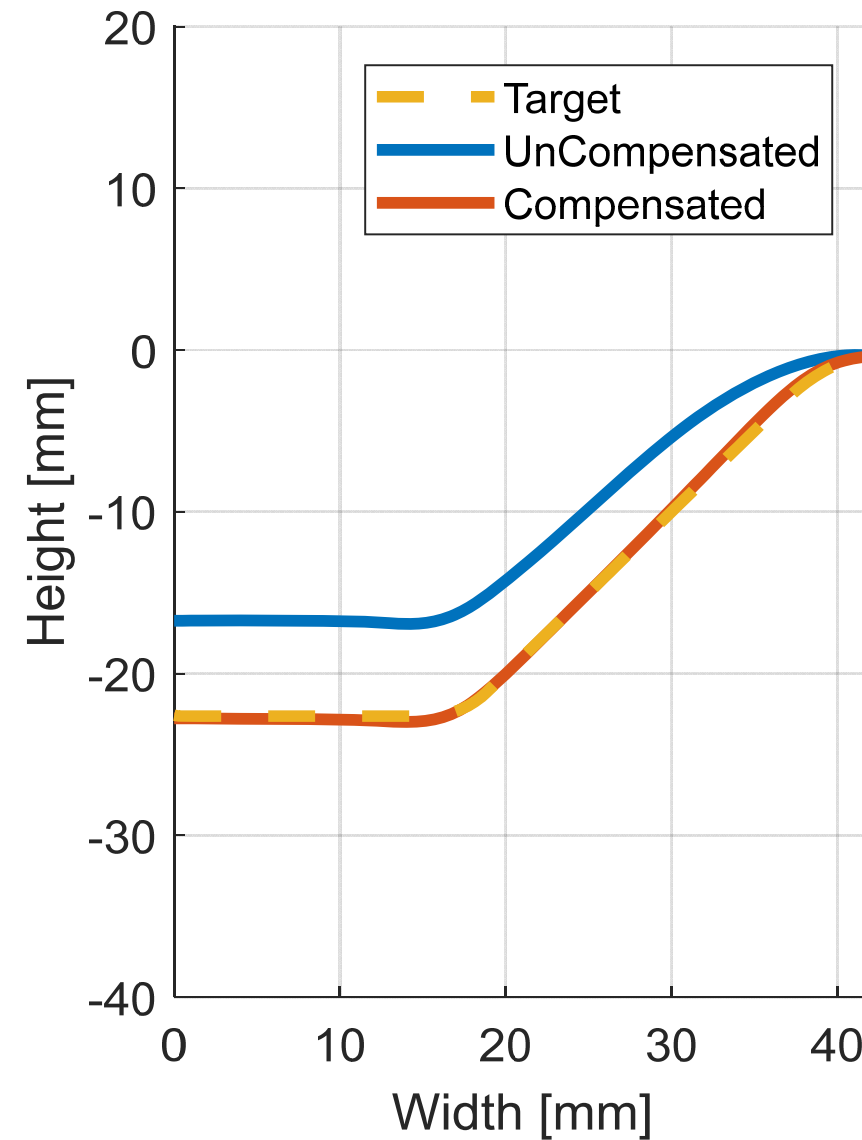
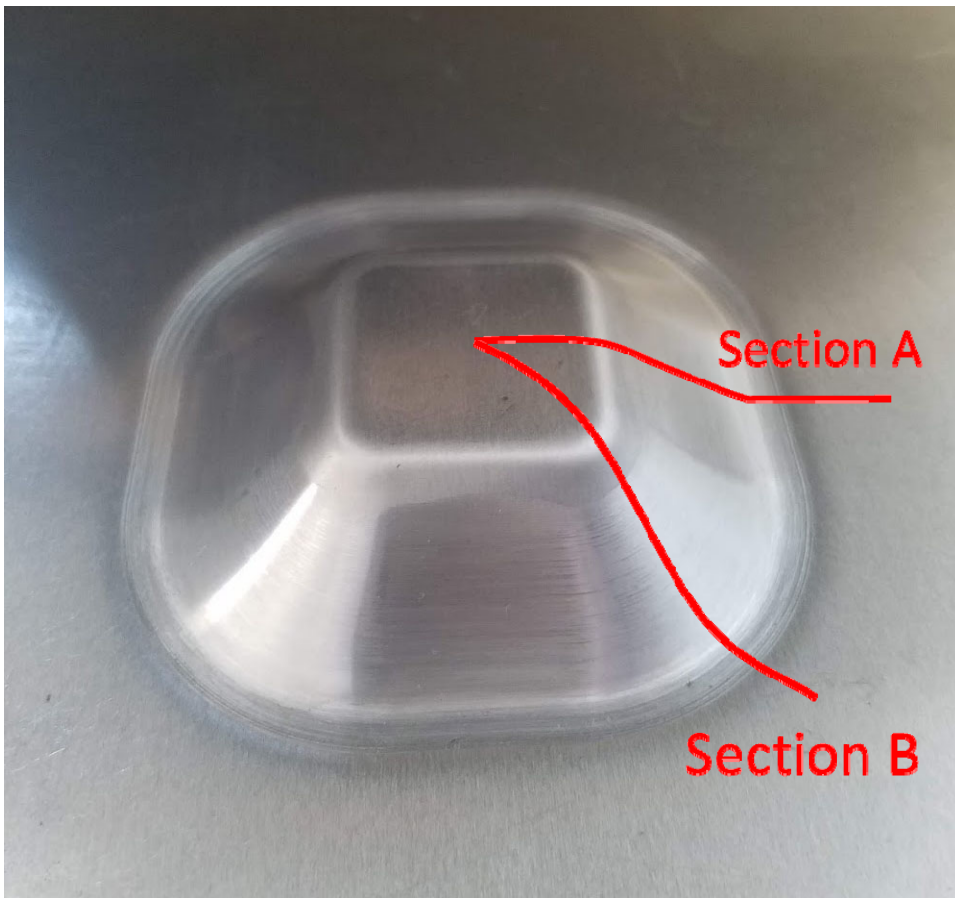
- Springback is the **elastic response** of the formed sheet due to the **change of the forming force**;
- The **forming force** can be easily measured online;



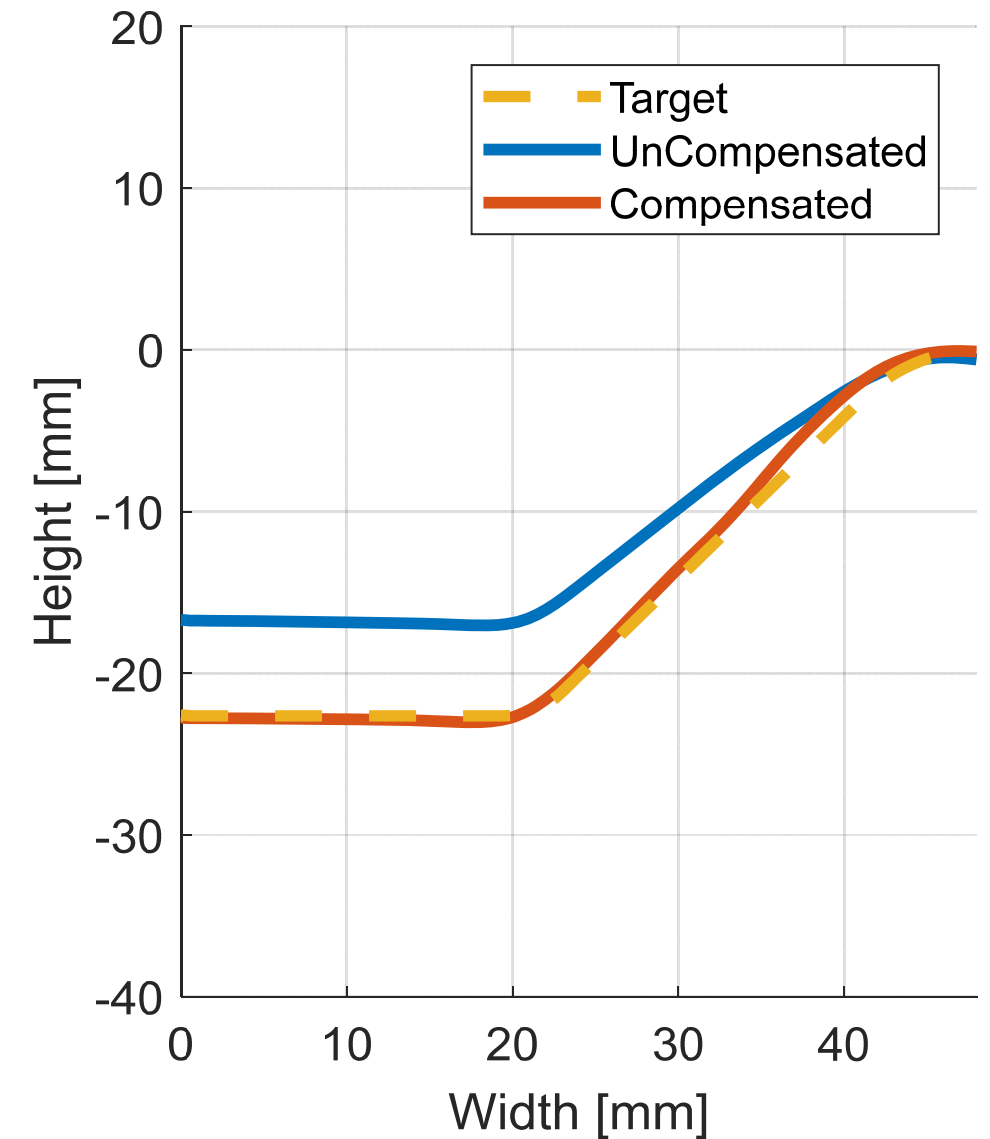
# Proposed Control System for DSIF



# Experimental Verification

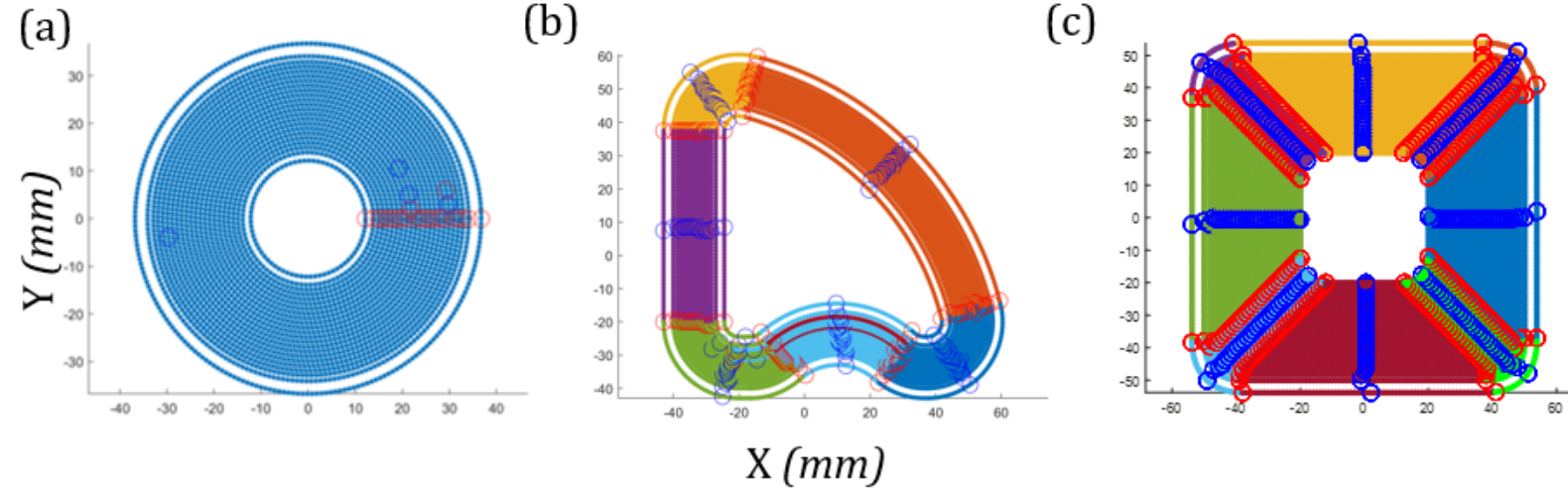


Section A



Section B

# Geometric Accuracy

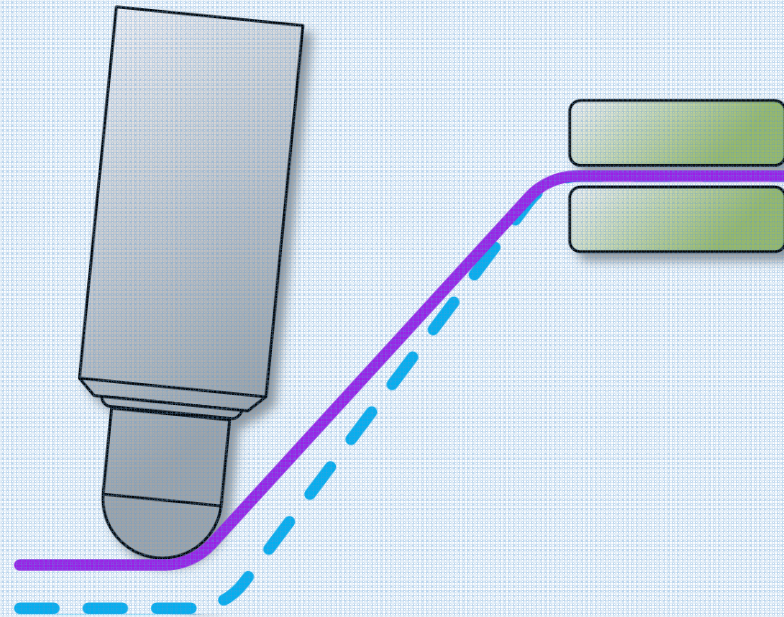


**Table 1** Comparison of geometric deviations for the test cases.

Geometry	Cone		Fish fin			Pyramid	
	Ref	SC	Ref	SC	SC+FC	Ref	SC+FC
Max. error (mm)	5.7	1.5	5.0	3.0	2.0	4.8	1.2
Avg. error (mm)	3.1	0.8	3.2	1.9	1.2	2.6	0.2

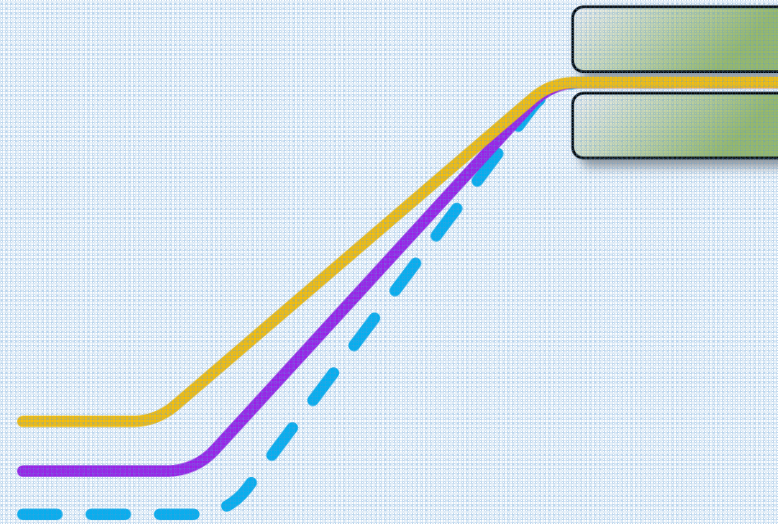
# Challenge - Geometric Accuracy

Tool/Machine Deflection



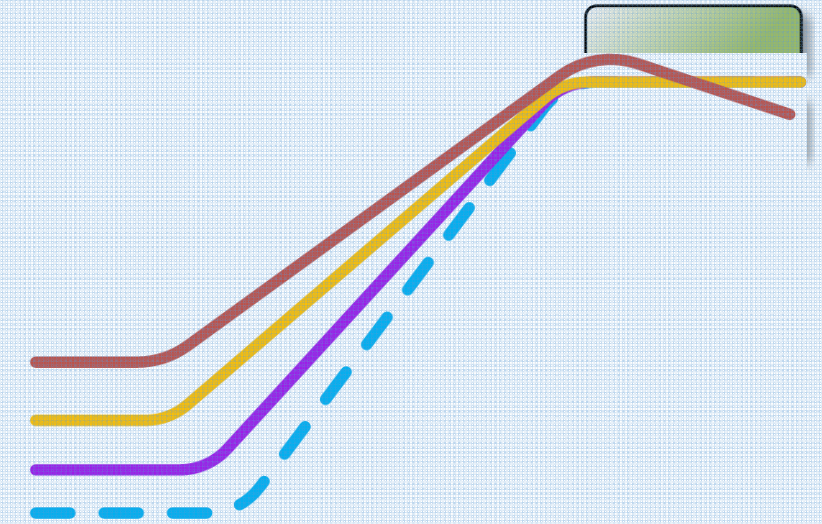
- requires **Compliance Compensation** for forming tool

In-process Springback



- requires **Springback Compensation**

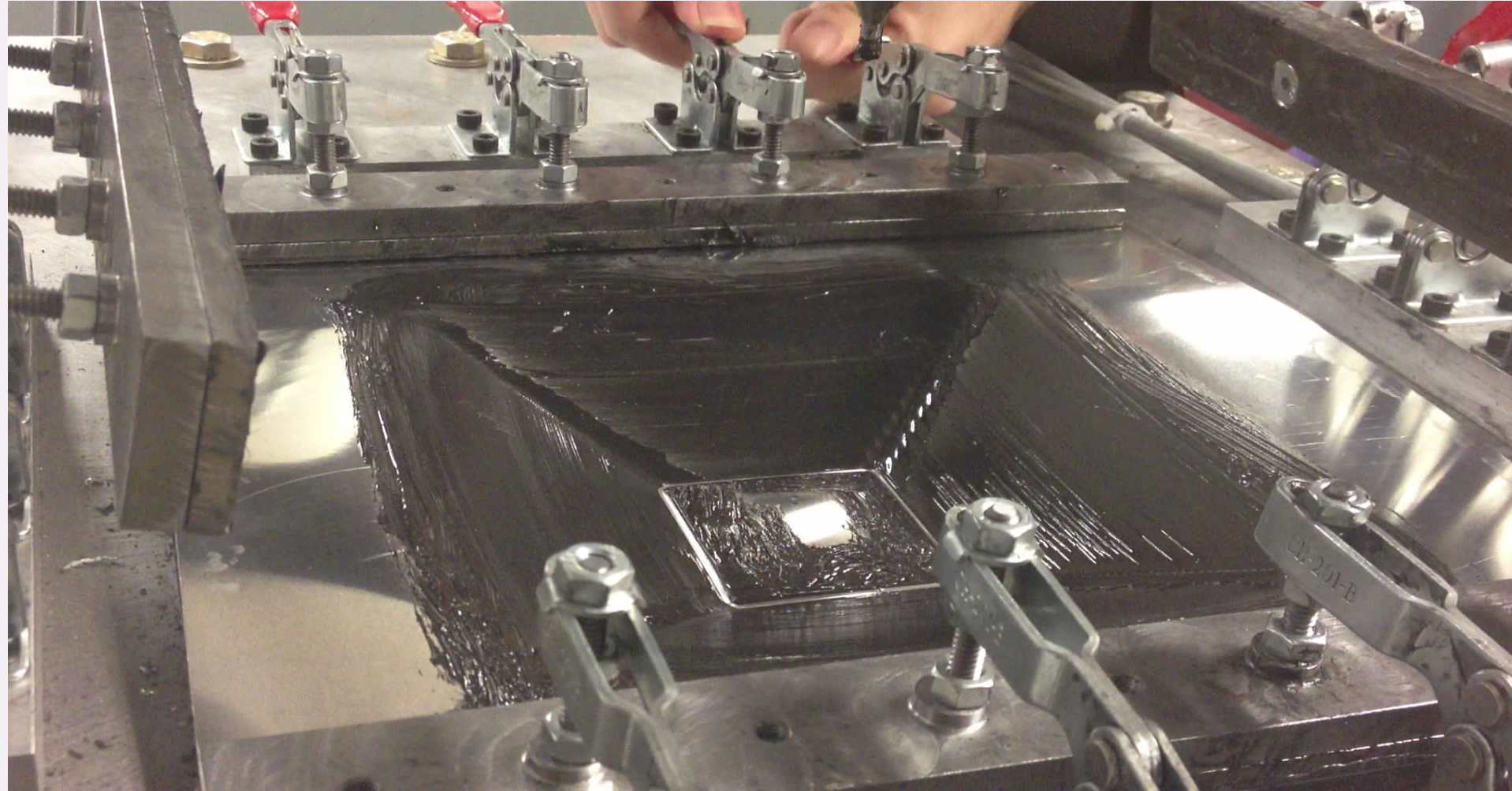
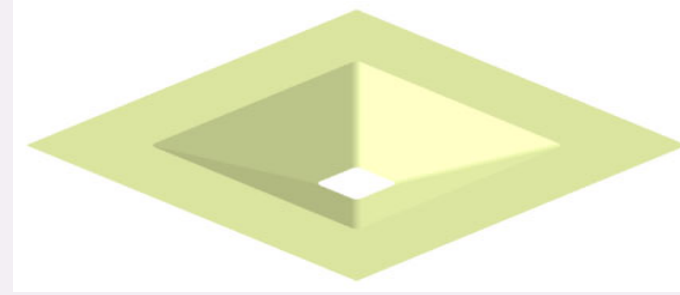
Post-process Springback



- requires **Post-annealing**

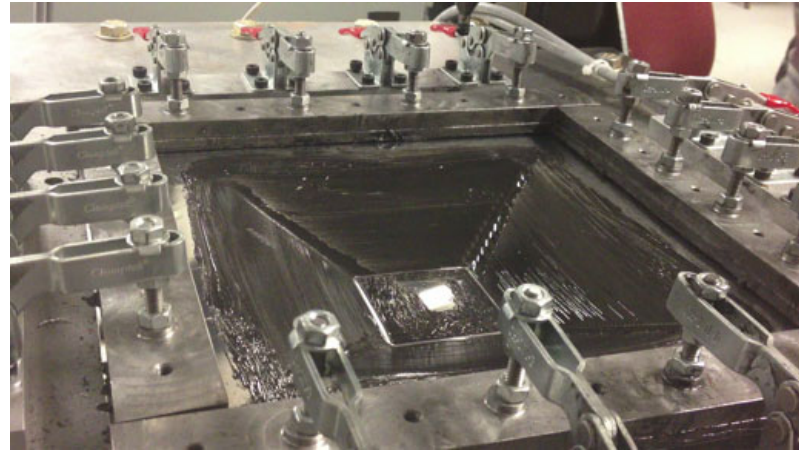
# Springback Reduction

- A universal method to significantly reduce springback due to unclamping



# Springback Reduction from Thermal Stress Relief

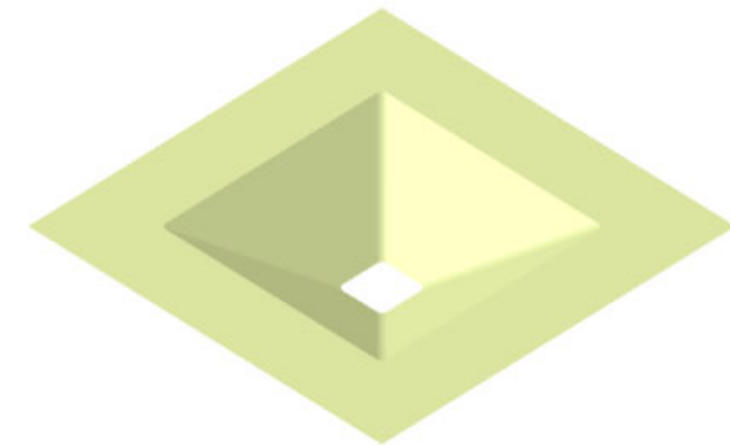
- Stage 1  
Original part within the machine clamp



- Stage 2  
Freestanding original part



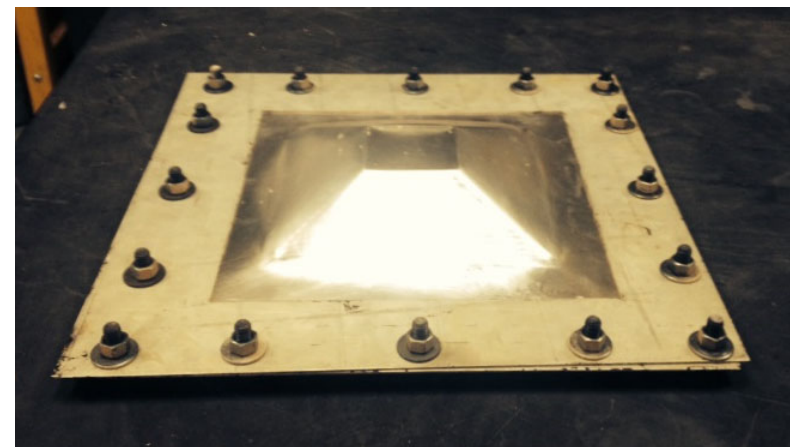
Target geometry  
(truncated pyramid)



- Stage 4  
Freestanding annealed part



- Stage 3  
Original part within the portable clamp



# Springback Evaluation

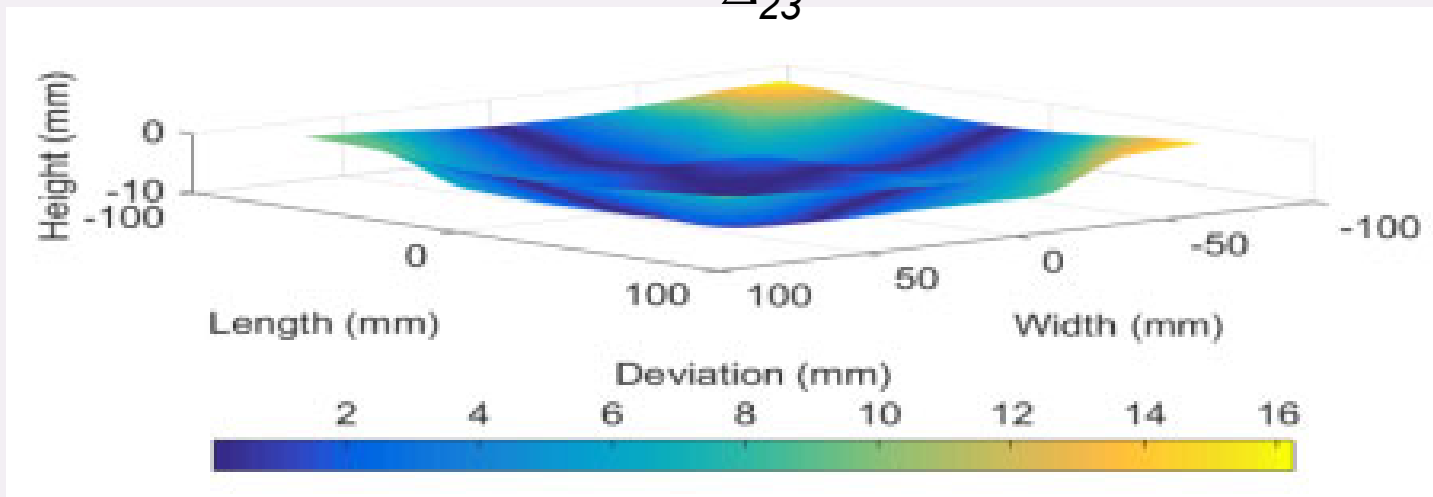


- Assume: Stage 1 = Stage 3
- Inner surface scanned by Romer Absolute Arm with an integrated laser scanner

## Stage 2



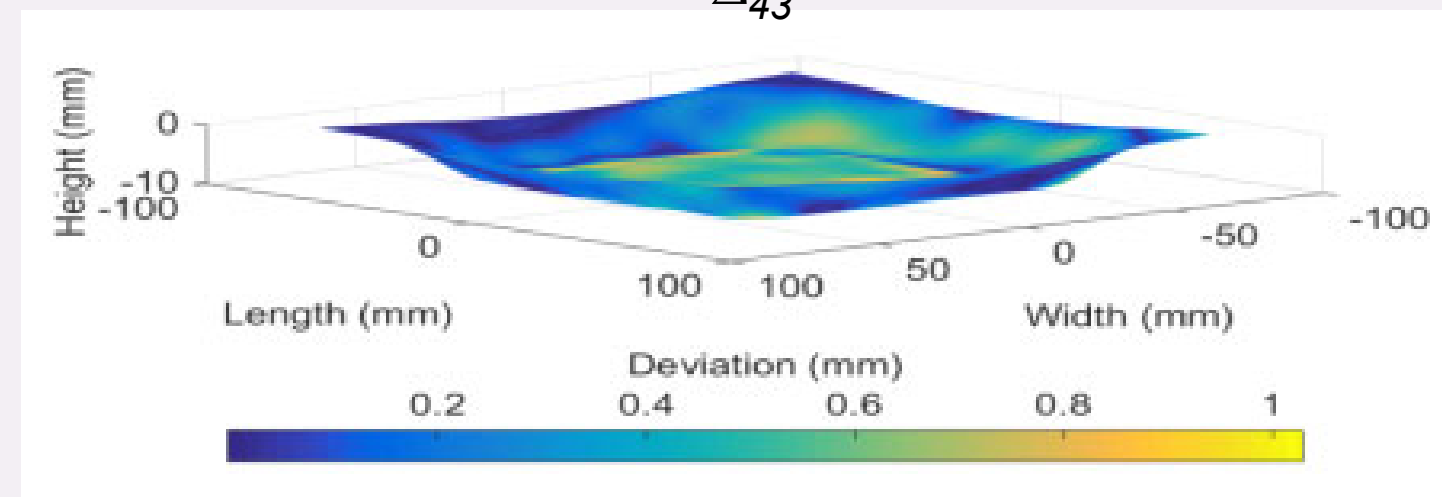
## $\Delta_{23}$



## Stage 4

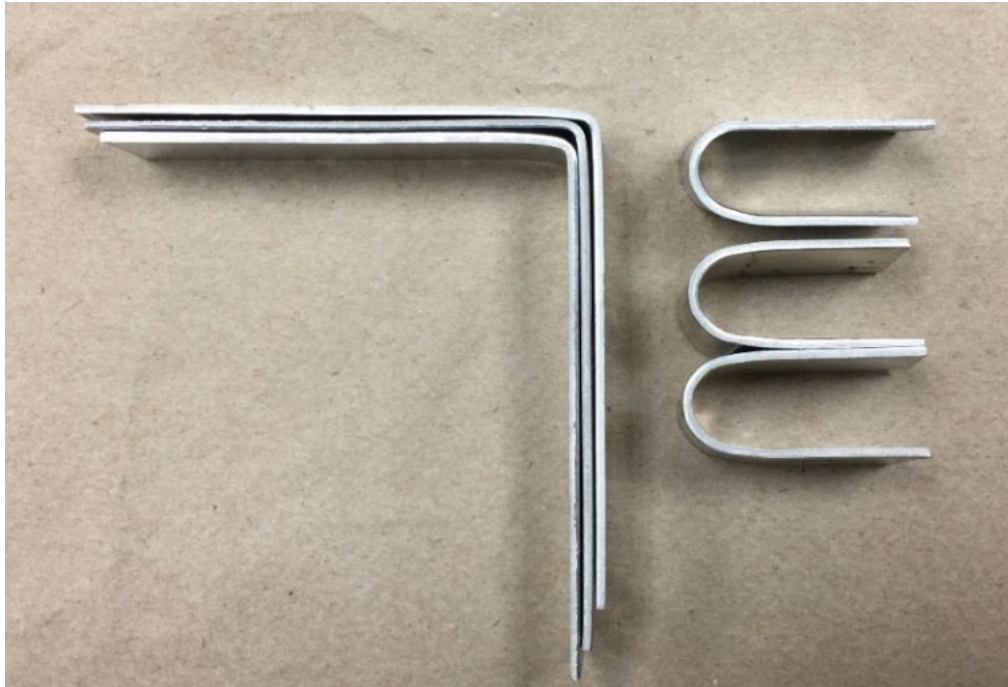


## $\Delta_{43}$



# Bending and Annealing

- Two different bending angles & four different annealing parameter sets



Annealing Parameter		Angle for 90° Bending Tests (°)	Angle for 0° Bending Tests (°)
Temp. (°C)	Time (hr)		
RT	NA	100.2 ± 0.3	17.2 ± 0.9
170	1	90.2 ± 0.8	0 ± 0
130	1	93.3 ± 0.8	0.9 ± 0.2
250	0.5	92.8 ± 0.4	1.1 ± 0.6

Selected parameters

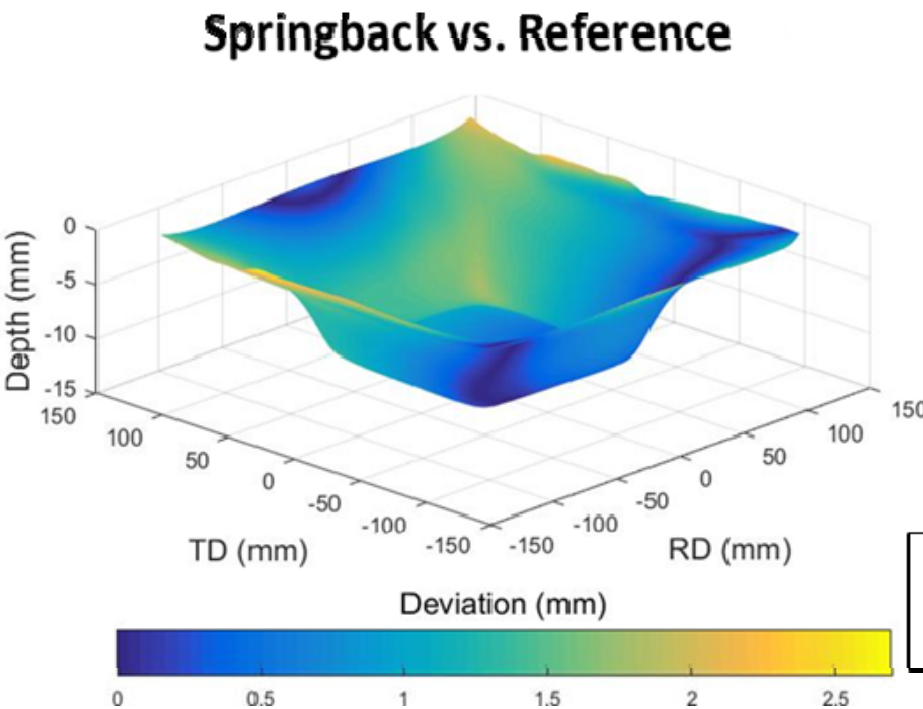
Standard stress relieve annealing for AA7075-O (SAE AMS2770)

- 1) Temperature: 333-349°C
- 2) Heat for 2 hrs
- 3) Air cool to RT



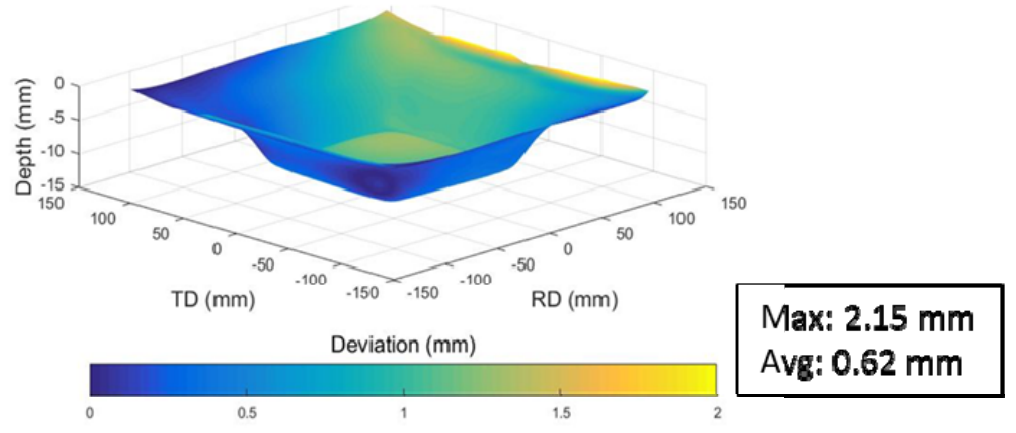
# Validation of the Selected Parameters

- 3D geometrical deviation map of a part with springback

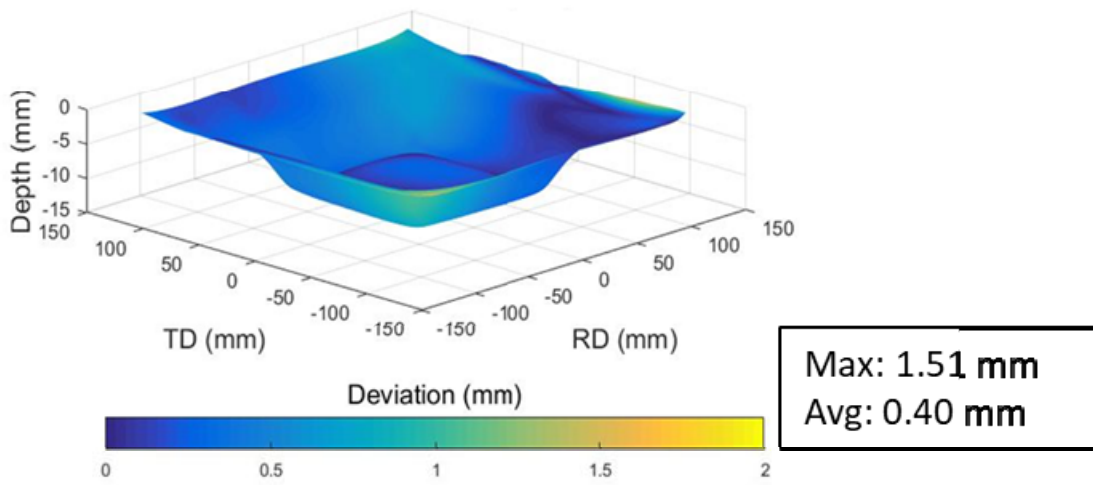


- Geometrical deviation map of the two different annealed cases

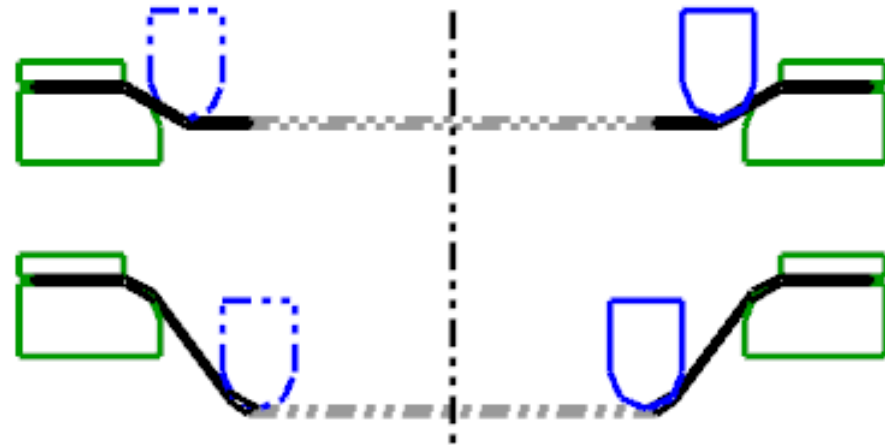
### Annealed (not clamped) vs. Reference



### Annealed (clamped) vs. Reference



## Single-sided incremental hole flanging



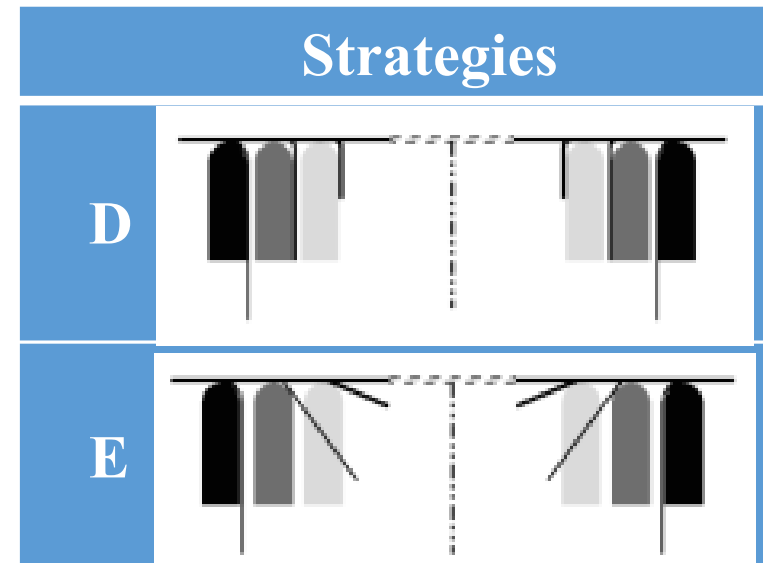
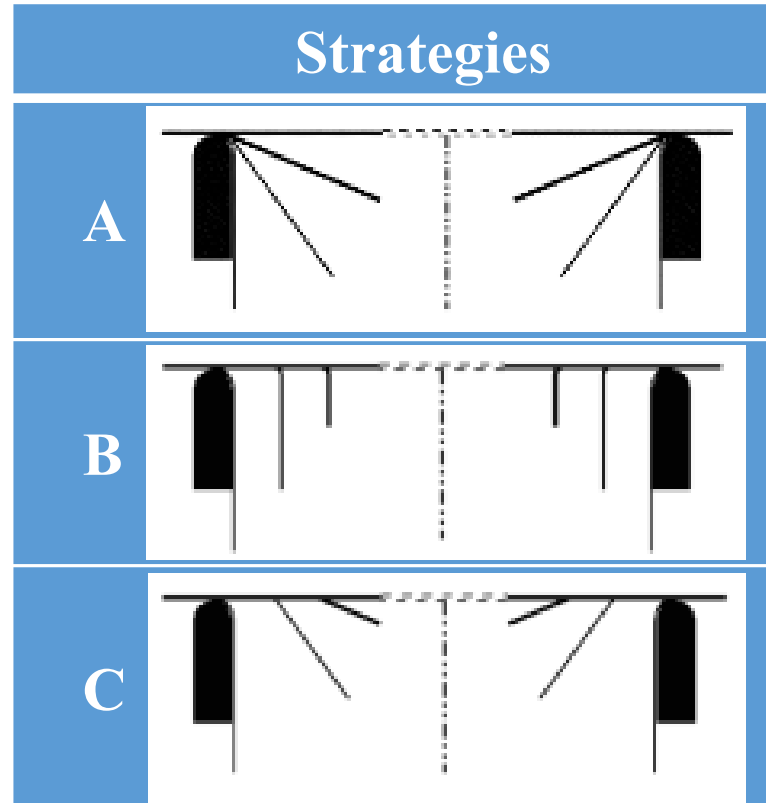
Z. Cui, L. Gao. Studies on hole-flanging process using multistage incremental forming. CIRP Journal of Manufacturing Science and Technology 2 (2010) 124-128

## Dieless double-sided incremental hole flanging (Current work)

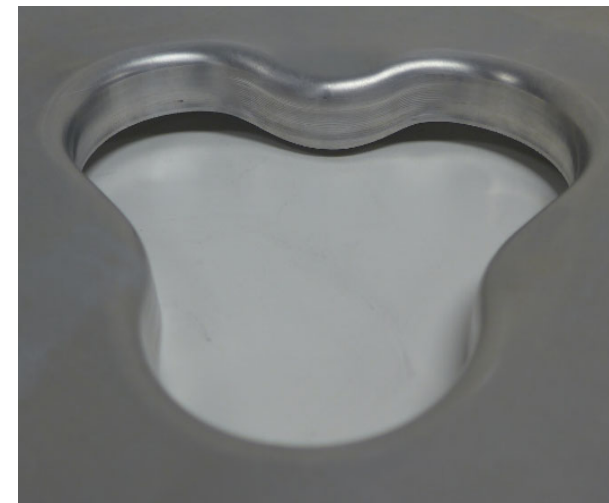
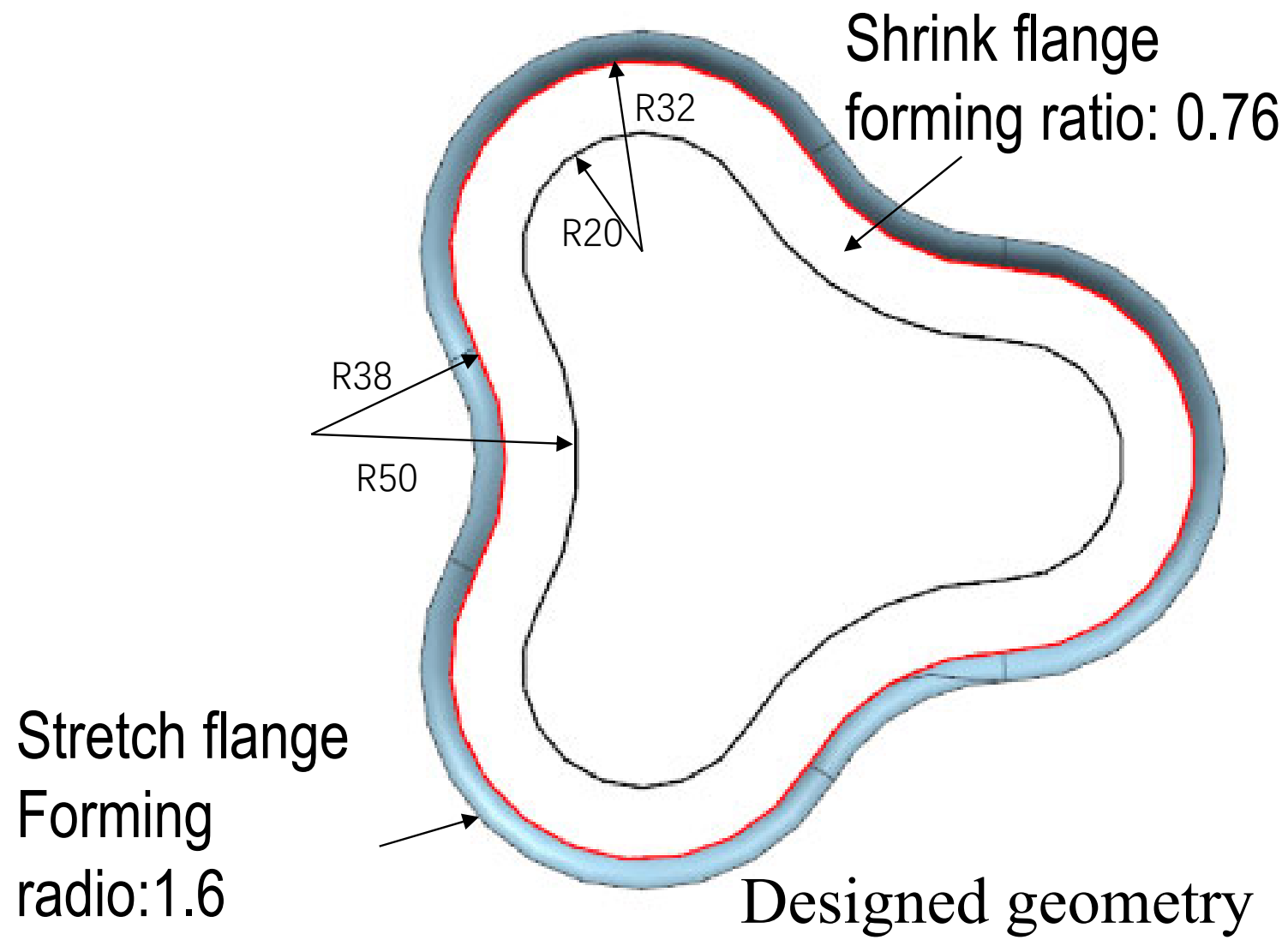


Huan Zhang, Zixuan Zhang, Huaqing Ren, Newell Moser, Jian Cao. Dieless double-sided incremental hole-flanging with different toolpath strategies. MSEC 2016-8829

# Experimental Results



# Asymmetric hole flanging experiment



Achieved part



Northwestern | McCORMICK SCHOOL OF ENGINEERING



U.S. DEPARTMENT OF ENERGY

Energy Efficiency & Renewable Energy

ADVANCED MANUFACTURING OFFICE



NIST  
National Institute of Standards and Technology  
U.S. Department of Commerce

# Thank You

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Current students: Newell Moser, Dohyun Leem, Jiayi Xie, Shuheng Liao, Zilin Jiang



AMPL Advanced Manufacturing Processes Laboratory  
AMPL.MECH.NORTHWESTERN.EDU

# Incremental Forming Publications

- 1) Ren, H., Xie, J., Liao, S., Leem, D., Ehmann, K. and Cao, J. (2019) “In-situ springback compensation in incremental sheet forming”, *CIRP Annals*, Vol. 68(1).
- 2) Ndip-Agbor, E. E., Cheng, P., Moser, N., Ehmann, K. and Cao, J. (2019) “Prediction of Rigid Body Motion in Multi-Pass Single Point Incremental Forming”, *Journal of Materials Processing Technology*, Vol. 269, pp. 117-127, [doi.org/10.1016/j.jmatprotec.2019.02.007](https://doi.org/10.1016/j.jmatprotec.2019.02.007).
- 3) Shi, Y. Zhang, W.Z., Cao, J. and Ehmann, K. F. (2019) “Experimental study of water jet incremental micro-forming with supporting dies”, *J. Materials Processing Technology*, Vol. 268, pp. 117-131, <https://doi.org/10.1016/j.jmatprotec.2019.01.012>.
- 4) Zhang, X., He, T., Miwa, H., Nanbu, T., Murakami, R., Liu, S., Cao, J. and Wang, Q. J. (2019) “A new approach for analyzing the temperature rise and heat partition at the interface of coated tool tip-sheet incremental forming systems”, *Int. J. of Heat and Mass Transfer*, Vol. 129, 1172–1183, <https://doi.org/10.1016/j.ijheatmasstransfer.2018.10.056>.
- 5) Yang, D.Y., Bambach, M., Cao, J., Duflou, J.R., Groche, P., Kuboki, T., Sterzing, A., Tekkaya, A.E., Lee, C.W. (2018) “Flexibility in metal forming”, *CIRP Annals*, Vol. 67(2), <https://doi.org/10.1016/j.cirp.2018.05.004>.
- 6) Ren, H., Li, F., Moser, N., Leem, D., Li, T., Ehmann, K. and Cao, J. (2018) “General contact force control algorithm in double-sided incremental forming”, *CIRP Annals*, Vol. 67(1), pp. 381-384, <https://doi.org/10.1016/j.cirp.2018.04.057>.
- 7) Zhang, H., Zhang, Z.X., Ren, H.Q., Cao, J. and Chen J. (2018) “Deformation mechanics and failure mode in stretch and shrink flanging by double-sided incremental forming”, *Int. J. Mechanical Sciences*, Vol. 144, 216-222, <https://doi.org/10.1016/j.ijmecsci.2018.06.002>.
- 8) Duflou, J.R., Habraken A.M., Cao, J., Malhotra, R., Bambach M., Adams D., Vanhove, H., Mohammadi A. and Jeswiet J. (2018) “Single point of incremental forming: state-of-the-art and prospects”, *Int. J. of Material Forming*, Vol. 11(6), pp. 743-773, <https://doi.org/10.1007/s12289-017-1387-y>.

# Incremental Forming Publications

- 9) Ndip-Agbor, E. E., Ehmann, K. and Cao, J. (2018) “Automated flexible forming strategy for geometries with multiple features in double-sided incremental forming”, *ASME J. of Manufacturing Science and Engineering*, Vol. 140(3), 0310041, DOI: 10.1115/1.4038511.
- 10) Cao, T., Lu, B., Cao, J. and Chen, J. (2017) “Experimental investigations on the forming mechanism of a new incremental stretch-flanging strategy with a featured tool”, *Int. J. Advanced Manufacturing Technology*, Vol. 92(5-8), pp.2953-2964, <http://dx.doi.org/10.1007/s00170-017-0355-5>.
- 11) Moser, N., Pritchett, D., Ren, H.Q., Ehmann, K.F. and Cao, J. (2016) “An efficient and general finite element model for double-sided incremental forming”, *ASME J. of Manufacturing Science and Engineering*, Vol. 138, September, 091007 (10 pages), doi:10.1115/1.4033483.
- 12) Davarpanah, M.A., Zhang, Z.X., Bansal, S., Cao, J. and Malhotra, R. (2016) “Preliminary Investigations on Double Sided Incremental Forming of Thermoplastics”, *Manufacturing Letters*, Vol. 8, pp.21-26, <http://dx.doi.org/10.1016/j.mfglet.2016.05.003>
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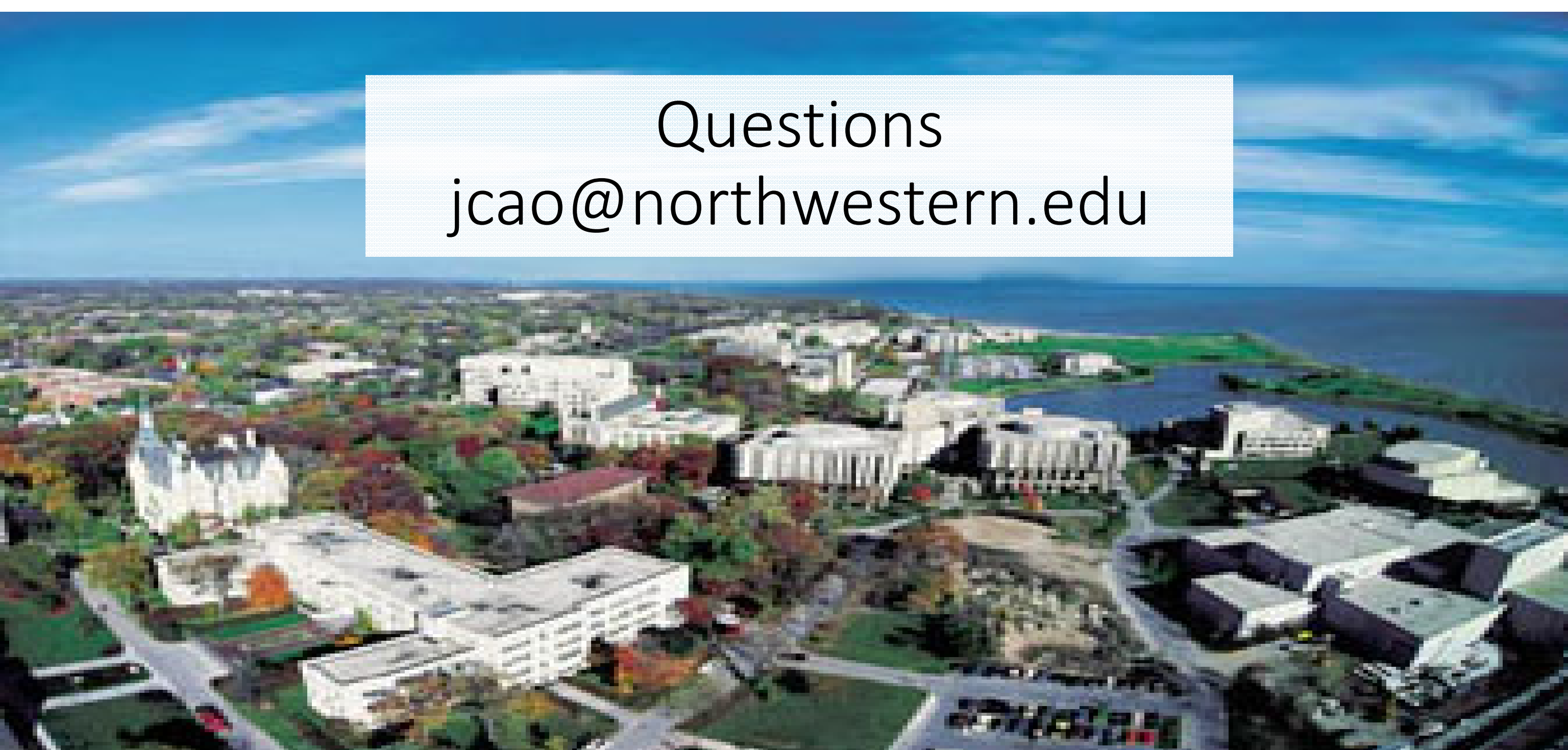


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An aerial photograph of the Northwestern University campus in Evanston, Illinois. The image shows various university buildings, green spaces, and a large lake in the background under a blue sky with light clouds. A white rectangular text box is superimposed in the upper center of the image.

Questions  
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